

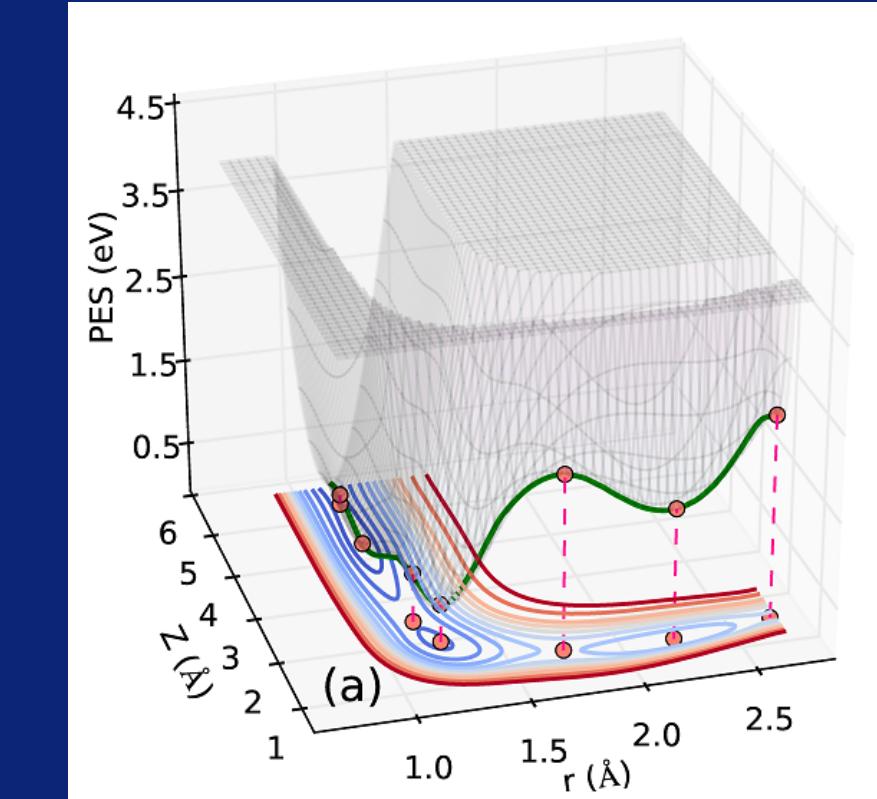
# Machine learning in computational chemistry

## Foundations and applications

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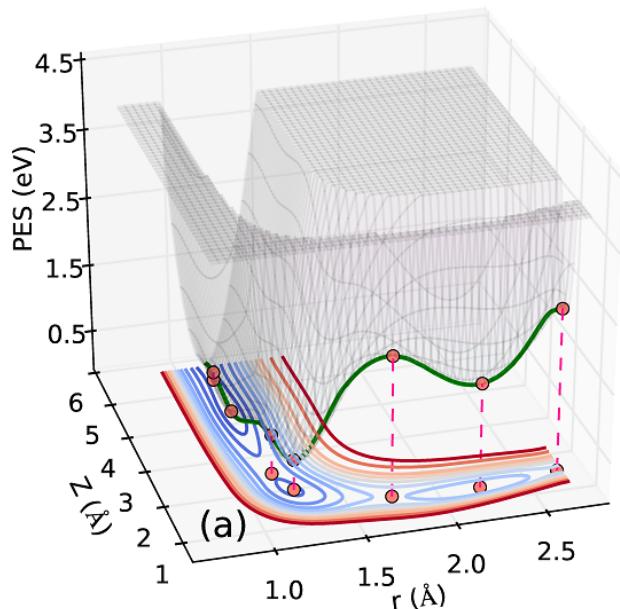
# Contents

- 1) Neural Networks (NNs):  
Structure & “Learning” (1h)  
*Hands-on:* Training a simple NN (45 min)
- 2) NNs for potential energy surfaces:  
Coordinate representation (~45 min)  
*Hands-on:* (Re-)Fitting a potential energy surface for O<sub>2</sub>@Pd(100) (~20 min + last night)
- 3) Applications in gas-surface dynamics (<1h)

# Langevin dynamics 1: PESs

$$m\ddot{\mathbf{R}} = -\nabla V(\mathbf{R})$$

potential energy surfaces (PESs)



I. Goikoetxea, J. Beltrán, **JM**, et al., New J. Phys. **14**, 013050 (2012).

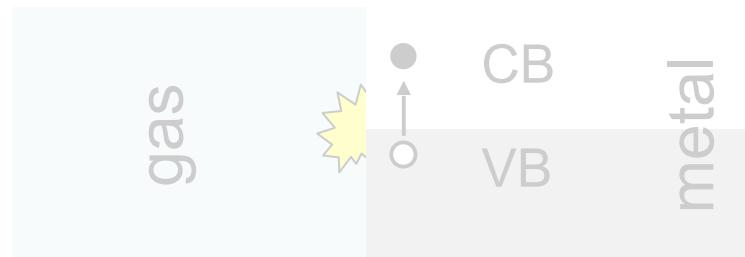
I. Goikoetxea, **JM**, et al., Phys. Rev. Lett. **112**, 156101 (2014).

**JM** and K. Reuter, Angew. Chem. Int. Ed. **53**, 4721 (2014).

K. Shakouri, J. Behler, **JM**, et al., J. Phys. Chem. Lett. **8**, 2131 (2017).

$$-\eta(\mathbf{R})\dot{\mathbf{R}} + \mathbf{F}_{\text{random}}$$

electronic friction (EF)



