

# Molecular Simulation

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## Introduction

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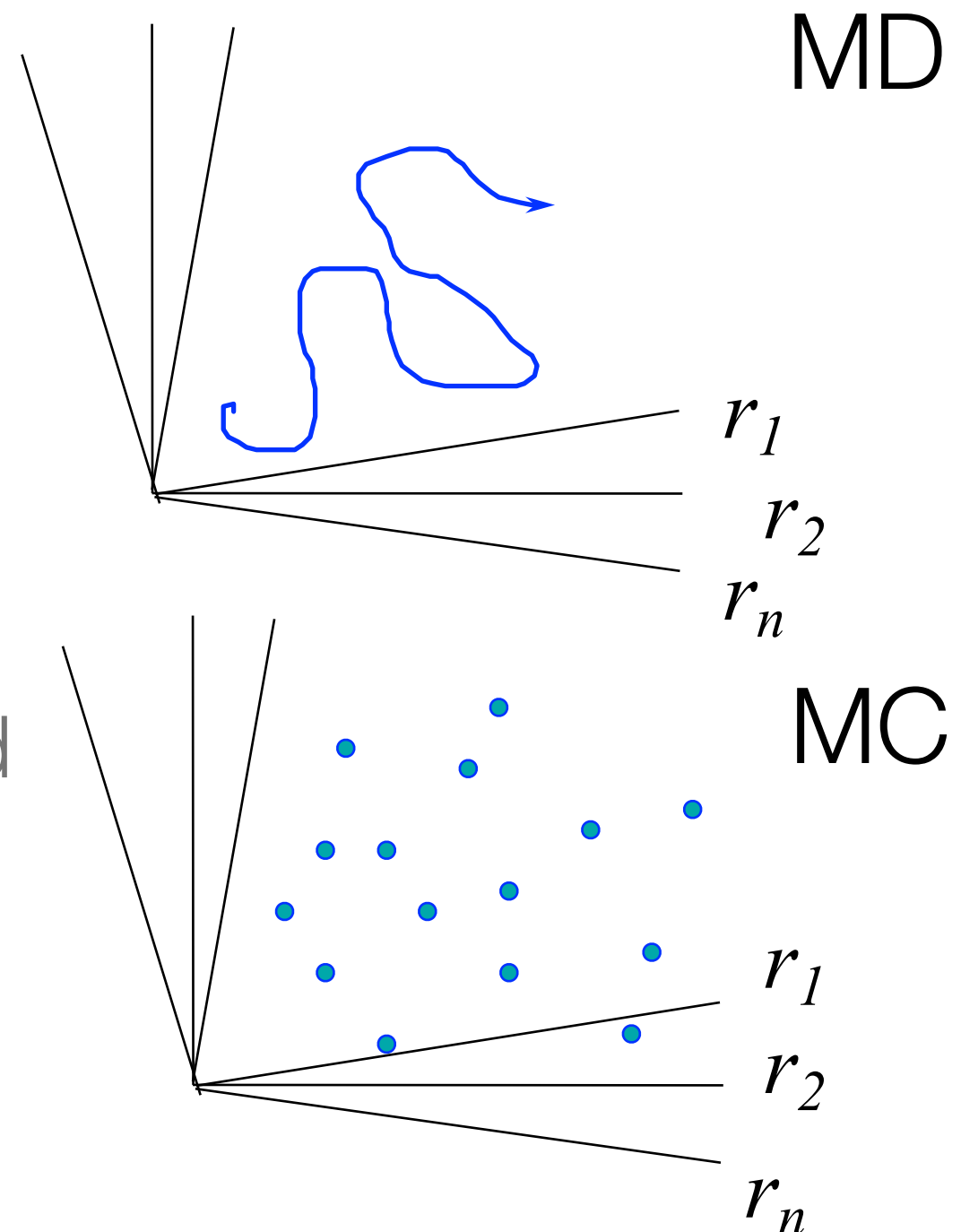
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- Why to use a simulation
- Some examples of questions we can address

# Molecular Simulations

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- **Molecular dynamics:** solve equations of motion
- **Monte Carlo:** importance sampling
- Calculate thermodynamic and transport properties for a given intermolecular potential



# Uses of Molecular Simulations

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We assume the interactions between the particles are known!

Exact= in the limit of infinitely long simulations the error bars can be made infinitely small

The idea for a given *intermolecular potential* “*exactly*” compute the *thermodynamic* and *transport* properties of the *system*

If one could envision an experimental system of these N particles that interact with the potential.

Pressure  
Heat capacity  
Heat of adsorption  
Structure  
....

Diffusion coefficient  
Viscosity  
...

# Why Molecular Simulations

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Paul Dirac, after completing his formalism of quantum mechanics: “*The rest is chemistry...*”.

This is a heavy burden the shoulders of “chemistry”:

The “*rest*”:

amounts to the *quantitative description* of the world around us and the prediction of all every-day phenomena ranging from the chemical reactions of small molecules to the integrated description of living organisms.

# Intermolecular potential

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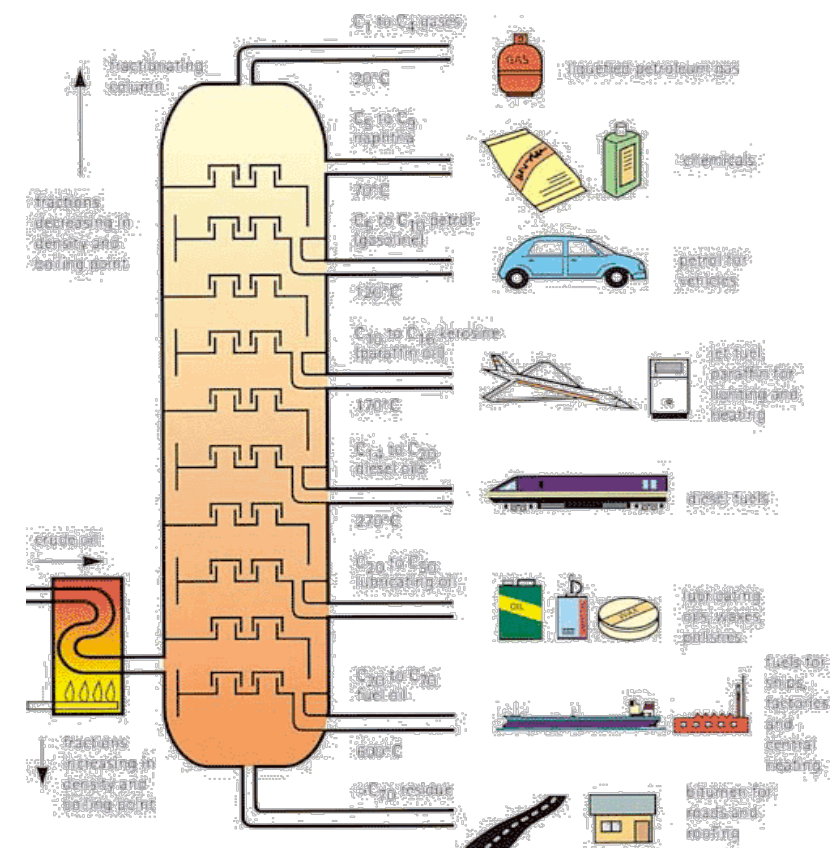
The intermolecular potential can:

- Mimic the experimental system as accurate as possible:
  - Replace experiments (dangerous, impossible to measure, expensive, ...)
- Make a model system:
  - Test theories that can not directly be tested with experiment

