Advanced Molecular Dynamics

Lyopanov instability and the shadow theorem (4.3.4) Lagrangian and Hamiltonians (Appendix A) MD at constant temperature (6.1) Constraints (15.1) Computer experiments (4.4)

Contents

- Recap of the Verlet algorithms
- Lyopunov instability and the shadow theorem
- Lagrangian and Hamiltonian approach
- MD at constant temperature: Thermostats
- Constraints
- Ensemble averaging and computing static and dynamic properties
- Example of biomolecular simulation

Recap: The Verlet algorithms

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Original Verlet algorithm

$$\mathbf{r}(t + \Delta t) \approx 2\mathbf{r}(t) - \mathbf{r}(t - \Delta t) + \frac{\Delta t^2}{m}\mathbf{f}(t)$$

Downside regular verlet algorithm: velocity is not known, worse accuracy.

Velocity verlet (Andersen 1983):

$$\mathbf{r}(t + \Delta t) \approx \mathbf{r}(t) + \mathbf{v}(t)\Delta t + \frac{\Delta t^2}{2m}\mathbf{f}(t)$$
$$\mathbf{v}(t + \Delta t) \approx \mathbf{v}(t) + \frac{\Delta t}{2m}[\mathbf{f}(t + \Delta t) + \mathbf{f}(t)]$$

(Is based on Trotter decomposition of Liouville operator formulation, also basis of Multiple time steps).

Velocity Verlet has the advantage of allowing multiple time stepping

Is Verlet a good algorithm?

Verlet algorithm

- is time reversible
- does conserve volume in phase space
- (is "symplectic")
- does not suffer from energy drift

...but is it a good algorithm?

i.e. does it predict the time evolution of the system correctly???

Molecular chaos

Dynamics of "well-behaved" classical many-body system is chaotic.

Consequence: Trajectories that differ very slightly in their initial conditions diverge exponentially ("Lyapunov instability")



Lyapunov instability

The Lyapunov disaster in action...



Any small error in the numerical integration of the equations of motion, will blow up exponentially....

always...

...and for any algorithm!!

SO:

Why should anyone believe Molecular Dynamics simulations ???

Answers:

- 1. In fact, one should not...
- Good MD algorithms (e.g. Verlet) can also be considered as good Monte Carlo algorithms –they therefore yield reliable STATIC properties ("Hybrid Monte Carlo")
- 3. What is the point of simulating dynamics, if we cannot trust the resulting time-evolution???
- 4. All is well (probably), because of...The Shadow Theorem.

Shadow theorem

- For any realistic many-body system, the shadow theorem is merely a hypothesis.
- It basically states that Good algorithms generate numerical trajectories that are "close to" a REAL trajectory of the many-body system.
- Question: Does the Verlet algorithm indeed generate "shadow" trajectories?
- Take a different look at the problem.
 - Do not discretize NEWTON's equation of motion...
 - ...but discretize the ACTION

Lagrangian Classical mechanics

X

t=0

 $S \leq S$

S<*S*

Newton:
$$F_i = m_i \frac{d^2 x_i(t)}{dt^2}$$

- Lagrange:
 - Consider a system that is at a point r₀ at time t=0 and at point r_t at time t=t, then the system follows a trajectory r(t) such that:

$$S \equiv \int_0^t dt' \mathcal{L}(r(t'))$$

is an extremum. The Lagrangian L is defined as:

$$\mathcal{L}(r(t)) = K - U(r)$$
 kinetic energy

Langrangian

For example, if we use cartesian coordinates:

$$\mathcal{L}(r(t)) = \sum_{i=1}^{N} \frac{1}{2} m_i \dot{r}_i^2 - U(r_1, r_2, \dots r_N)$$

What does this lead to?

Consider the "true" path R(t), with R(0)= r_0 and R(t)= r_t . Now, consider a path close to the true path:

$$r(t') = R(t') + \delta r(t')$$

Then the action S is an extremum if

$$\frac{\partial S}{\partial r(t')} = 0 \text{ for all } t$$

What does this lead to?