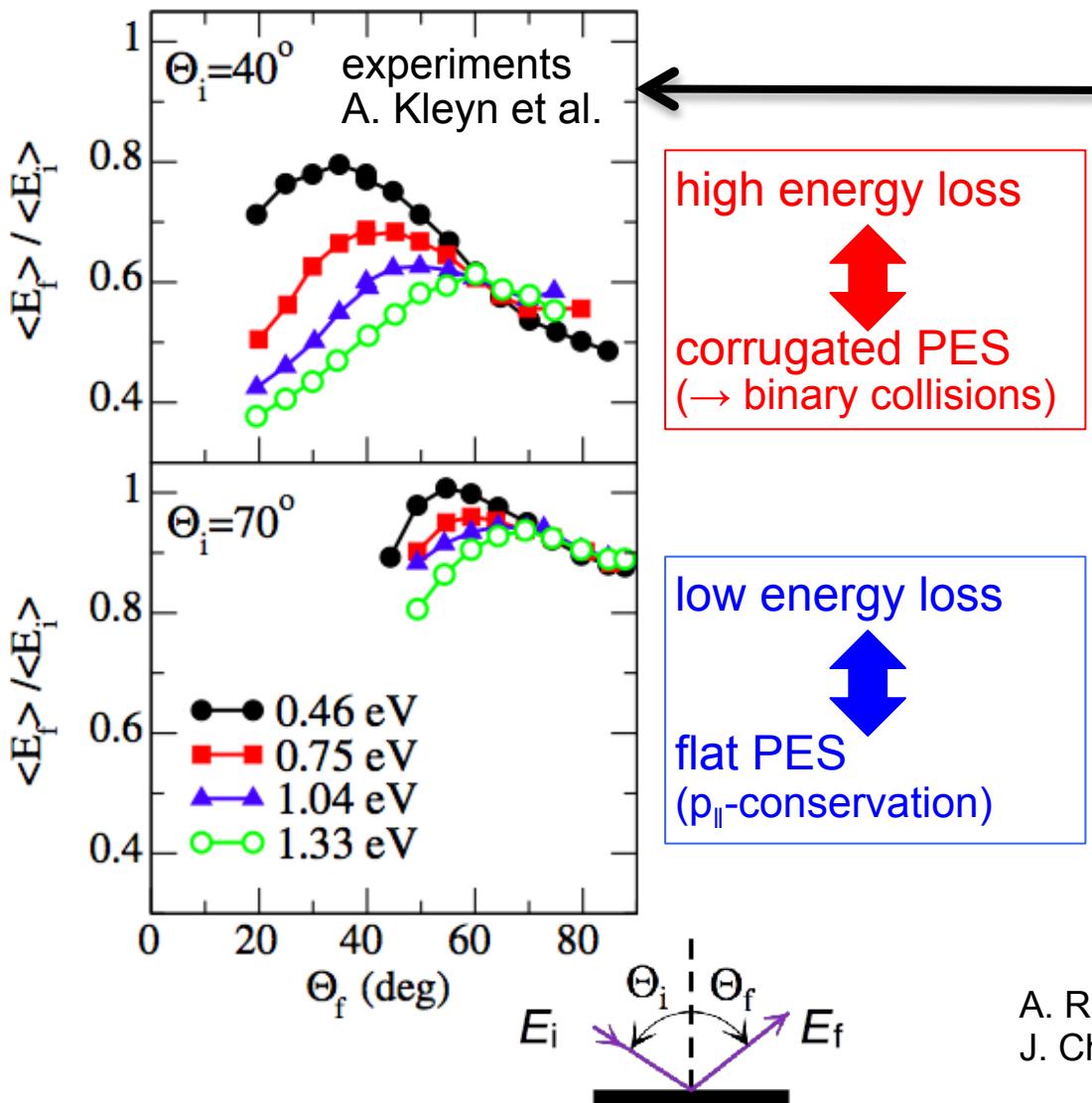
**JM** and K. Reuter, New J. Phys. **13**, 085010 (2011).

S. P. Rittmeyer, **JM** et al., Phys. Rev. Lett. **115**, 046102 (2015).

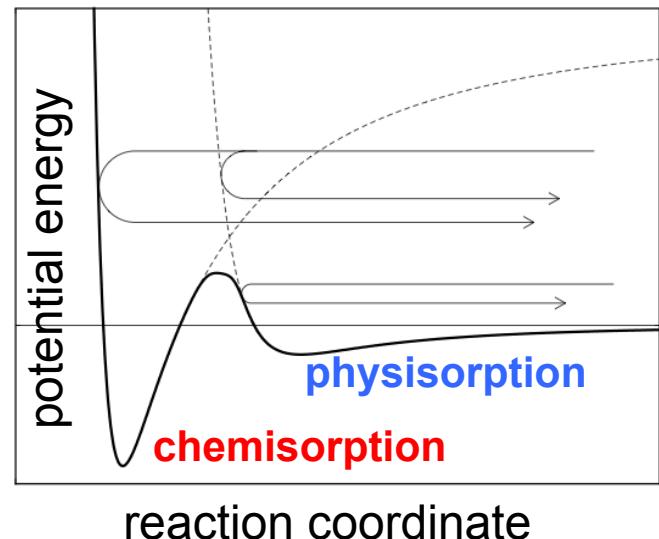
S. P. Rittmeyer, **JM** et al., Phys. Rev. Lett. **119**, 176808 (2017).

P. Spiering and **JM**, J. Phys. Chem. Lett. **9**, 1803 (2018).

# O<sub>2</sub> on Ag(111)

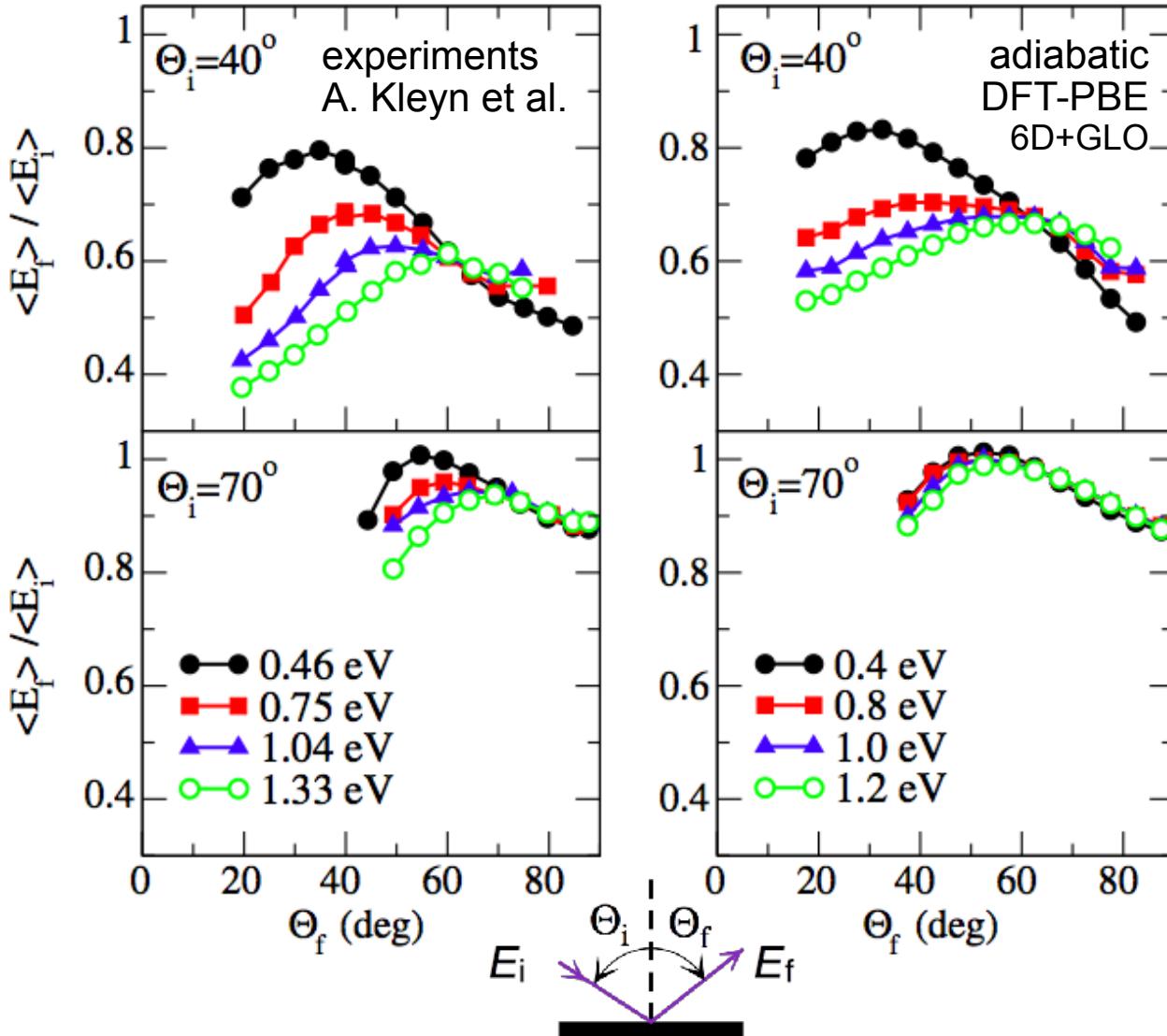


molecular scattering  
(time-of-flight)  
→ suggested interpretation:  
**double well in 1D**