If we know/guess the “true” intermolecular potential

# Example 1: Mimic the “real world”

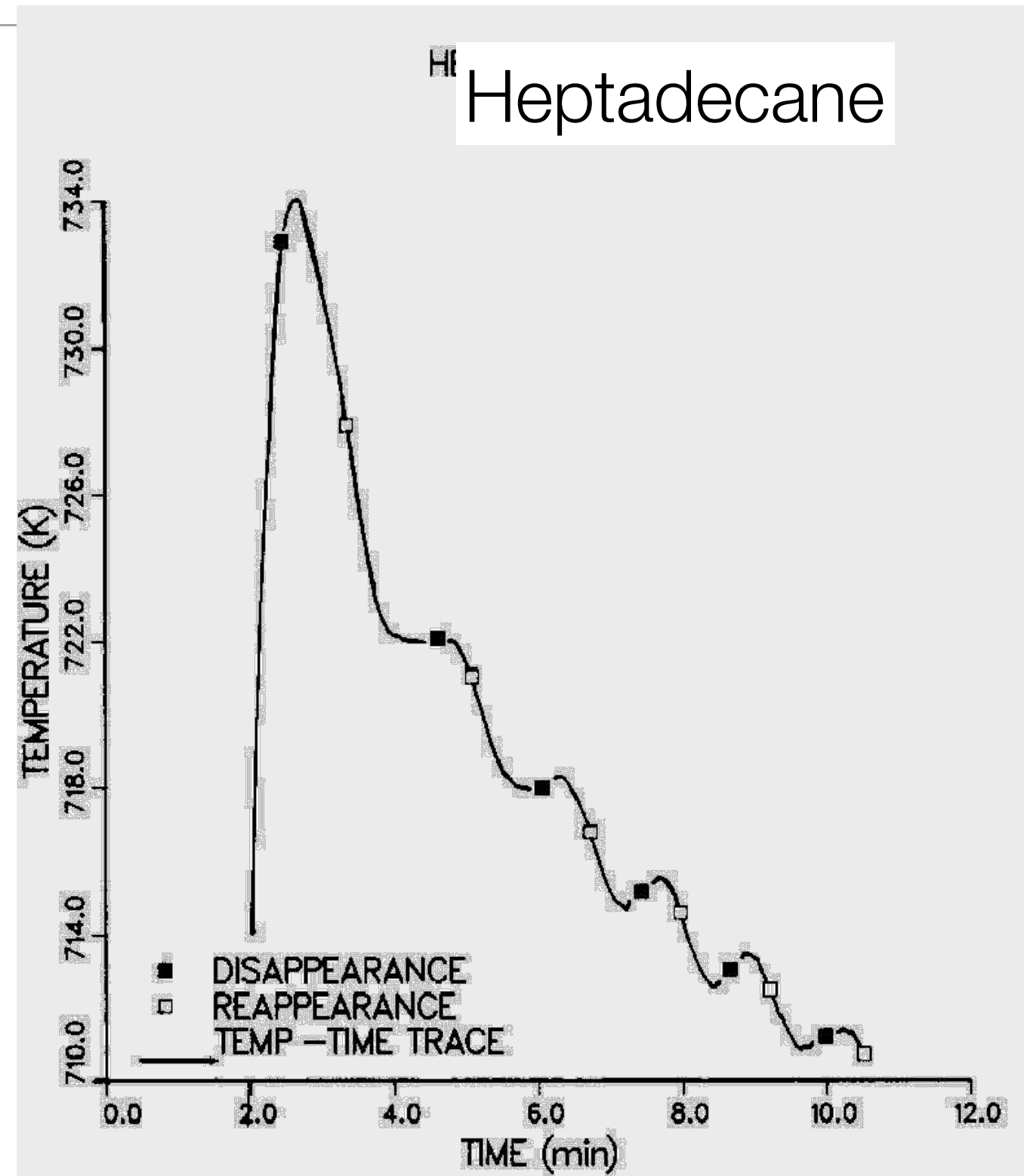
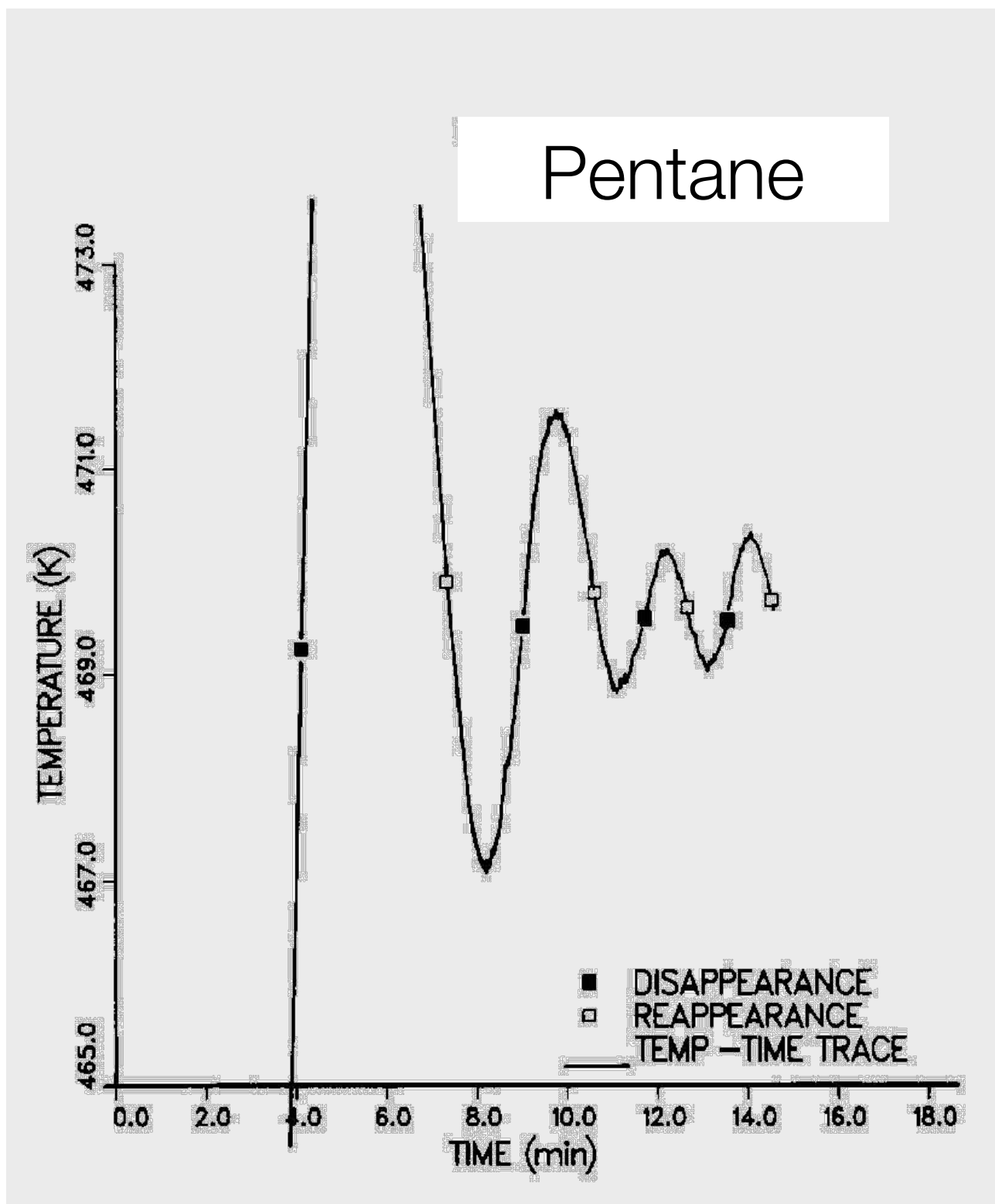
## Critical properties of long chain hydrocarbons



To *predict* the thermodynamic properties (boiling points) of the hydrocarbon mixtures it is convenient (=Engineering models use them) to know the critical points of the hydrocarbons.



# Critical points of long chain hydrocarbons

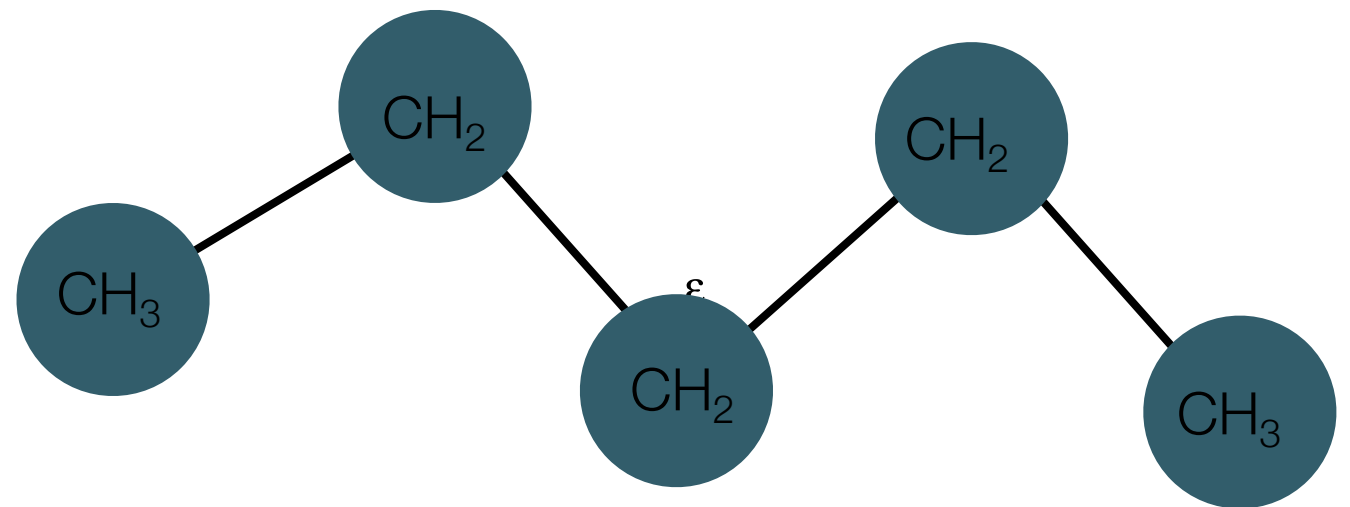


# Hydrocarbons: intermolecular potential

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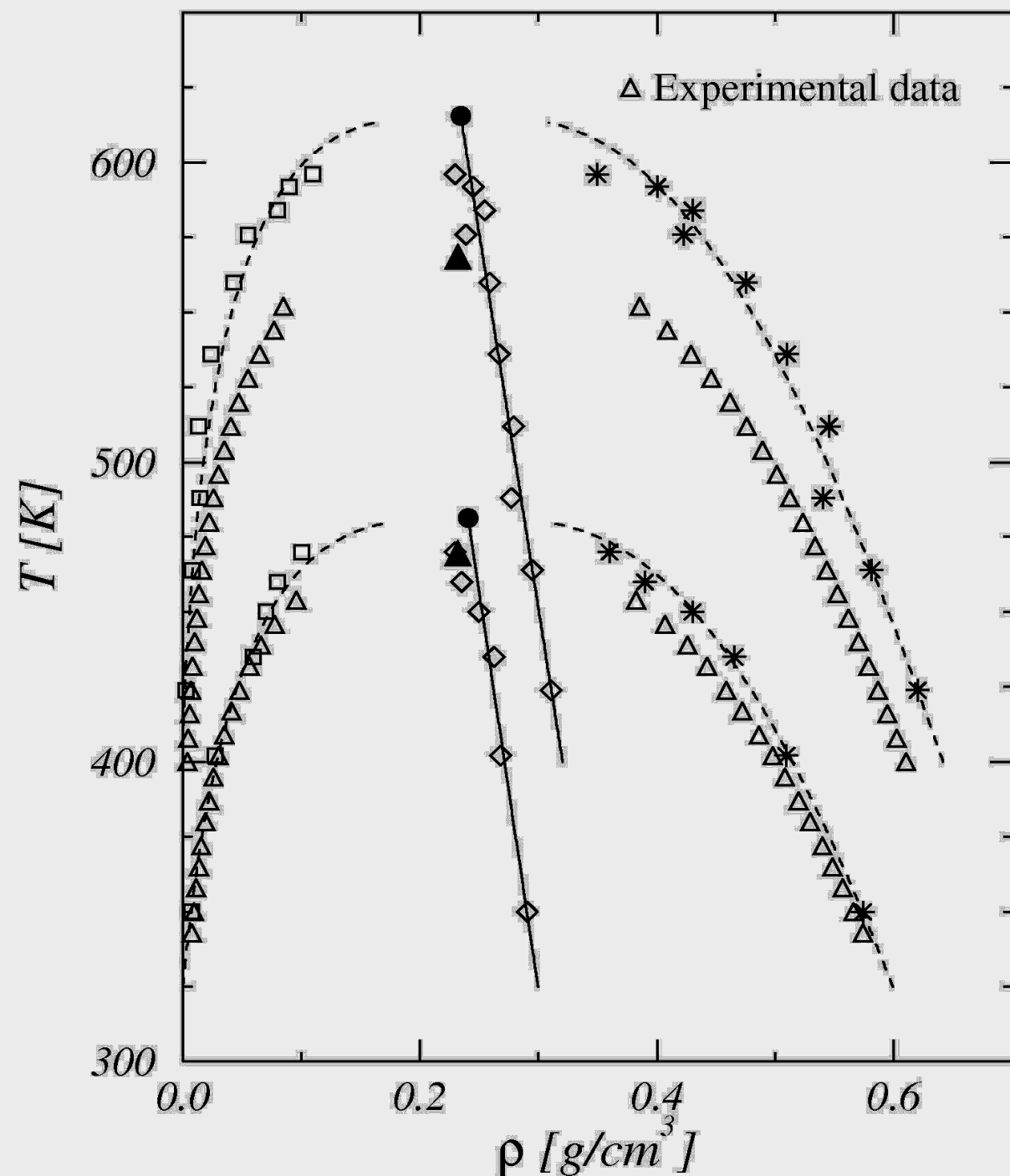
## United-atom model