Discretized action

$$S_{cont} = \int_{t_0}^{t_1} dt \mathcal{L}(t)$$
$$S_{disc} = \Delta t \sum_{i=0}^{i_{max}} \mathcal{L}(t_i)$$

$$\mathcal{L}(t_i) = K(t_i) - U(t_i)$$

For a one dimensional system this becomes

$$\mathcal{L}(t_i)\Delta t = \frac{1}{2}m\Delta t \frac{(x_{i+1} - x_i)^2}{\Delta t^2} - U(x_i)\Delta t$$
$$S_{disc} = \sum_{i=1}^{i_{max}} \left[\frac{m(x_{i+1} - x_i)^2}{2\Delta t} - U(x_i)\Delta t\right]$$

Minimize the action

Now do the standard thing: Find the extremum for small variations in the path, i.e. for small variations in all x_i .

$$\frac{\partial S_{disc}}{\partial x_i} = 0 \text{ for all } i$$

This will generate a discretized trajectory that starts at time t_0 at X, and ends at time t at X_t .



Minimizing the action

$$\frac{\partial S_{disc}}{\partial x_i} = \frac{\partial}{\partial x_i} \sum_{i=1}^{i_{max}} \left[\frac{m(x_{i+1} - x_i)^2}{2\Delta t} - U(x_i)\Delta t \right]$$

$$\frac{\partial S_{disc}}{\partial x_i} = \frac{-m(x_{i+1} - x_i) + m(x_i - x_{i-1})}{\Delta t} - \Delta t \frac{\partial U(x_i)}{\partial x_i}$$

$$0 = \frac{m}{\Delta t} \left(2x_i - x_{i+1} - x_{i-1} - \frac{\Delta t^2}{m} \frac{\partial U(x_i)}{\partial x_i} \right)$$

$$0 = 2x_i - x_{i+1} - x_{i-1} - \frac{\Delta t^2}{m} \frac{\partial U(x_i)}{\partial x_i}$$

$$x_{i+1} = 2x_i - x_{i-1} + \frac{\Delta t^2}{m} F(x_i)$$

- which is the Verlet algorithm!
- The Verlet algorithm generates a trajectory that satisfies the boundary conditions of a REAL trajectory –both at the beginning and at the endpoint.
- Hence, if we are interested in statistical information about the dynamics (e.g. time-correlation functions, transport coefficients, power spectra...)
 ...then a "good" MD algorithm (e.g. Verlet) is fine.

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Lagrangian approach

Lagrangian is sum of two terms

$$\mathcal{L}(\dot{r},r) = K(\dot{r}) - U(r) = \frac{m\dot{r}^2}{2} - U(r)$$

$$\frac{\partial \mathcal{L}}{\partial \dot{r}} = \frac{\partial K}{\partial \dot{r}} = p \qquad \qquad \frac{\partial \mathcal{L}}{\partial r} = -\frac{\partial U}{\partial r} = F$$

$$p = \frac{\partial \mathcal{L}(\dot{r}, r)}{\partial \dot{r}} \qquad \qquad \dot{p} = \frac{\partial \mathcal{L}(\dot{r}, r)}{\partial r}$$
Newton : F=ma

Hamiltonian approach



Hamiltonian approach

The Hamiltonian is defined as

$$\begin{split} H(p,r) &= p\dot{r} - \mathcal{L}(\dot{r},r) \\ H(p^N,r^N) &= U(r^N) + \sum_i \frac{p_i^2}{2m_i} \end{split}$$

Hamilton's equations are then

$$\dot{r} = \frac{\partial \mathcal{H}(r,p)}{\partial p} = \frac{p}{m}$$

$$\dot{p} = -\frac{\partial \mathcal{H}(r,p)}{\partial r} = -\frac{\partial U(r^N)}{\partial r}$$

Integrating equations of motion (by Verlet) conserves the Hamiltonian

Conservation of Hamiltonian

$$\begin{aligned} dH(p,r) &= \frac{\partial H}{\partial p} dp + \frac{\partial H}{\partial r} dr \\ \frac{\partial H}{\partial p} &= \dot{r} \qquad \frac{\partial H}{\partial r} = -\dot{p} \\ \frac{dH(p,r)}{dt} &= \frac{\partial H}{\partial p} \dot{p} + \frac{\partial H}{\partial r} \dot{r} = \dot{r} \dot{p} - \dot{p} \dot{r} = 0 \end{aligned}$$

So a solution to the Hamiltonians equation conserves the TOTAL energy

$$E = K + U$$

MD generates the NVE ensemble

How do we sample the canonical ensemble with MD?