A. Raukema, R. J. Dirksen, and A. W. Kleyn,  
J. Chem. Phys. **103** (1995) 6217.

# O<sub>2</sub> on Ag(111)



vdW-tail absent  
→ no physisorption  
nevertheless(!)  
accurately reproducing

✓ very low  
sticking probability  
 $S_0(E_i < 1.0 \text{ eV}) < 10^{-7}$

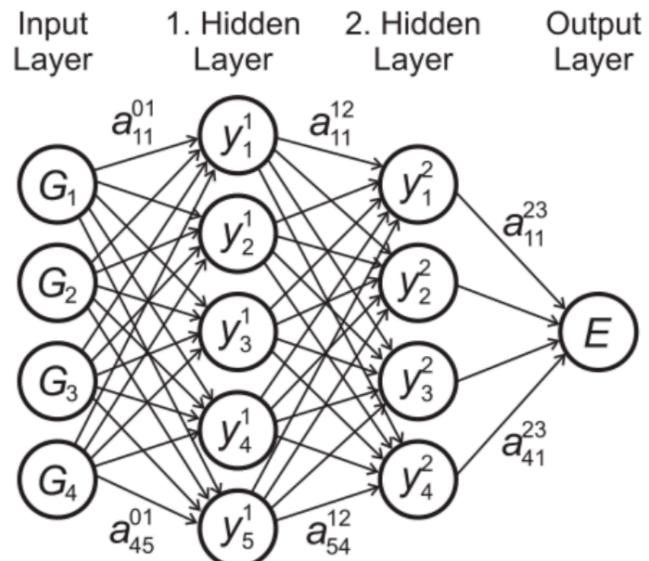
I. Goikoetxea, J. Beltran, JM et al.  
New J. Phys. **14**, 013050 (2012).

✓ scattering

I. Goikoetxea, JM et al.  
Phys. Rev. Lett. **112**, 156101 (2014).

# $N_2$ on Ru(0001): HD-NNP

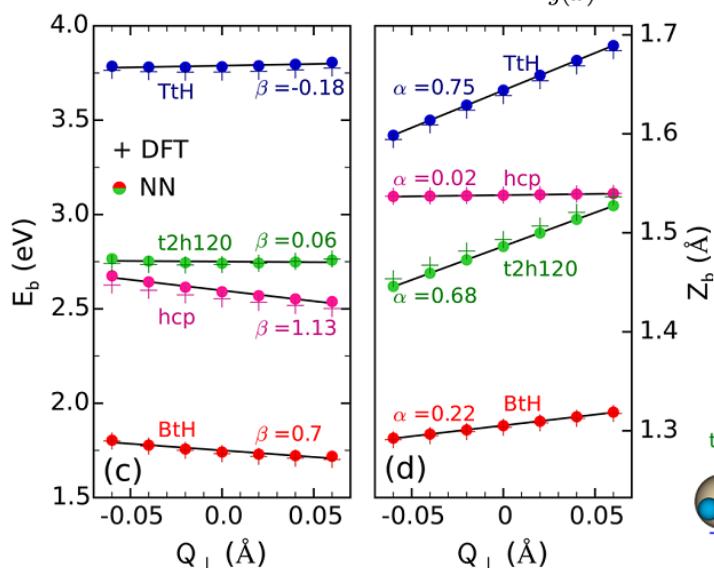
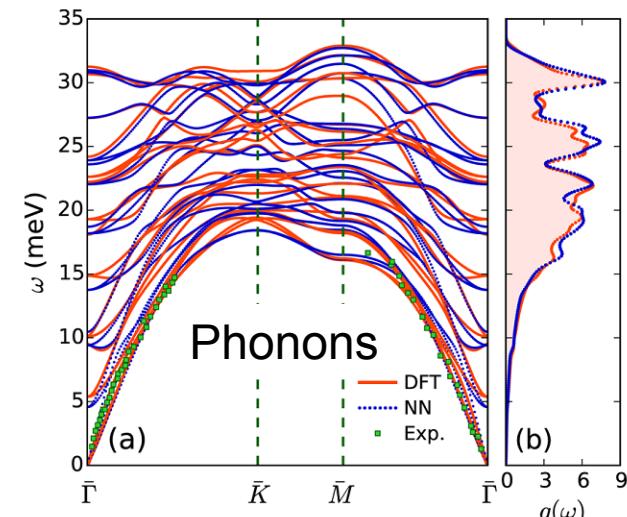
- A NNP that works for all supercells with different number of layers
- RuNNer code\*
- Symmetry functions:  $G^2$  and  $G^4$ ; 2 hidden layers: 20 nodes
- More than 25000 training data set
- VASP code for DFT calculations with RPBE functional



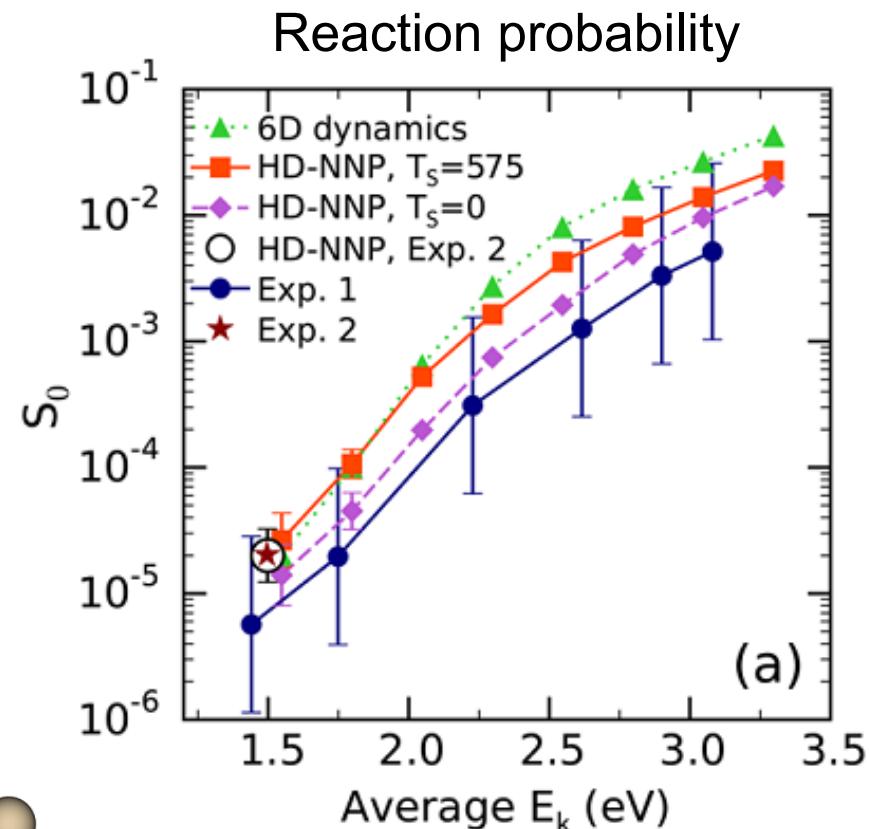
$$E = f_1^3 \left( b_1^3 + \sum_{l=1}^4 a_{l1}^{23} \cdot f_l^2 \left( b_l^2 + \sum_{k=1}^5 a_{kl}^{12} \cdot f_k^1 \left( b_k^1 + \sum_{j=1}^4 a_{jk}^{01} \cdot G_j \right) \right) \right)$$