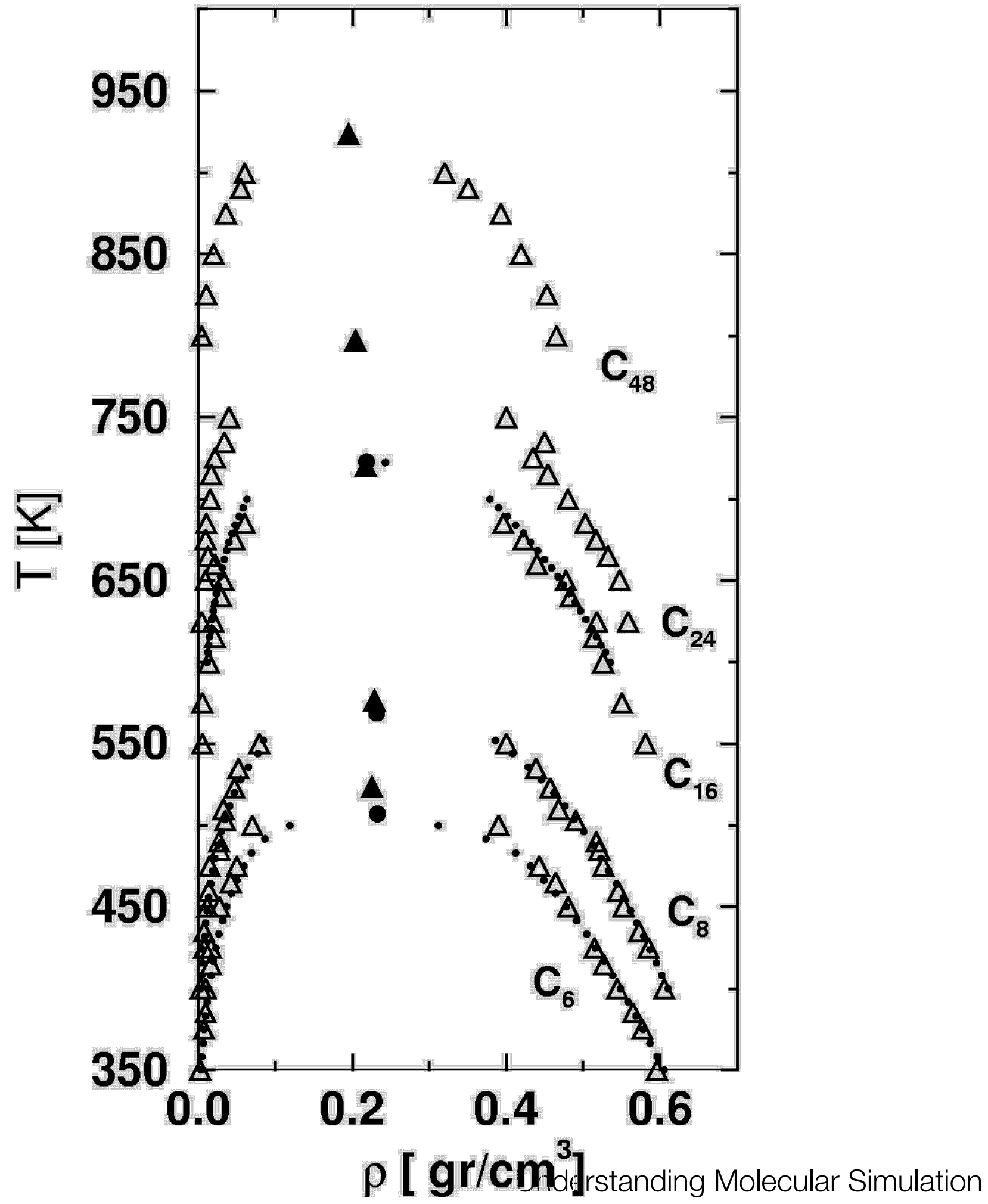
- Fixed bond length
- Bond-bending
- Torsion
- Non-bonded: Lennard-Jones

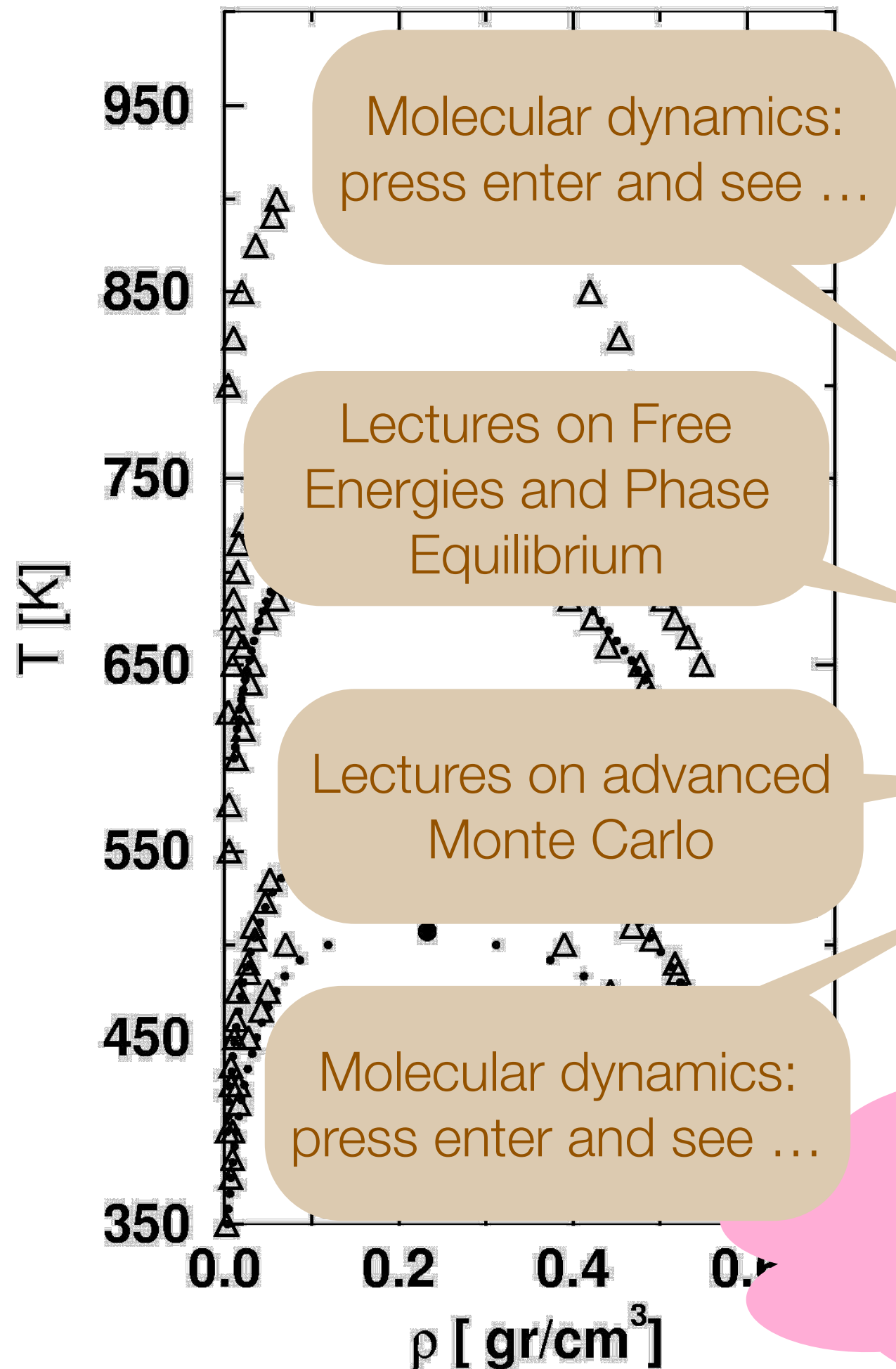


$$u(r) = 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r} \right)^{12} - \left( \frac{\sigma_{ij}}{r} \right)^6 \right]$$

# OPLS (Jorgensen) Model







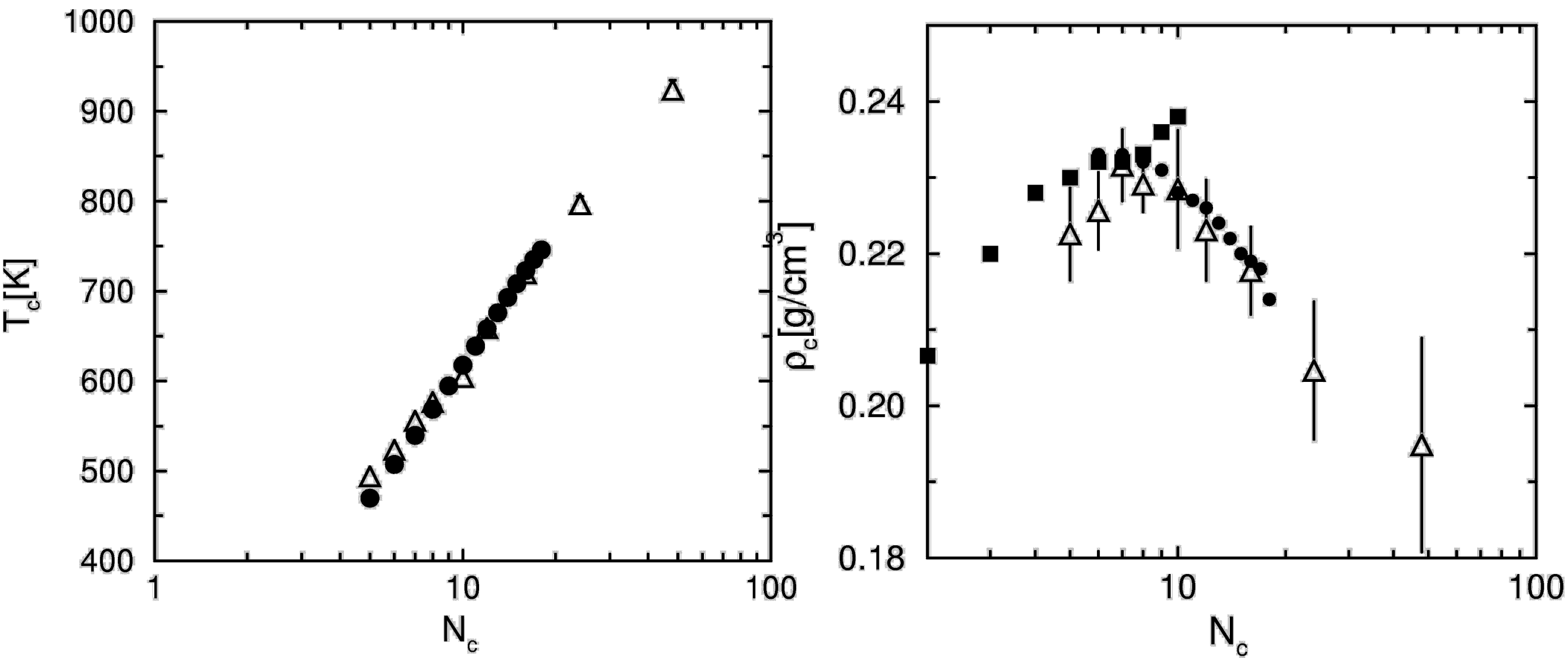
*But my system is  
extremely small, is the  
statistic reliable?*