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Constant Temperature: a naïve approach

Velocity scaling

$$\frac{3}{2}k_B T = \frac{1}{N}\sum_{i=1}^N \frac{1}{2}mv_i^2$$
$$v_i \to v_i \sqrt{\frac{T_{\text{req}}}{T}}$$

This is called the **isokinetic** thermostat

Does not sample the canonical ensemble!

Thermostat: From NVE to NVT

- Introduce proper thermostat in MD trajectory:
- deterministic thermostat:
 - Nose-Hoover
- stochastic thermostats:
 - Andersen
 - Langevin
 - Bussi
 - Nose Hoover- Langevin

All of these alter the velocities such that the trajectory samples the canonical NVT ensemble, and the partition function becomes

$$Q = \frac{1}{N!\Lambda^{3N}} \int e^{-\beta \mathcal{U}(r)} dr$$

These thermostats differ in how they achieve this

Andersen Thermostat

• Every particle has a fixed probability to collide with the Andersen demon

• After collision the particle is give a new velocity

$$P(v) = \left(\frac{\beta}{2\pi m}\right)^{3/2} \exp\left[-\beta m v^2/2\right]$$



 The probabilities to collide are uncorrelated (Poisson distribution)

$$P(t;v) = v \exp\left[-vt\right]$$

Algorithm 14 (Molecular Dynamics: Andersen Thermostat)

```
MD at constant temperature
program md_Andersen
                                                                          initialization
call init (temp)
                                                                          determine the forces
call force(f,en)
t=0
                                                                          MD loop
do while (t.lt.tmax)
                                                                          first part of the eqs. of motion
       call integrate(1, f, en, temp)
                                                                          determine the forces
      call force(f,en)
                                                                          second part of eqs. of motion
      call integrate(2, f, en, temp)
      t=t+dt
                                                                          sample averages
      call sample
enddo
stop
end
                                                       \begin{aligned} \mathbf{r}(\mathbf{t} + \Delta \mathbf{t}) &= \mathbf{r}(\mathbf{t}) + \mathbf{v}(\mathbf{t})\Delta \mathbf{t} + \frac{\mathbf{f}(\mathbf{t})}{2\mathbf{m}}\Delta \mathbf{t}^2 \\ \mathbf{v}(\mathbf{t} + \Delta \mathbf{t}) &= \mathbf{v}(\mathbf{t}) + \frac{\mathbf{f}(\mathbf{t} + \Delta \mathbf{t}) + \mathbf{f}(\mathbf{t})}{2\mathbf{m}}\Delta \mathbf{t}. \end{aligned}
```

Algorithm 15 (Equations of Motion: Andersen Thermostat)



Andersen thermostat: static properties



Andersen thermostat: dynamic properties



Velocity rescaling revisited

- The Andersen thermostat samples the correct ensemble, but is rather violent • to the dynamics.
- The **Bussi** thermostat combines rescaling with a stochastic approach: •
 - Evolve a single time step with a symplectic integrator e.g. velocity Verlet
 - Calculate the kinetic energy K_t .
 - Evolve the kinetic energy $K_t = K_t + dK$ for a single time step using an auxiliary continuo

Wiener noise term

$$dK = (\bar{K} - K)\frac{dt}{\tau} + 2\sqrt{\frac{K\bar{K}}{N_f}}\frac{dW}{\sqrt{\tau}}$$

Rescale the velocities so as to enforce thi energy K_t.

$$\alpha = \sqrt{\frac{K_t}{K}}$$

relaxation time parameter

Bussi thermostat

Solving the differential equation

$$dK = (\bar{K} - K)\frac{dt}{\tau} + 2\sqrt{\frac{K\bar{K}}{N_f}}\frac{dW}{\sqrt{\tau}}.$$

gives

$$\begin{aligned} \alpha^{2} &= e^{-\Delta t/\tau} + \frac{\bar{K}}{N_{f}K} (1 - e^{-\Delta t/\tau}) (R_{1}^{2} + \sum_{i=2}^{N_{f}} R_{i}^{2}) \\ &+ 2e^{-\Delta t/2\tau} \sqrt{\frac{\bar{K}}{N_{f}K} (1 - e^{-\Delta t/\tau})} R_{1}. \end{aligned} \tag{Bus}$$