\* J. Behler and M. Parrinello, Phys. Rev. Lett. 98, 146401 (2007)  
J. Behler, J. Chem. Phys. 134, 074106 (2011)

# $N_2$ on Ru(0001): fully mobile surface



Electronic and mechanical coupling

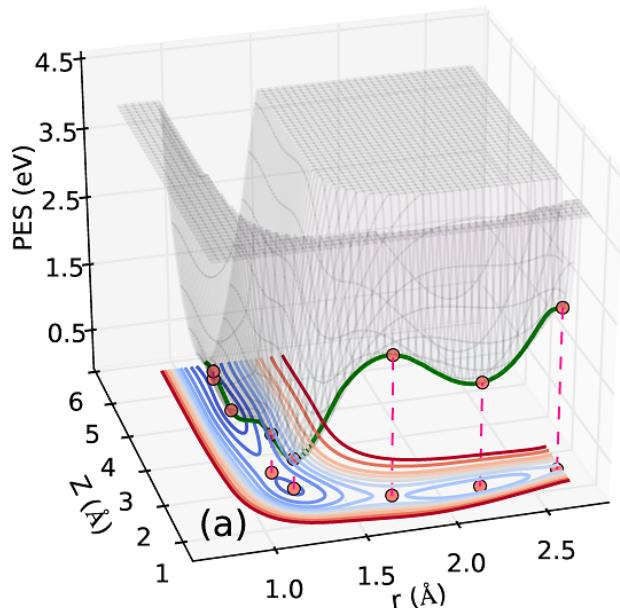


K. Shakouri, J. Behler, **JM**, and G.-J. Kroes,  
J. Phys. Chem. Lett. **8**, 2131 (2017)  
J. Phys. Chem. C (2018) DOI: 10.1021/acs.jpcc.8b06729

# Langevin dynamics 2: EF

$$m\ddot{\mathbf{R}} = -\nabla V(\mathbf{R})$$

potential energy surfaces (PESs)



I. Goikoetxea, J. Beltrán, **JM**, et al., New J. Phys. **14**, 013050 (2012).

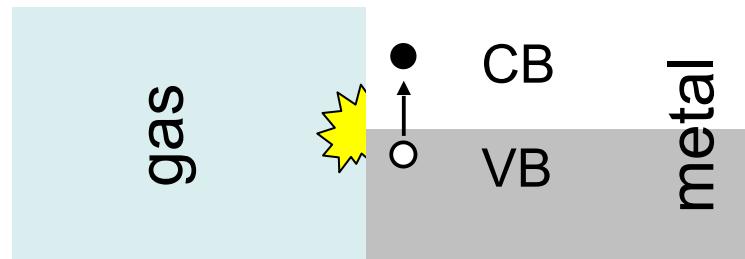
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K. Shakouri, J. Behler, **JM**, et al., J. Phys. Chem. Lett. **8**, 2131 (2017).

$$-\eta(\mathbf{R})\dot{\mathbf{R}} + \mathbf{F}_{\text{random}}$$

electronic friction (EF)



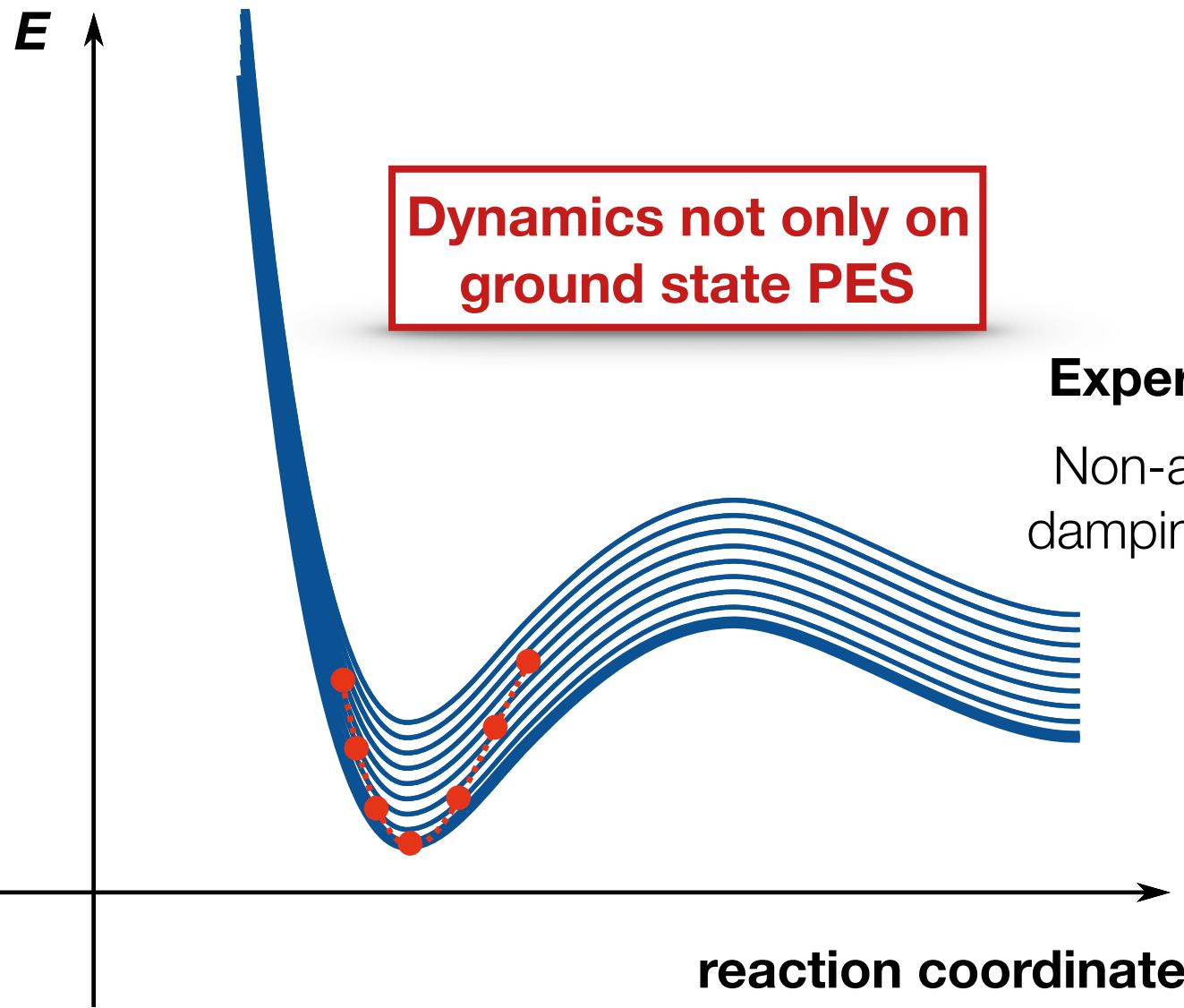
**JM** and K. Reuter, New J. Phys. **13**, 085010 (2011).