Computational issues:

- How to compute vapour-liquid equilibrium?
- How to deal with long chain hydrocarbons?

*But C48 moves much slower  
than methane (C1). Do I have  
enough CPU time*

# Critical Temperature and Density



Nature **365**, 330 (1993).

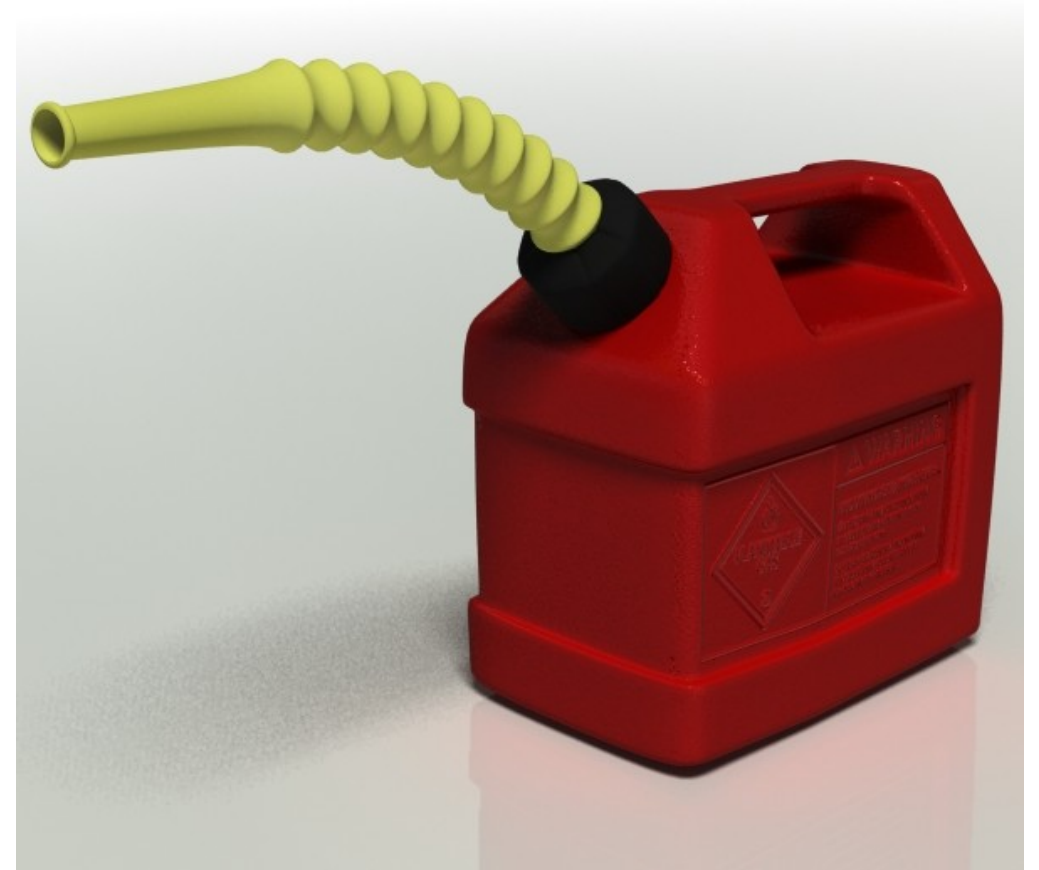
# Methane storage

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# Methane cars: the technological obstacle

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Gasoline, 1 liter



34.2 MJ

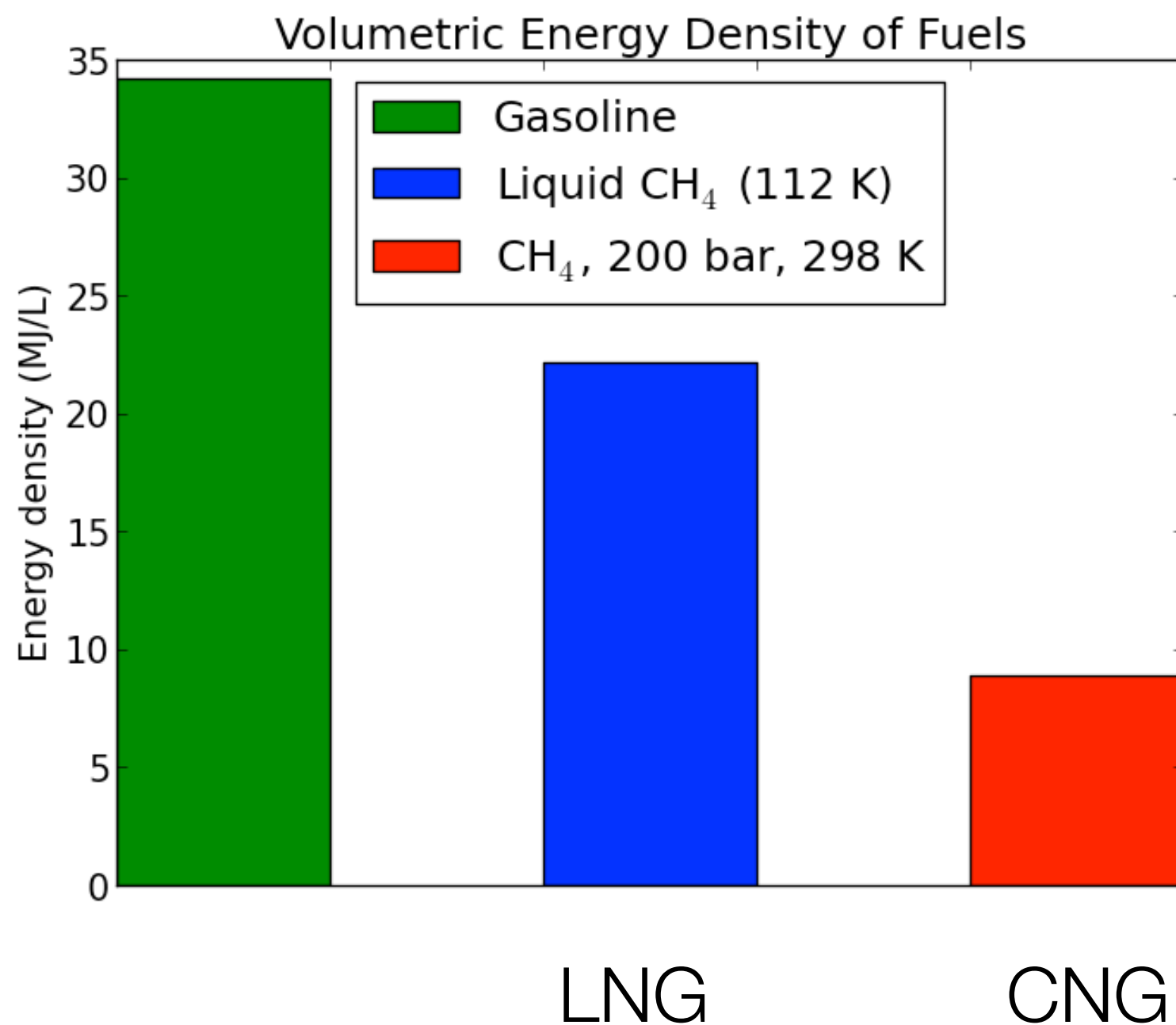


0.036 MJ



# Methane versus gasoline

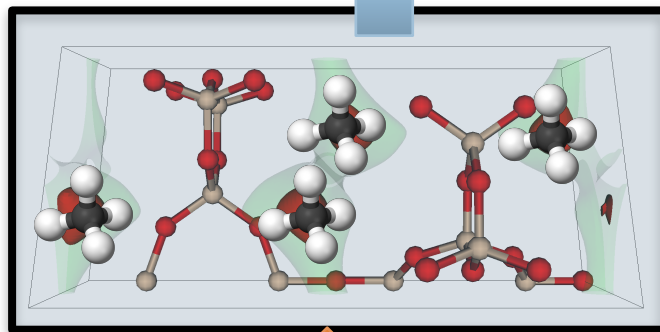
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# Pressure swing adsorption