(Bussi et al 2007)

Where the Ri are independent Gaussian random numbers

Nose Hoover thermostat



Nose-Hoover Thermostat

$$\mathcal{H}_{\text{Nose}} = \sum_{i=1}^{N} \frac{p_i^2}{2ms^2} + \frac{p_s}{2Q} + U(r^N) + \frac{g}{\beta} \ln s$$

equations of motion follow from Hamilton's equations.

$$\frac{\mathrm{d}r_{i}}{\mathrm{d}t} = \frac{\partial \mathcal{H}_{\mathrm{Nose}}}{\partial p_{i}} = \frac{p_{i}}{ms^{2}} \qquad \frac{\mathrm{d}p_{i}}{\mathrm{d}t} = -\frac{\partial \mathcal{H}_{\mathrm{Nose}}}{\partial r_{i}} = -\frac{\partial U(r^{N})}{\partial r_{i}}$$
$$\frac{\mathrm{d}s}{\partial t} = \frac{\partial \mathcal{H}_{\mathrm{Nose}}}{\partial p_{s}} = \frac{p_{s}}{Q} \qquad \frac{\mathrm{d}p_{s}}{\mathrm{d}t} = -\frac{\partial \mathcal{H}_{\mathrm{Nose}}}{\partial s} = \frac{1}{s} \left(\sum \frac{p_{i}^{2}}{ms^{2}} - \frac{g}{\beta} \right)$$

Nose Hoover implementation

NH equation of motion can be rewritten as (Hoover 1984)

$$\dot{\mathbf{r}}_{i} = \mathbf{p}_{i}/m_{i}$$
$$\dot{\mathbf{p}}_{i} = \mathbf{f}_{i} - \xi \mathbf{p}_{i}$$
$$\dot{\xi} = \left(\sum_{i} p_{i}^{2}/m_{i} - 3N/\beta\right)/Q$$

Where $\xi = p_s/Q$ now denotes a kind of 'friction' term

Mass Q determines the damping

Effect of mass Q

Lennard-Jones fluid



mean square displacement

temperature relaxation

Nose Hoover Langevin thermostat

- Nose Hoover is not ergodic (NH Chains can alleviate this)
- Better option might be Nose-Hoover-Langevin (Leimkuhler 2012)

$$\dot{q} = p \qquad \mu \text{ is mass}$$

$$\dot{p} = f(q) - \xi p$$

$$\dot{\xi} = (p^2 - k_B T) / \mu - \gamma \xi + \sigma \dot{w}$$

• Newton, Nosé-Hoover, Ornstein-Uhlenbeck

Friction and noise term

• Trotter formula, e.g.:

$$egin{aligned} e^{-\Delta t \hat{L}} &pprox & e^{-(\Delta t/2) \hat{L}_{\mathsf{NH}}} + e^{-(\Delta t/2) \hat{L}_{p}} + e^{-(\Delta t/2) \hat{L}_{q}} + e^{-\Delta t \hat{L}_{\mathsf{OU}}} \ &+ e^{-(\Delta t/2) \hat{L}_{q}} + e^{-(\Delta t/2) \hat{L}_{p}} + e^{-(\Delta t/2) \hat{L}_{\mathsf{NH}}} \end{aligned}$$

• with: $\hat{L} = \hat{L}_q + \hat{L}_p + \hat{L}_{NH} + \hat{L}_{OU}$ and $P(p,q;t+\Delta t) = e^{-\Delta t \hat{L}} P(p,q;t)$

Implementation of NHL thermostat

(Leimkuhler 2012)
$$c_1 = \exp(-\gamma \frac{\Delta t}{2})$$
 $c_2 = \sqrt{\frac{2k_{\rm B}T}{\mu}(1-c_1^2)}$

$$\begin{split} \xi &:= c_1 \xi + c_2 R\\ p &:= e^{-\xi \Delta t/2} p\\ p &:= p + \frac{\Delta t}{2} f(q)\\ q &:= q + \frac{\Delta t}{2} p\\ \xi &:= \xi + \Delta t (2E_{\text{kin}} - N_f k_{\text{B}} T)/\mu\\ q &:= q + \frac{\Delta t}{2} p \end{split}$$

force call

$$p := p + \frac{\Delta t}{2} f(q)$$

 $p := e^{-\xi \Delta t/2} p$
 $\xi := c_1 \xi + c_2 R$

Note the similarity to Velocity rescaling (Bussi)