S. P. Rittmeyer, **JM** et al., Phys. Rev. Lett. **115**, 046102 (2015).

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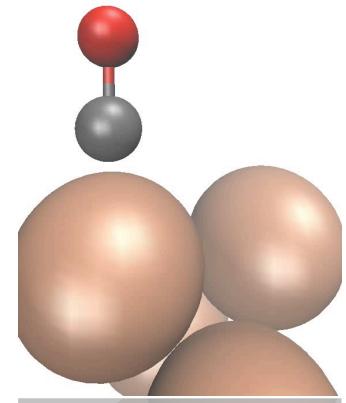
P. Spiering and **JM**, J. Phys. Chem. Lett. **9**, 1803 (2018).

# Beyond Born-Oppenheimer



**Experimental evidence**

Non-adiabatic vibrational damping on metal surfaces



# Orbital Dependent Friction

- Electron phonon couplings

$$g_{i\alpha}^{kab}(\vec{R}) = \left\langle \psi_{ak}(\vec{R}) \left| \frac{\partial V_{KS}(\vec{R})}{\partial R_{i\alpha}} \right| \psi_{bk}(\vec{R}) \right\rangle$$

			$j = 1$	$j = 2$
			$\beta = 1$	$\beta = 2$
			1	2
			3	
			1	
			2	
			3	

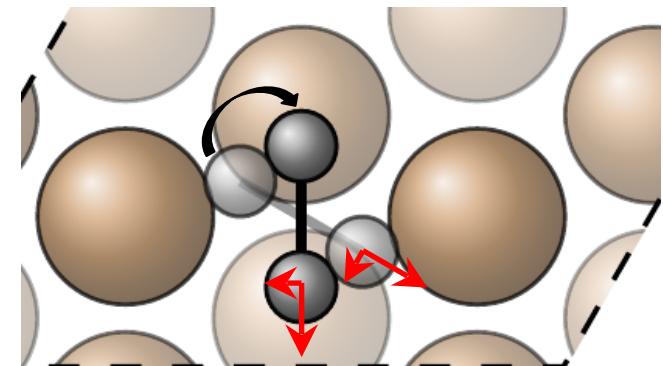
- Fermi's golden rule-like expression

$$\eta_{i\alpha j\beta}^{\text{ODF}}(\vec{R}) = h \sum_{abk} g_{i\alpha}^{kab}(\vec{R}) g_{j\beta}^{kab}(\vec{R})^* \delta(\epsilon_{ak} - \epsilon_F) \delta(\epsilon_{bk} - \epsilon_F)$$

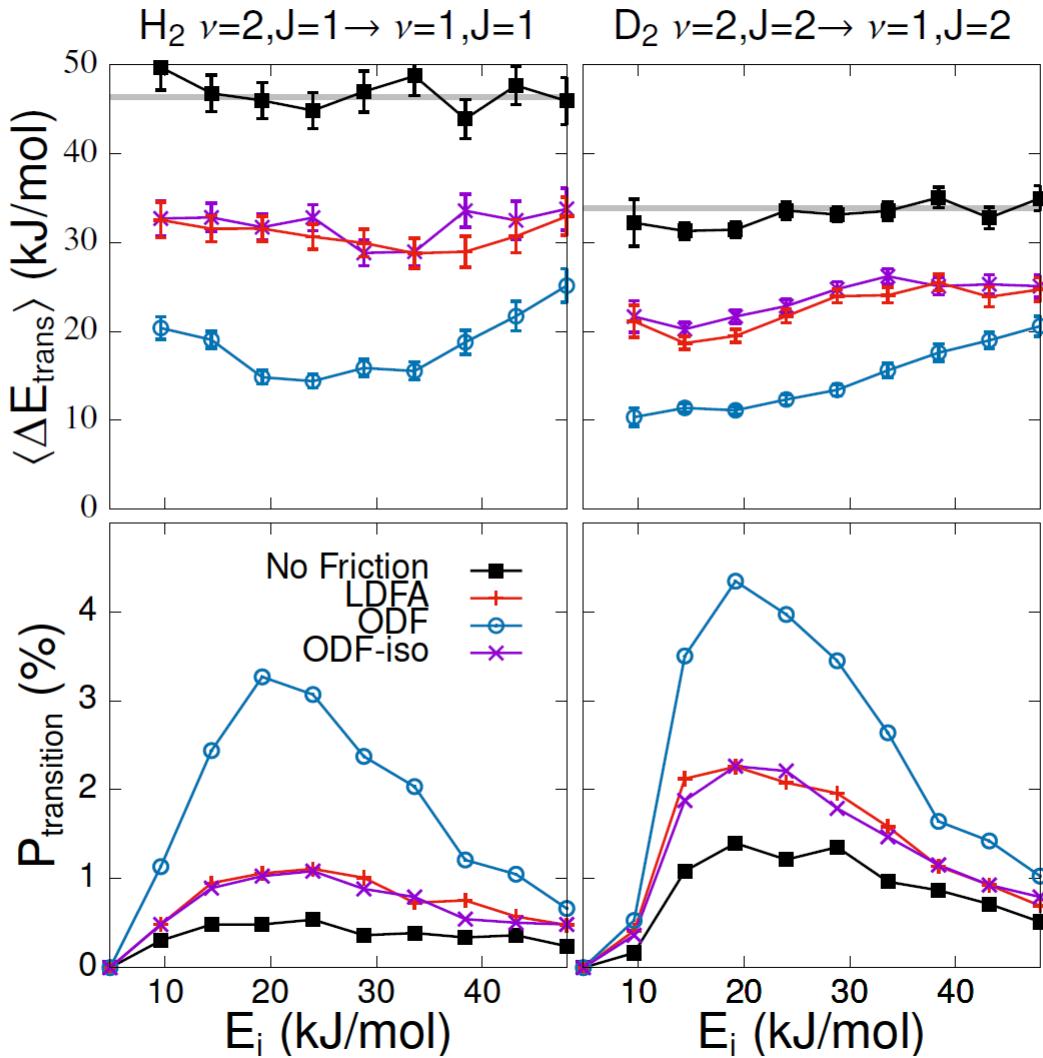
R. Maurer et al., Phys. Rev. B 94, 115432 (2016) & references therein