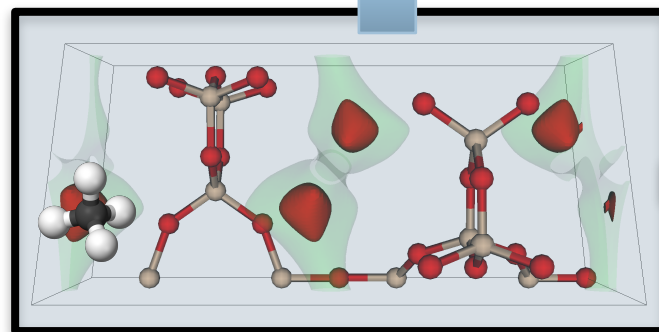


65 bar

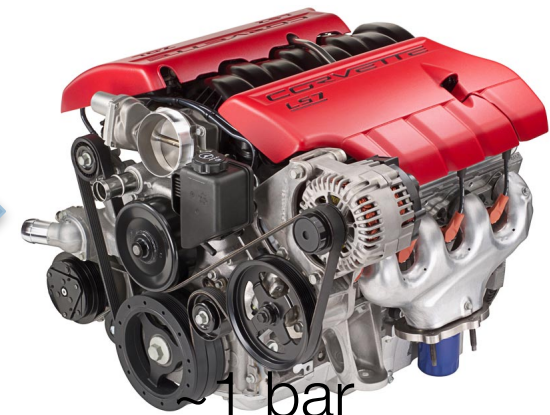


$P_H = 65 \text{ bar}$

5.8 bar



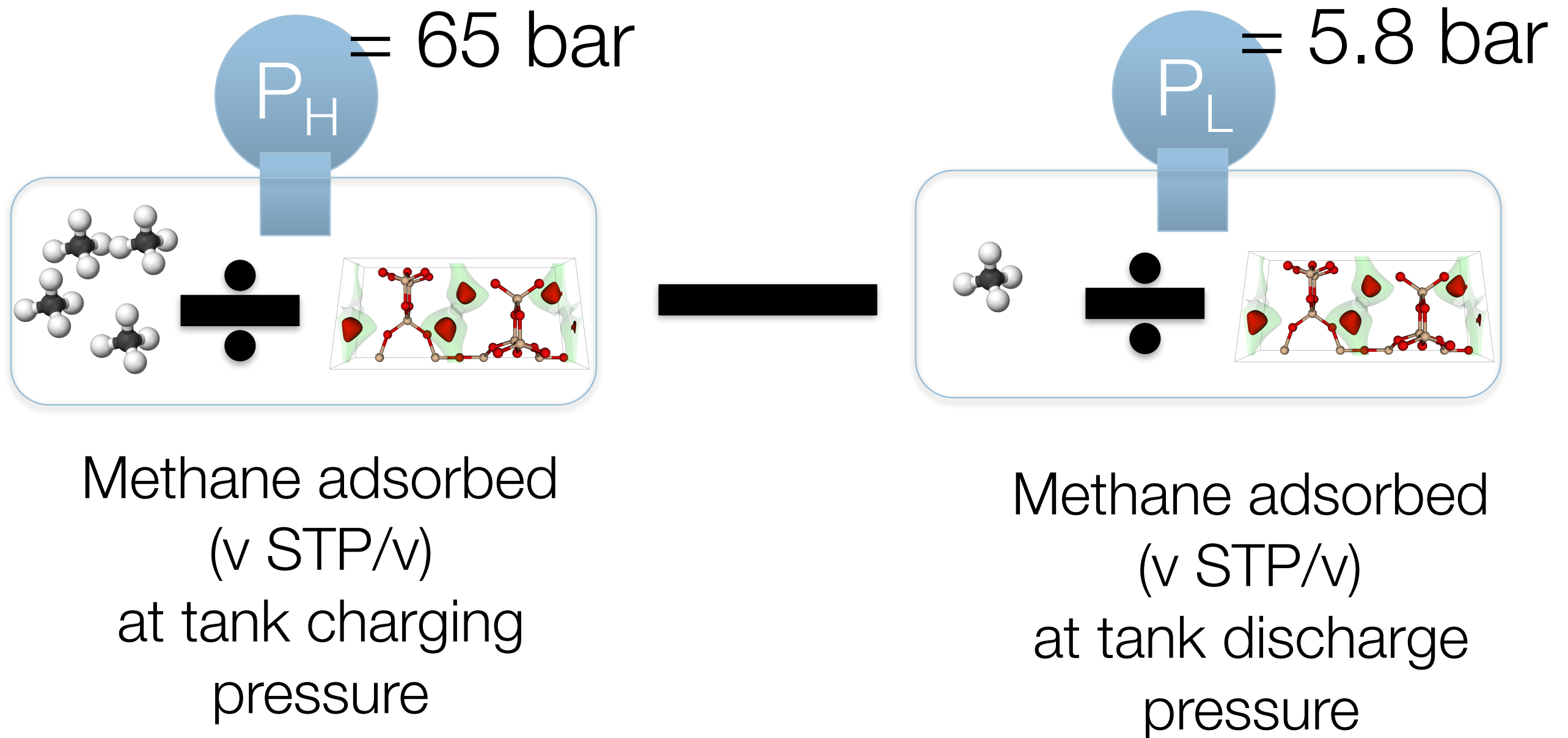
$P_L = 5.8 \text{ bar}$



1 bar

Insufficient  
flow

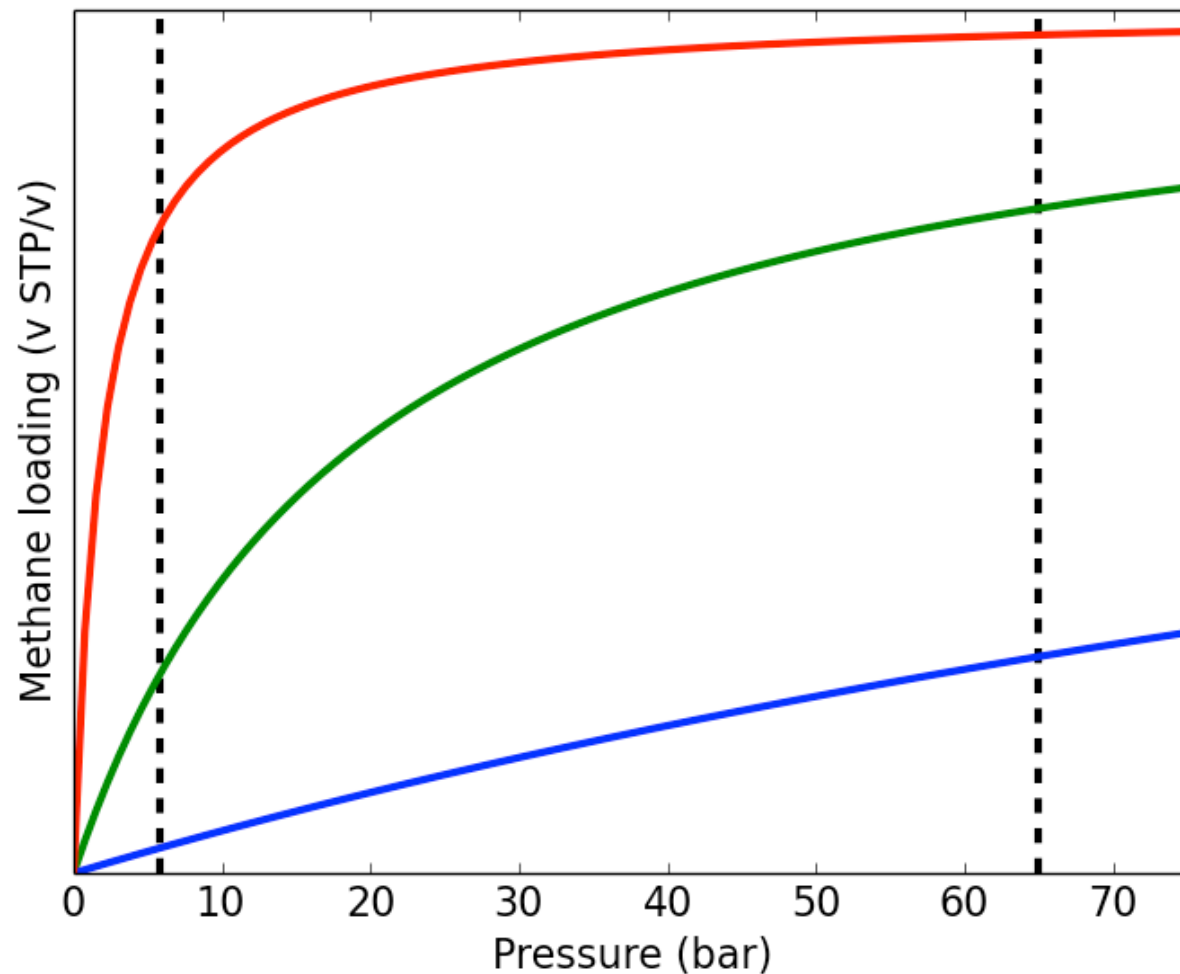
# The deliverable capacity



**ARPA-E (DOE) target: 315 m<sup>3</sup> STP methane/m<sup>3</sup> adsorbent**

# An optimal heat of adsorption?

Goal: maximize deliverable capacity



“For methane, an optimal enthalpy change of [16.2] kJ/mol is found.”