Constant Pressure

- The pressure can be kept constant using a similar extended Lagrangian formalism as the Nose Hoover thermostat.
- rectangular boxes
 - Andersen barostat,
 - Martyna-Tuckerman-Klein barostat,
 - Nosé-Hoover Langevin barostat
- variable box shape
 - Parrinello Rahman barostat

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Ensemble averages by ergodicity

time averages over a NVT MD trajectory

$$\bar{A} = \frac{1}{\mathcal{T}} \int_0^{\mathcal{T}} A(t) dt$$

ensemble average

$$\langle A \rangle = \frac{\int dr^N A(r^N) \exp(-\beta \mathcal{U}(r^N))}{\int dr^N \exp(-\beta \mathcal{U}(r^N))}$$

Ergodicity theorem states that for an 'ergodic system'

$$\bar{A} = \langle A \rangle$$

Computing equilibrium properties

Ensemble averages follow from time averages

$$\langle A \rangle = \bar{A} = \frac{1}{\mathcal{T}} \int_0^{\mathcal{T}} A(t) dt$$

Temperature follows from equipartition: $\frac{1}{2} k_B T$ per d.o.f.

$$T = \frac{\left\langle 2K \right\rangle}{k_B f} \qquad \qquad K = \frac{1}{2} \sum_{i=1}^N m v_i^2$$

Where f is number of degrees of freedom

Pressure follows from virial expression

$$P = \frac{Nk_BT}{V} + \frac{1}{3V} \left\langle \sum_{i < j}^{N} \mathbf{f}_{ij} \mathbf{r}_{ij} \right\rangle$$

Computing free energy landscape

Statistical mechanics gives us

$$F = -k_B T \ln Q = -k_B T \ln \int dr^N e^{-\beta U(r^N)}$$

Project free energy on collective variable q

$$F(q) = -k_B T \ln \int dr^N \delta(q - q(r^N)) e^{-\beta U(r^N)}$$
$$F(q) = -k_B T \ln \langle \delta(q - q(r^N)) \rangle$$
$$= -k_B T \ln P(q)$$

The result is a Landau free energy

This can be generalized to multiple dimensions

$$\beta F(x,y) = -\ln P(x,y)$$



Transport coefficients: Diffusion

Diffusion equation (Fick's second law)

$$\frac{\partial c(x,t)}{\partial t} = D \frac{\partial^2 c(x,t)}{\partial x^2}$$

Solution for an initial $c(x,0)=\delta(0)$: all molecules at origin

$$c(x,t) = \frac{1}{\sqrt{4\pi Dt}} \exp\left(-\frac{x^2}{4Dt}\right)$$

Mean square displacement of the molecules

$$\langle x^2(t) \rangle = \frac{\int dx x^2 c(x,t)}{\int dx c(x,t)} = \int dx \frac{x^2 e^{-\frac{x^2}{4Dt}}}{\sqrt{4\pi Dt}} = 2Dt$$

Time derivative gives

$$2D = \lim_{t \to \infty} \frac{d\left\langle x^2(t) \right\rangle}{dt}$$

Diffusion in 3 dimensions

$$D = \frac{1}{6} \lim_{t \to \infty} \frac{d \langle \mathbf{r}^2(t) \rangle}{dt}$$

Relation to velocity

 \rangle .

Relation to velocity

$$\Delta x(t) = \int_0^t dt' v_x(t').$$

$$\left\langle x^2(t) \right\rangle = \left\langle \left(\int_0^t dt' v_x(t') \right)^2 \right\rangle$$

$$= \int_0^t \int_0^t dt' dt'' \left\langle v_x(t') v_x(t'') \right\rangle$$

$$= 2 \int_0^t \int_0^{t'} dt' dt'' \left\langle v_x(t') v_x(t'') \right\rangle.$$

$$\left\langle v_x(t') v_x(t'') \right\rangle = \left\langle v_x(t'-t'') v_x(0) \right\rangle.$$

$$\frac{\partial \langle x^2(t) \rangle}{\partial t} = 2 \frac{\partial}{\partial t} \int_0^t dt' \int_0^{t'} dt'' \langle v_x(t') v_x(t'') \rangle$$
$$\left\langle v_x(t') v_x(t'') \right\rangle = \left\langle v_x(t'-t'') v_x(0) \right\rangle.$$
$$2D = \lim_{t \to \infty} 2 \int_0^t dt'' \left\langle v_x(t-t'') v_x(0) \right\rangle$$