- no “chemically intuitive” functional form

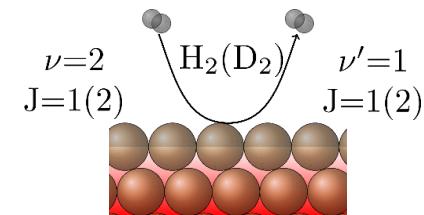
- NN fit(s) of 21 functions of 6 variables
- positive definiteness  
→ Cholesky decomposition
- challenge: symmetry inherent to tensor transformations  
intertwines tensor elements



# $H_2$ on Cu(111): fingerprint observables



$$\Delta E = \Delta E_{\text{vib}} + \underbrace{\Delta E_{\text{rot}}}_{=0} + \Delta E_{\text{trans}}$$



LDFA: scalar friction  
obtained from atoms-in-jellium modell  
("local-density friction approximation")

ODF-iso: scalar friction  
obtained from "isotropicalization"  
of ODF tensor

P. Spiering and JM  
J. Phys. Chem. Lett. **9**, 1803 (2018).

# Summary & Conclusions

- PES construction based on NNs:
  - specific coordinates for particular application domains  
(and further developments, e.g. PIP-NN)
  - some of-the-shelf implementations are nowadays available for “high-dimensional” schemes
- O<sub>2</sub> on Ag(111):
  - $>10^7$  trajectories allow to study reactive and scattering events
  - simple picture (“physisorption+chemisorption wells”) disputed
- N<sub>2</sub> on Ru(0001):
  - motion of surface atoms included → insights into phonons!
- NN-fits for electronic friction tensors have allowed to predict “fingerprints” for competing models  
(first application: H<sub>2</sub> on Cu(111))

# Acknowledgements



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@TU München



Jörg Behler



Paul Spiering



Khosrow Shakouri



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@FHI Berlin

**Thank you very much for your attention!**

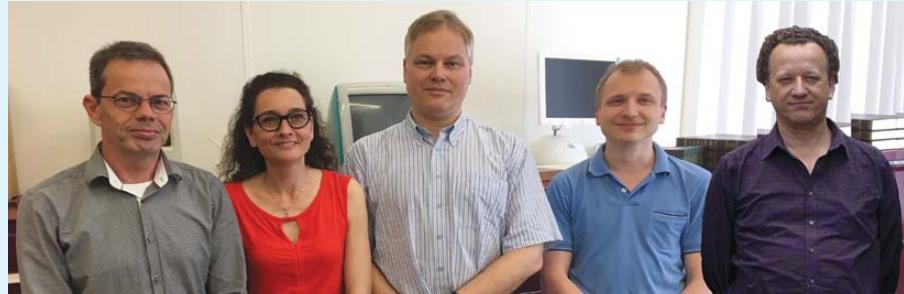


# Division Computational & Theoretical Chemistry

**Kick-off meeting:  
March 26, 2019  
Amsterdam**



Division Computational  
& Theoretical Chemistry



CTC-Board (fltr): Evert Jan Meijer, Célia Fonseca Guerra, Matthias Bickelhaupt, Jörg Meyer and Gerrit Groenenboom

**Kick-off meeting  
March 26, 2019, Amsterdam**

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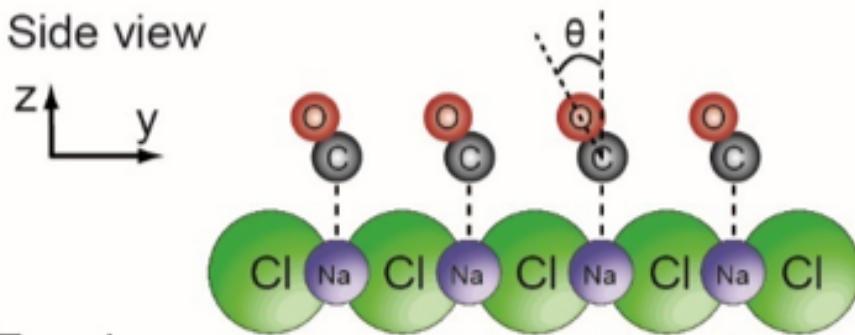
Visit the website: <https://ctc.kncv.nl/en/join-the-ctc>



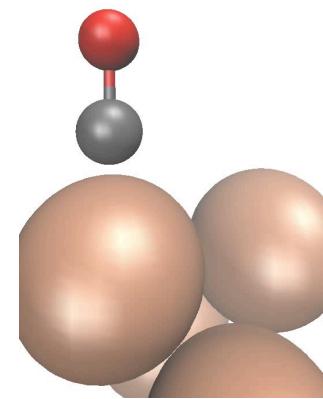
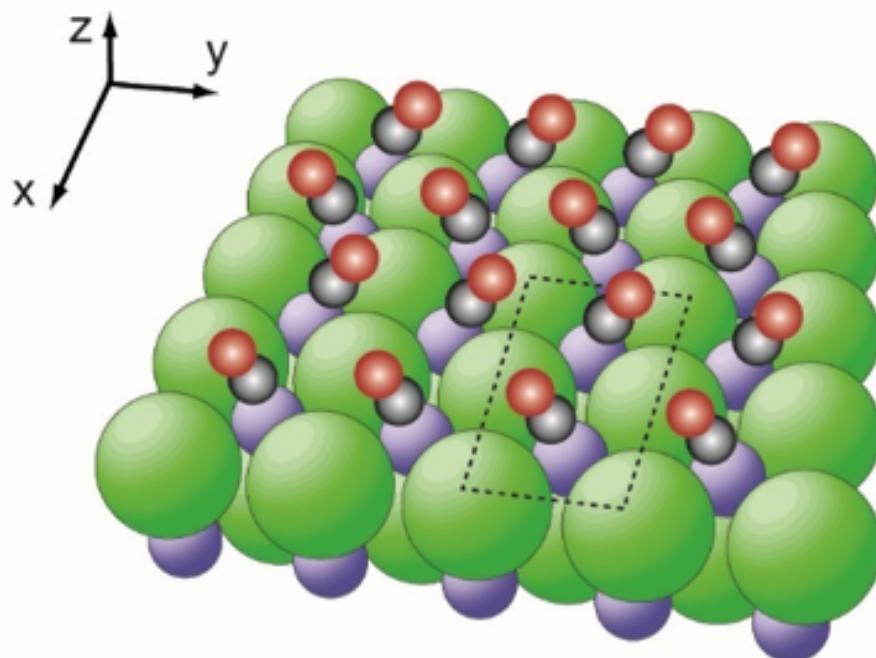
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# CO@NaCl(100) (1)