*Langmuir* 2006, 22, 1688–1700

## Optimum Conditions for Adsorptive Storage

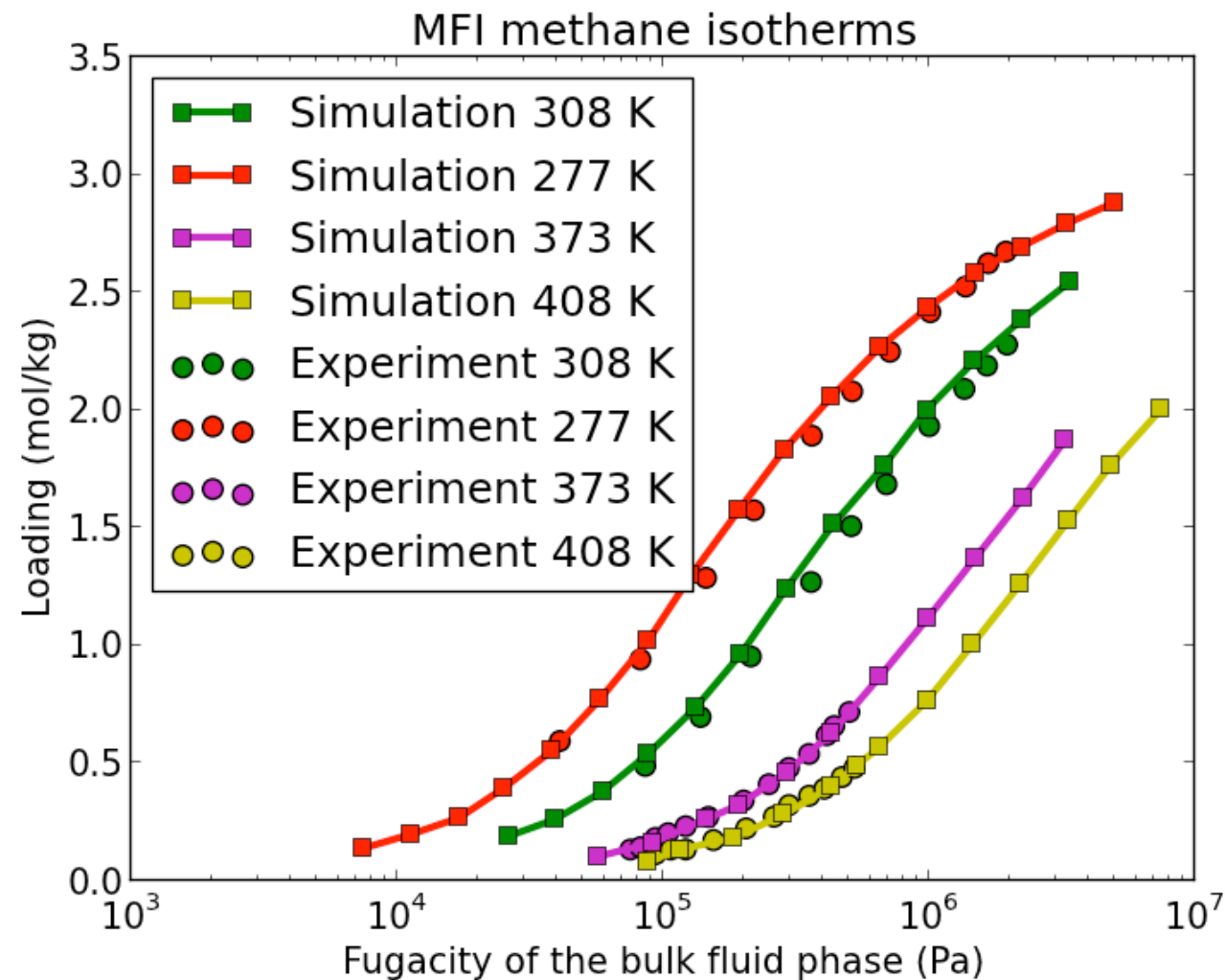
Suresh K. Bhatia<sup>†</sup>

*Division of Chemical Engineering, The University of Queensland, Brisbane, QLD 4072 Australia*

Alan L. Myers<sup>\*</sup>

*Department of Chemical and Biomolecular Engineering, University of Pennsylvania, Philadelphia, Pennsylvania 19104*

# In silico screening of zeolites

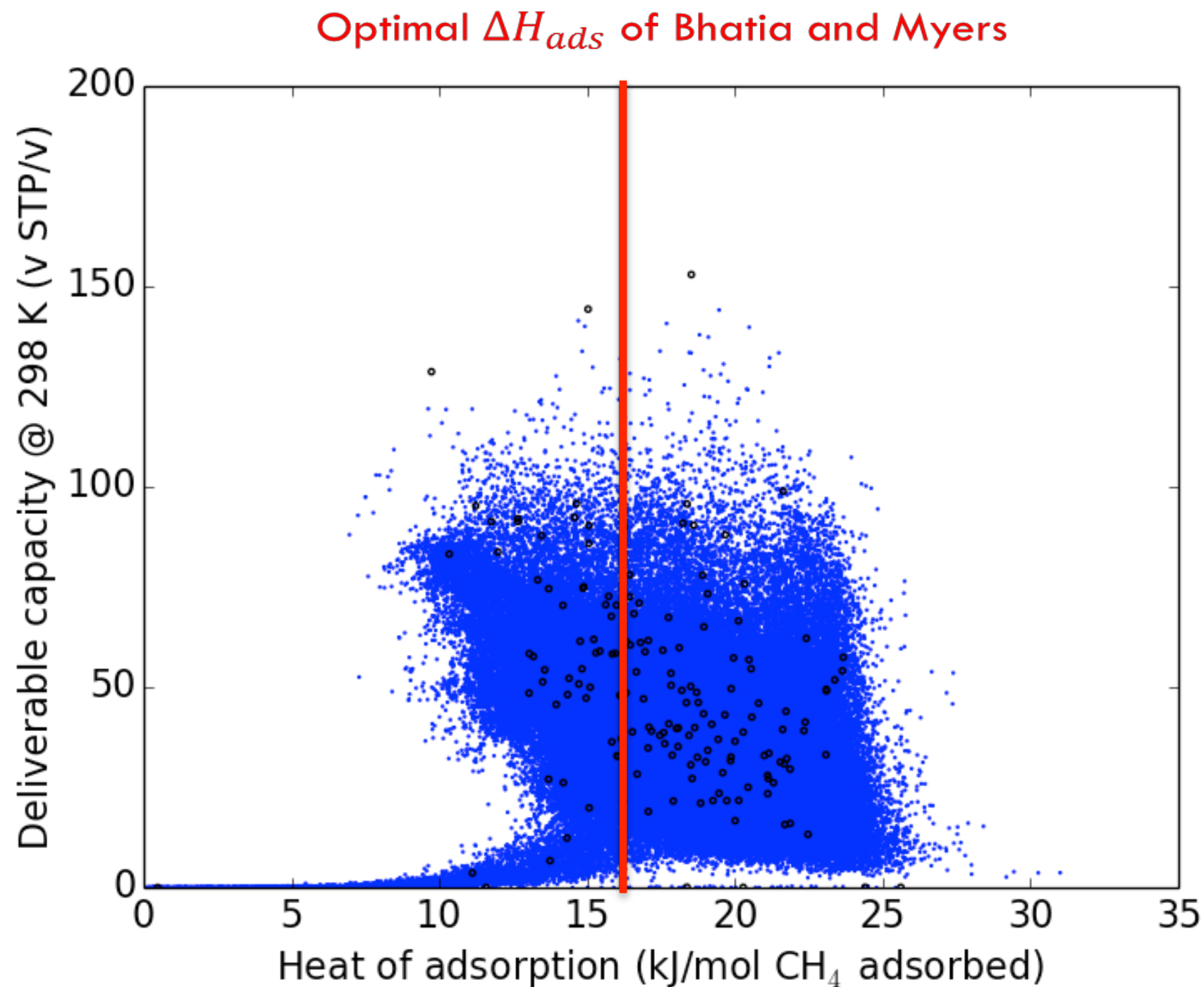


MFI expt'l data: Sun *et al.* (1998) *J. Phys. Chem. B.* 102(8), 1466-1473.

Zhu *et al.* (2000) *Phys. Chem. Chem. Phys.* 2(9), 1989-1995.

Force field: Dubbeldam *et al.* (2004) *Phys. Rev.* 93(8), 088302.

# In silico screening of zeolites



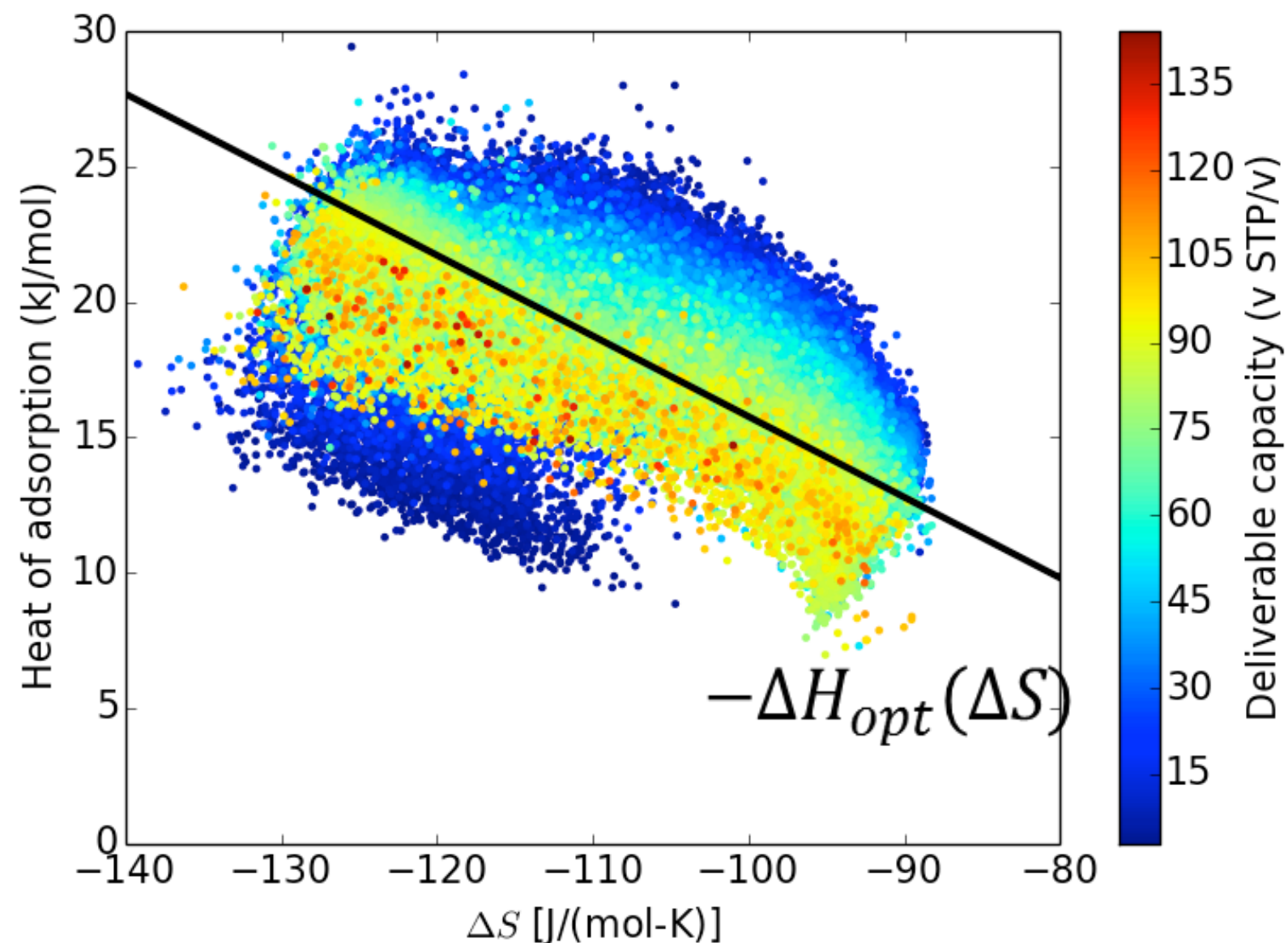
C. Simon *et al.* (2014) *Phys. Chem. Chem. Phys.* 16 (12), 5499-5513