Define $\tau = t - t$ "

$$D = \int_0^\infty d\tau \, \langle v_x(\tau) v_x(0) \rangle$$

Green – Kubo relation

Also exists for other transport coefficients, such as viscosity and conductivity

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All-atom force fields for biomolecules

• Potential energy for protein

$$V(\mathbf{r}) = \sum_{bonds} k_r (r - r_{eq})^2 + \sum_{angles} k_{\theta} (\theta - \theta_{eq})^2 + \sum_{dihedrals} \frac{1}{2} v_n (1 + \cos(n\phi - \phi_0))$$
$$+ \sum_{i < j} \left(\frac{a_{ij}}{r_{ij}^{12}} - \frac{b_{ij}}{r_{ij}^6} + \frac{q_i q_j}{\varepsilon r_{ij}} \right)$$

vdW interactions only between non-bonded |i-j|>4

Ewald sums

Coloumb interaction

$$U_{Coul} = \frac{1}{2} \sum_{i=1}^{N} q_i \phi(r_i)$$

- With $\phi(r)$ the electrostatic potential at position r

$$\phi(r_i) = \sum_{j,\mathbf{n}} \frac{q_j}{\left|r_{ij} + \mathbf{n}L\right|}$$

- The sum runs over all periodic images n
- This equation does converge poorly.



- The trick of the Ewald sum is to add a screened potential of the opposite sign, such each charge q is canceled
- A direct sum of the screened potentials converges much quicker.

- Thus 3 contributions
 - Direct sum of point charges q with Gaussian screening with charge (converges quickly)
 - Compensating screening with charge q (can be represented by a Fourier series)
 - Self energy correction

$$U_{coul} = \frac{1}{2V} \sum_{k \neq 0} \frac{4\pi}{k^2} |\rho(k)|^2 \exp(-k^2 / 4\alpha) - \left(\frac{\alpha}{\pi}\right)^{1/2} \sum_{1=0}^{N} q_i^2 + \frac{1}{2} \sum_{i \neq j}^{N} \frac{q_i q_j erfc(\sqrt{\alpha}r_{ij})}{r_{ij}}$$

Currently available empirical force fields

- CHARMm (MacKerrel et 96)
- AMBER (Cornell et al. 95)
- GROMOS (Berendsen et al 87)
- OPLS-AA (Jorgensen et al 95)
- ENCAD (Levitt et al 83)
- Subtle differences in improper torsions, scale factors 1-4 bonds, united atom rep.
- Partial charges based on empirical fits to small molecular systems
- Amber & Charmm also include ab-initio calculations
- Not clear which FF is best : top 4 mostly used
- Water models also included in description
 - TIP3P, TIP4P
 - SPC/E
- Current limit: 10⁶ atoms, microseconds (with Anton ms)



X-tal structure of Trigger Factor (TF)

- Chaperone protein characterized in E. coli
- Dual role:
 - Ribosome exit tunnel
 - Downstream in cytosol
- Flexible dragon-shaped structure
- 432 amino acid residues
- 3 domains:
 - N-terminal:Tail
 - C-terminal: Body + Arms
 - PPlase domain: Head



A. Hoffmann, B. Bukau, and G. Kramer, Biochimica et Biophysica Acta 1803 (2010), 650

Solution structure very different from x-tal



MD 250 ns trajectories in 50 mM salt solution

Amber FF

System with explicit water: 200000 atoms

Collapse Mechanism



Trigger factor interacting with substrate



Conclusions Trigger factor

- Trigger factor very flexible in solution
 - crystal structure collapses
 - first hydrophobic collapse of Head-Arm I
 - followed by hydrophilic interaction of Nterm-Arm2
- Structural motions in TF stabilized in presence of substrate protein
- N-terminal crucial: mostly hydrophilic interactions with MBP subfold
- C-terminal crucial: also hydrophobic interactions with unfolded chain

- Clearly MD is not long enough
- Dynamics is dominated by rare events caused by high barriers



Next Thursday: rare events!