Side view



Top view



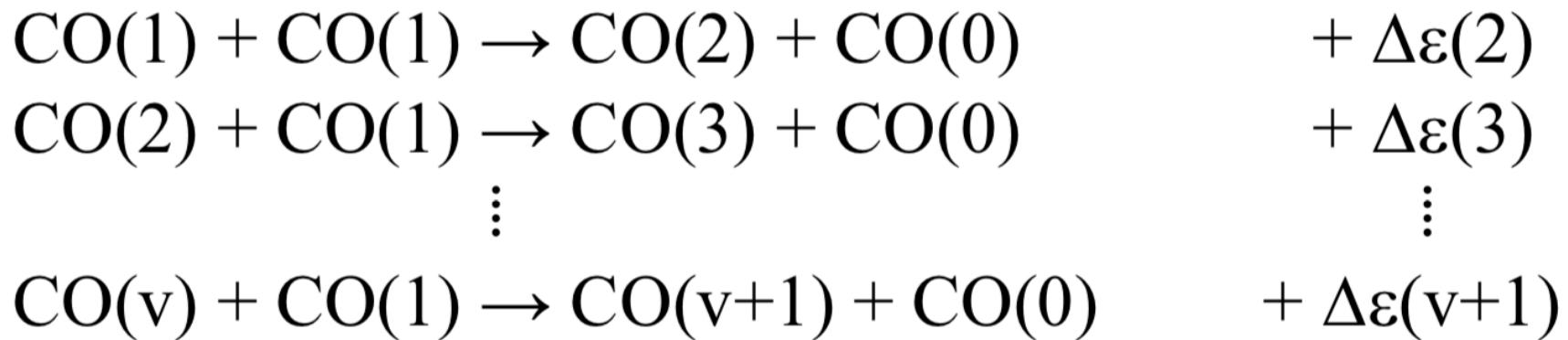
The Sommerfeld  
ground-wave limit  
for an adsorbed  
molecule at a surface