Understanding Molecular Simulation



# Enthalpy vs. entropy

- $\Delta S$  not the same for all materials
- Wide range of  $\Delta H$  that yields optimal material



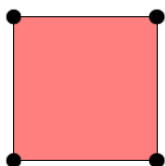
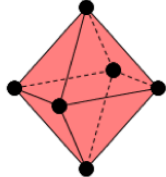


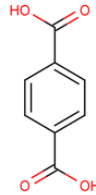
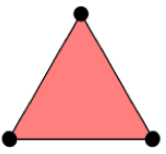
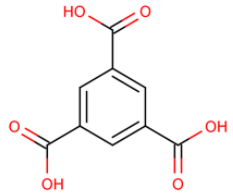
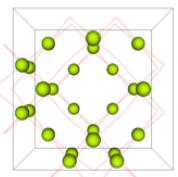
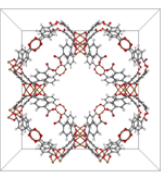
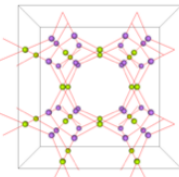
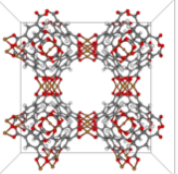
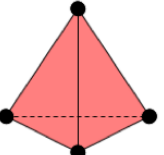
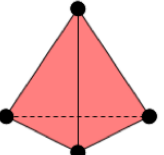

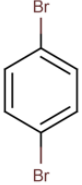

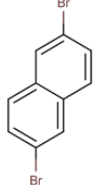
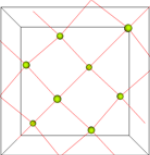
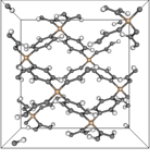
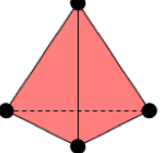

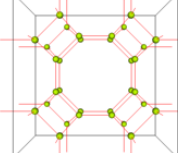
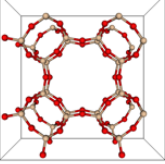
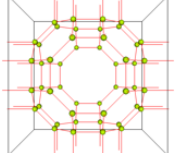
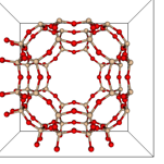
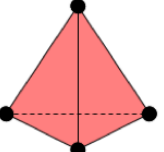
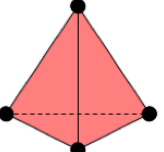

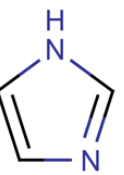

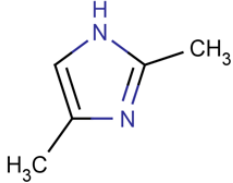
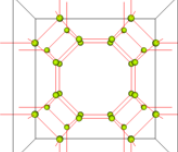
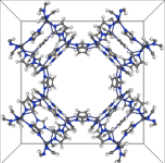
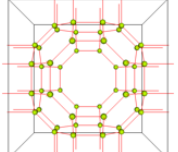
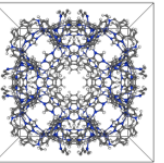
# Can we find a material that meets the DOE target?

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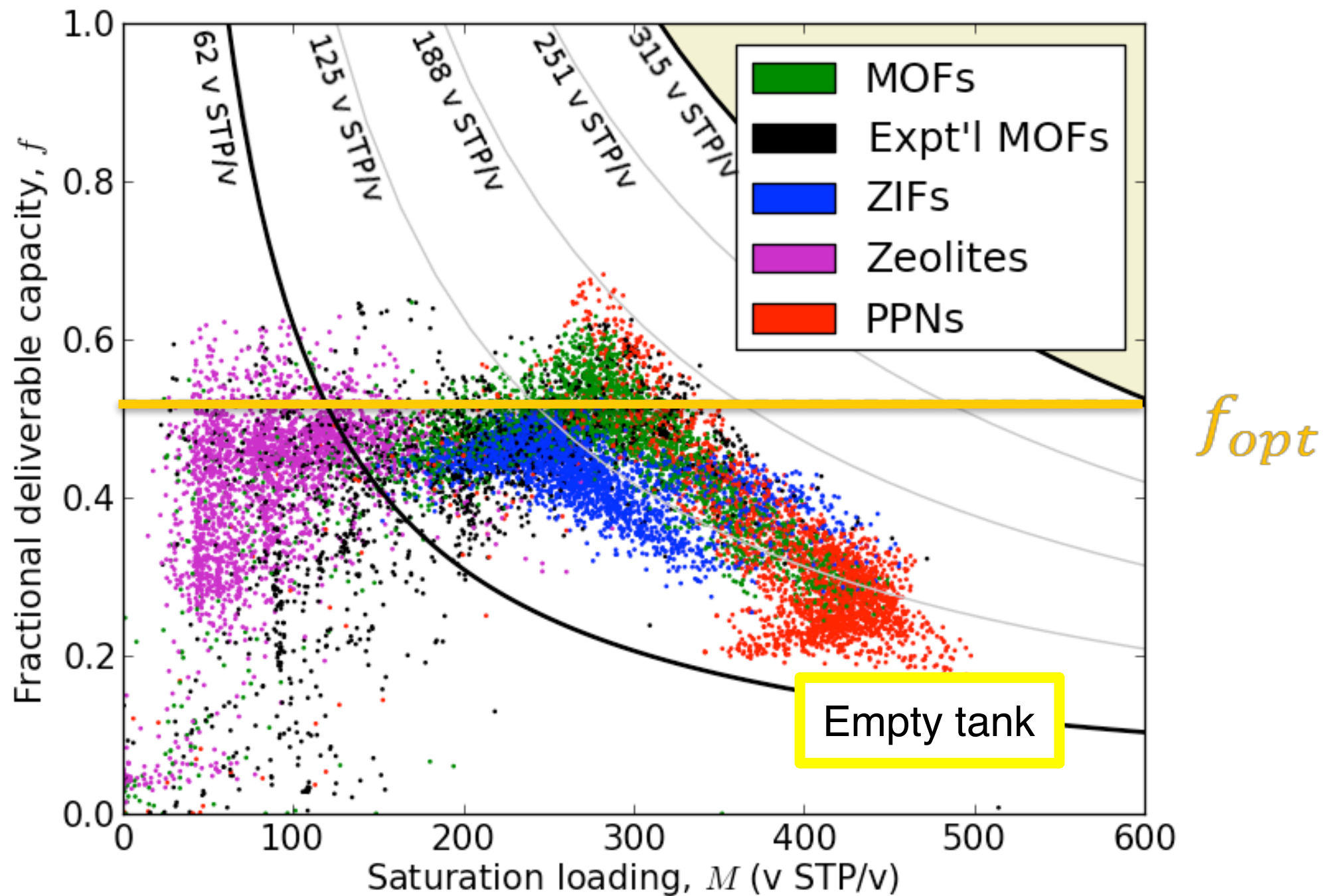
Screening > 100,000 materials

- zeolites
- Metal organic Frameworks, MOFs (Snurr and co-workers)
- zeolitic imidazolate frameworks, ZIFs, (Haranczyk)
- Polymer Porous Networks, PPNs (Haranczyk)



Material class	Building blocks				Topologies	
MOFs	 <div>Cu—Cu</div>	 	 	 	 	 
PPNs	 <div>Si</div>	 <div>Ge</div>	 	 	 	
Zeolites	 <div>Si</div>	 <div>O</div>		 	 	
ZIFs	 <div>Zn</div>	 <div>Fe</div>	 	 	 	 

# Insight from the model



## Example 3: make a model system

Question: are attractive interactions important in the condensed phase?

**YES:**

- Attractive forces are needed
- Theories predict this ..

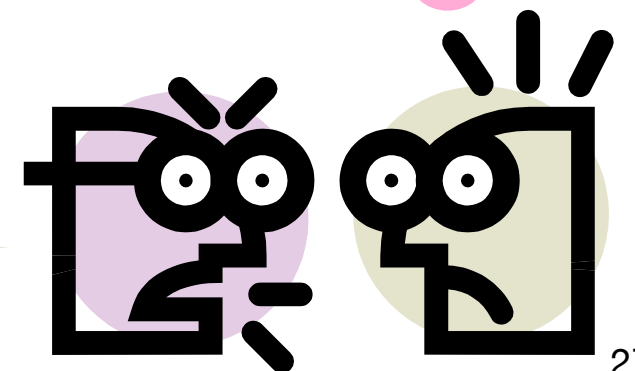
**BUT:**

- There are no molecules with *only* attractive interactions

How to test the theory?

Your theory is  
**WRONG** it disagrees  
with the experiments

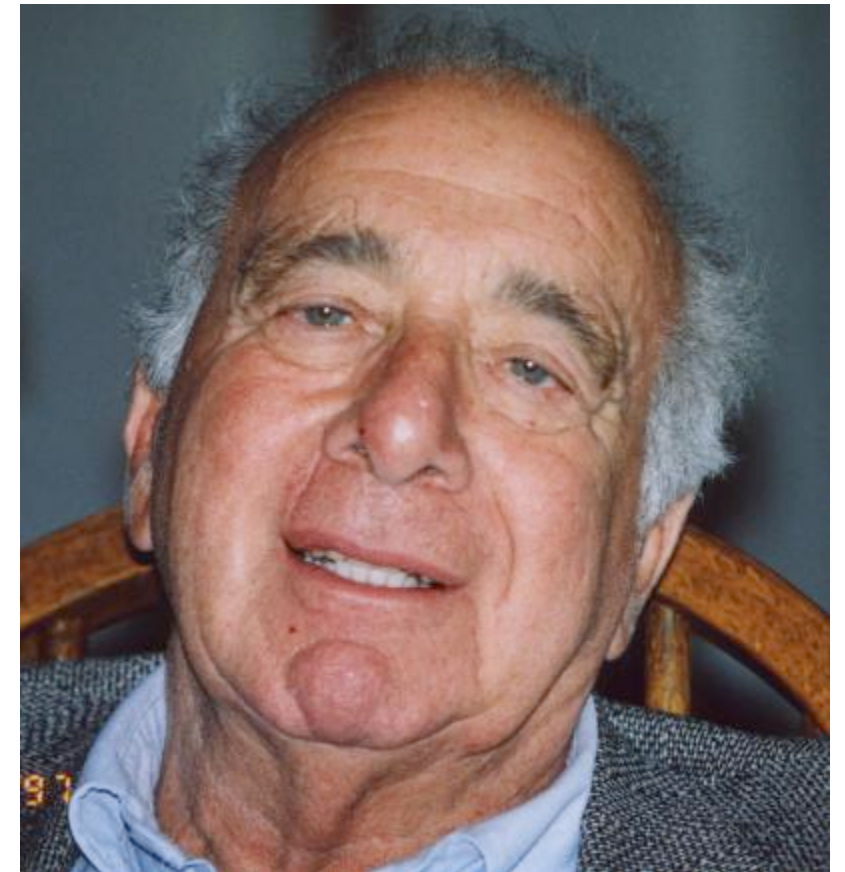
My theory is **RIGHT**: but  
this experimentalist refuses  
to use molecules that do  
not have any attractive  
interactions