L. Chen, J. A. Lau, D. Schwarzer,  
J. Meyer, V. B. Verma, A. M. Wodtke

DOI: 10.1126/science.aav4278

# CO@NaCl(100) (2) - “State changes”

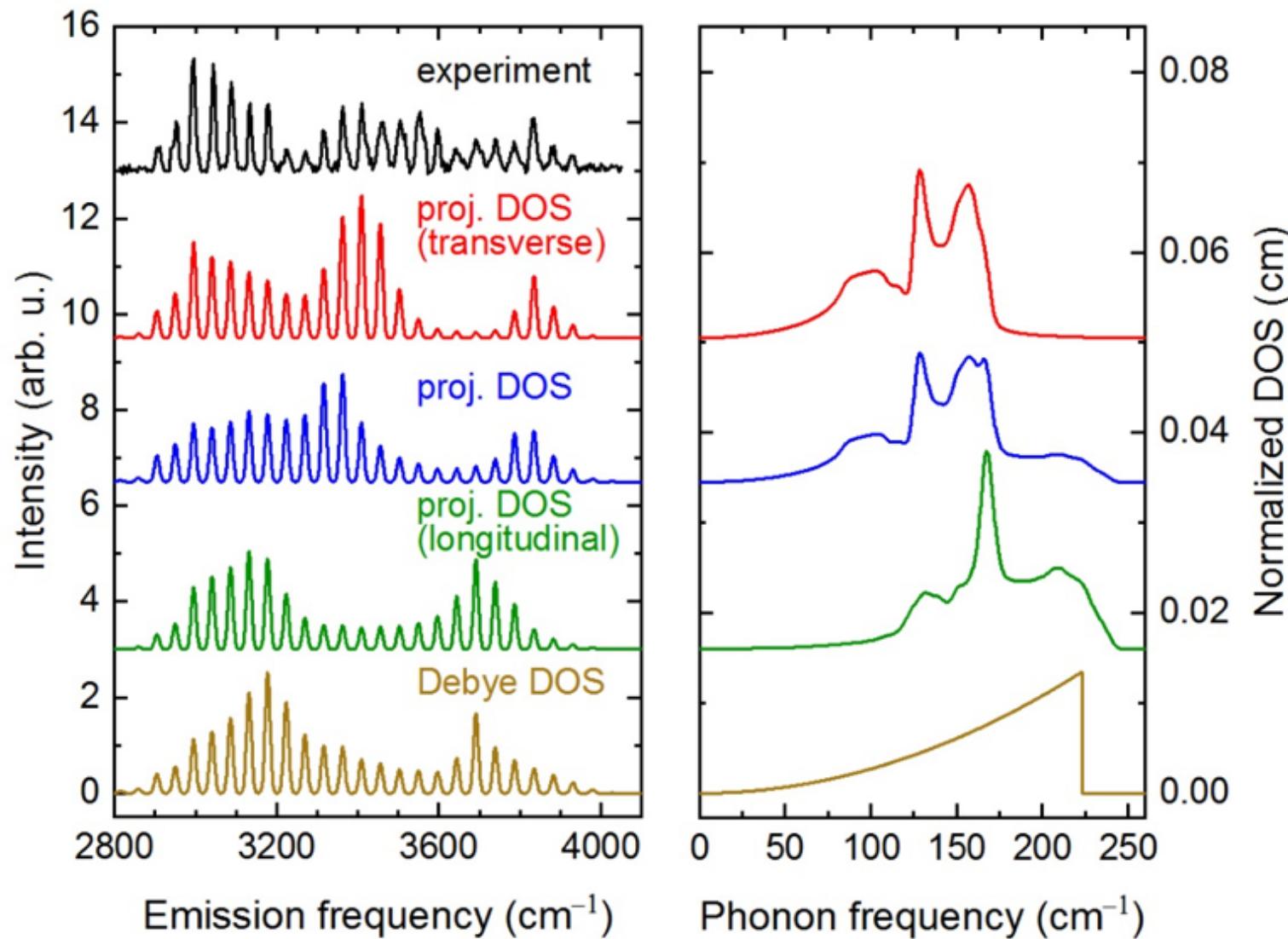
- Pooling



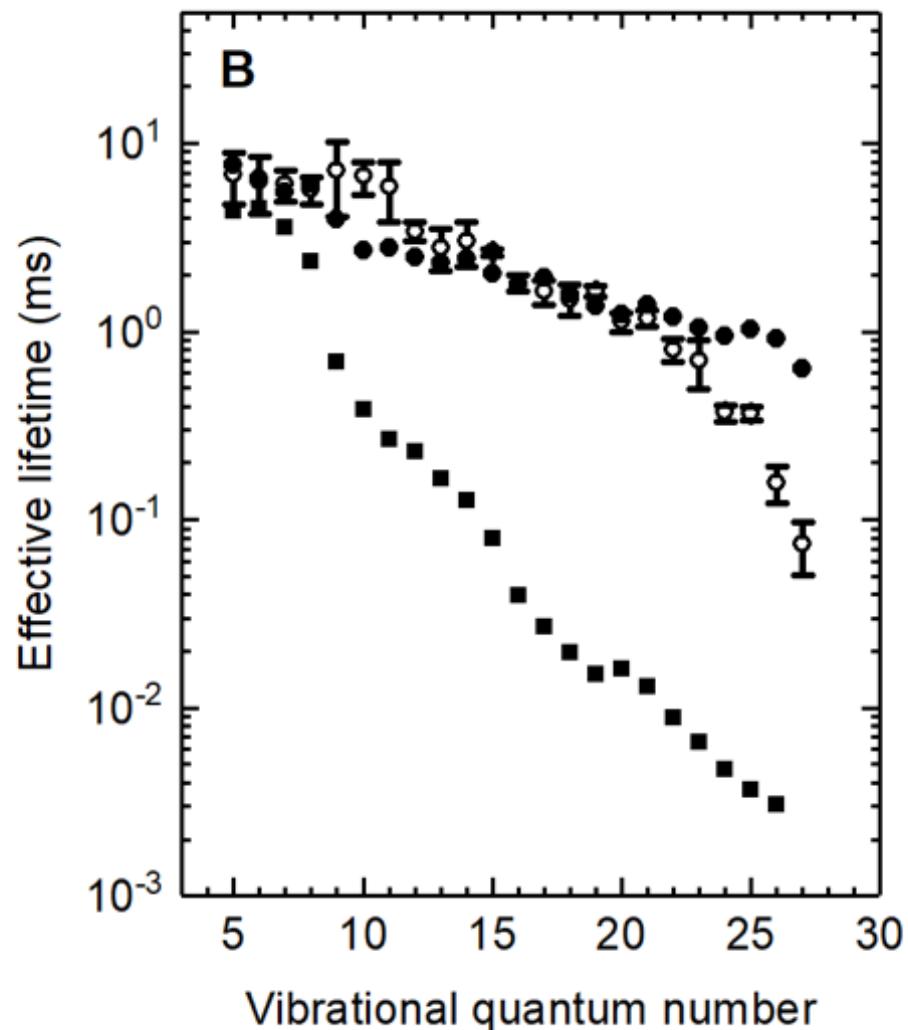
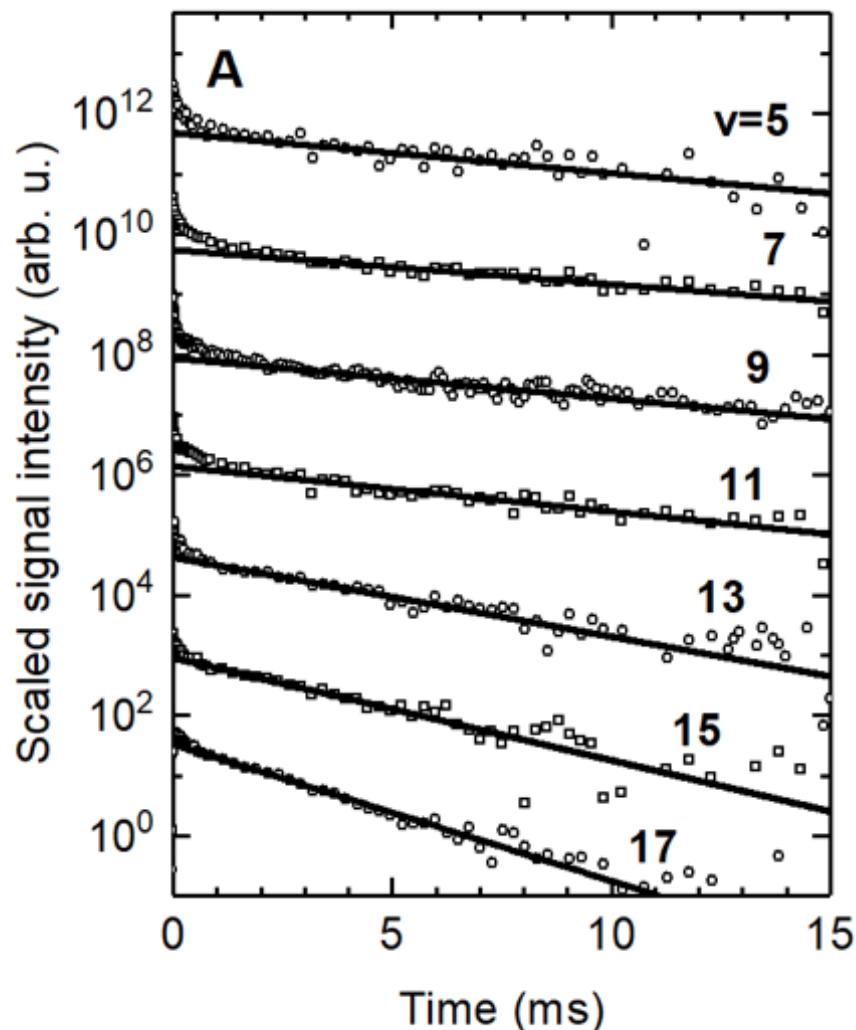
- Dissipation



# CO@NaCl(100) (3) - Phonons

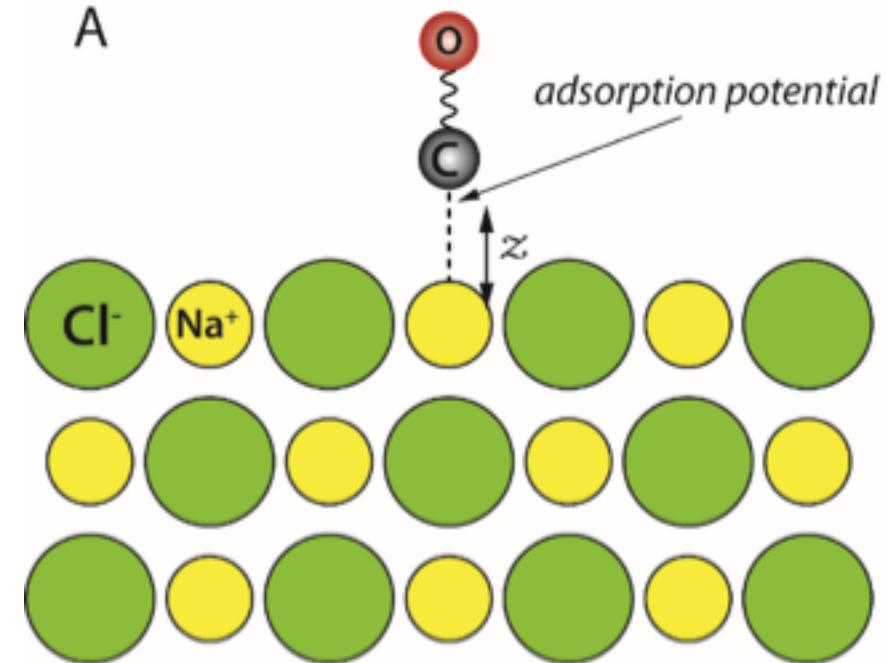


# CO@NaCl(100) (4) - Lifetimes



# CO@NaCl(100) (5) - Theories...

A



B