# But we can simulate hard spheres ..

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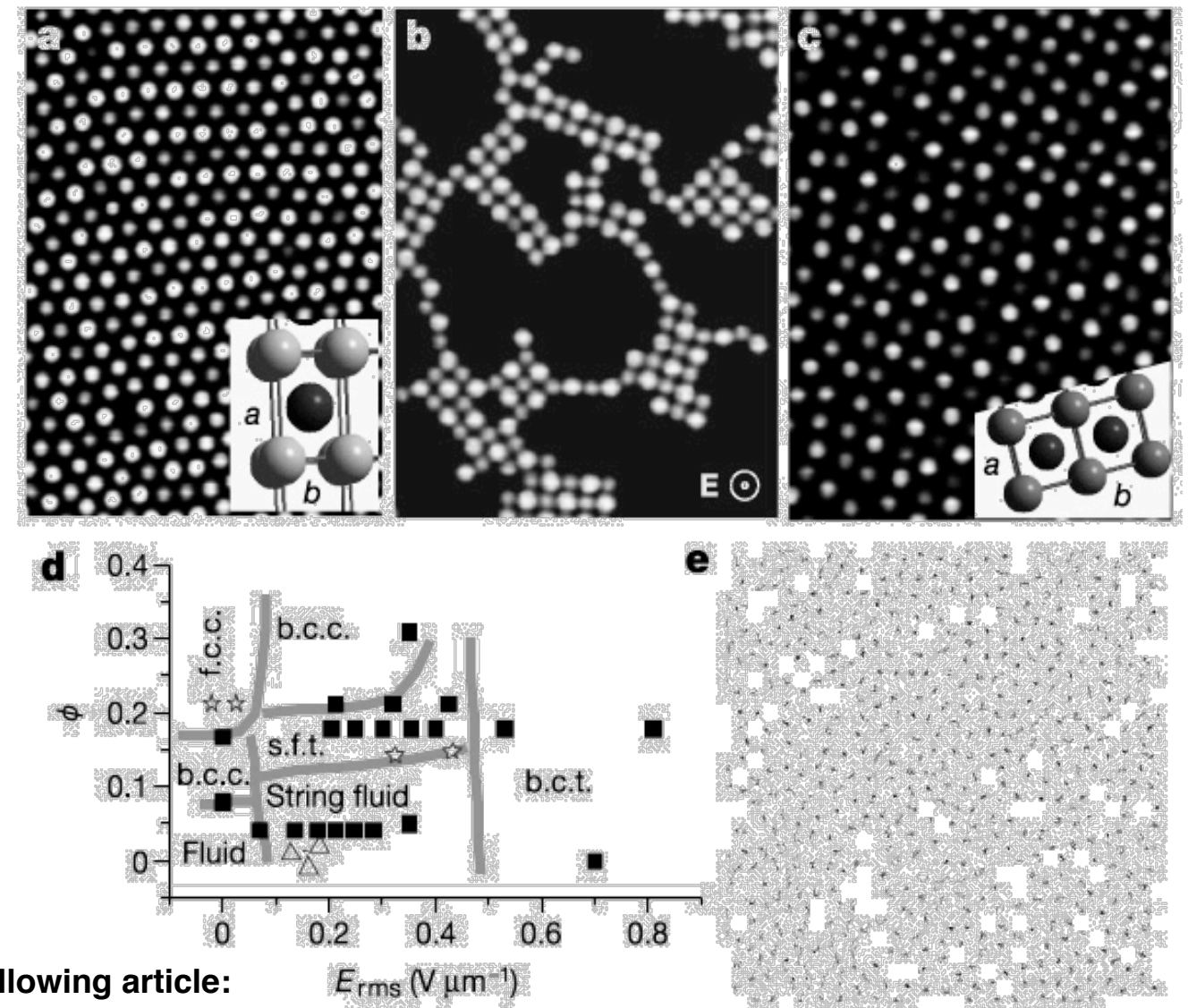
- Bernie Alder carried out Molecular Dynamics simulations of the freezing of hard spheres
- But, .... did the scientific community accept this computer results as experimental evidence ...
- ... during a Gordon conference it was proposed to vote on it ...
- ... and it was voted against the results of Alder





# Experiments are now possible

.. But not on molecules  
but on colloids:



From the following article:

[A colloidal model system with an interaction tunable from hard sphere to soft and dipolar](#)

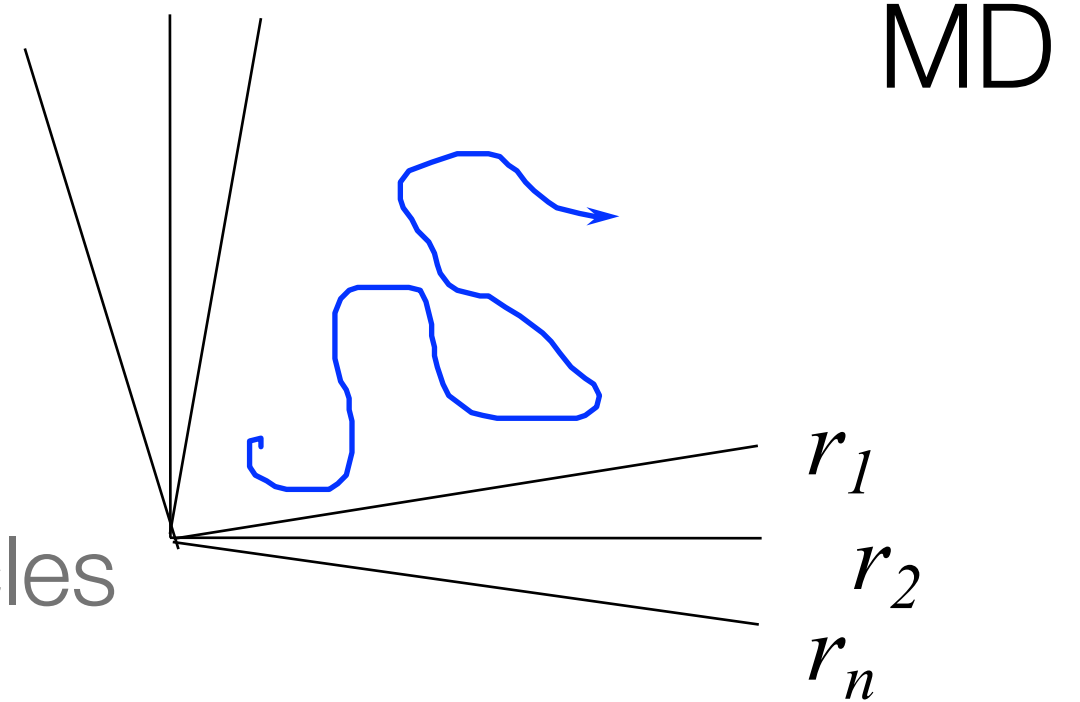
Anand Yethiraj and Alfons van Blaaderen  
Nature 421, 513-517 (30 January 2003)

# Molecular Dynamics

- Theory:

$$\mathbf{F} = m \frac{d^2 \mathbf{r}}{dt^2}$$

- Compute the forces on the particles
- Solve the equations of motion
- Sample after some timesteps

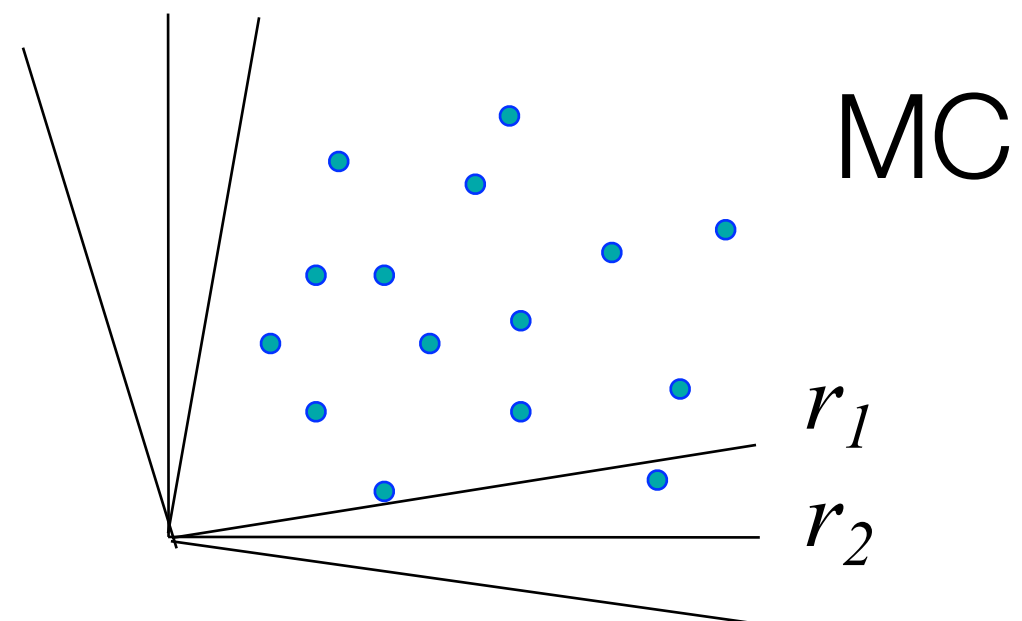


# Monte Carlo

- Generate a set of configurations with the *correct* probability
- Compute the thermodynamic and transport properties as averages over all configurations

How to compute these properties from a simulation?

What is the correct probability?  
Statistical  
Thermodynamics



# Classical and Statistical Thermodynamics

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Problem: we have a set of coordinates and velocities -what to do with it?

- Statistical Thermodynamics
  - The probability to find a particular configuration
  - Properties are expressed in term of averages
  - Free energies
- Thermodynamics: relation of the free energies to thermodynamic properties