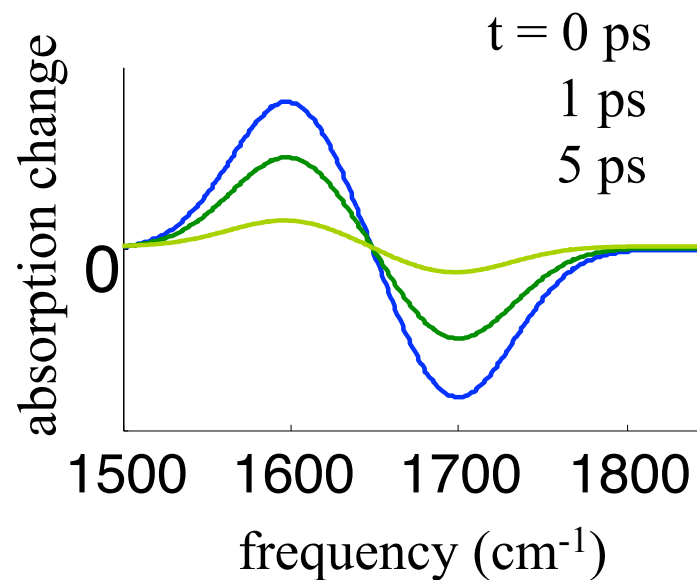
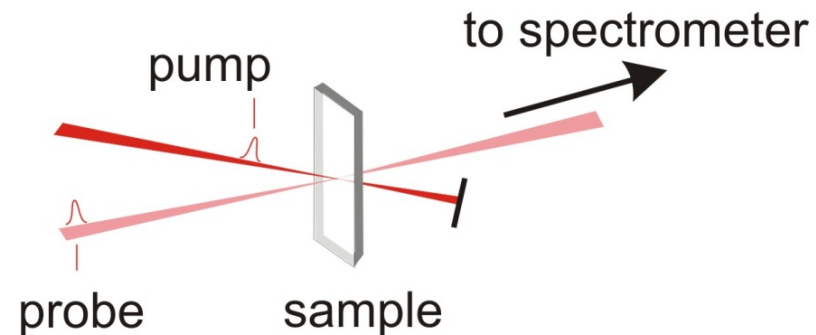
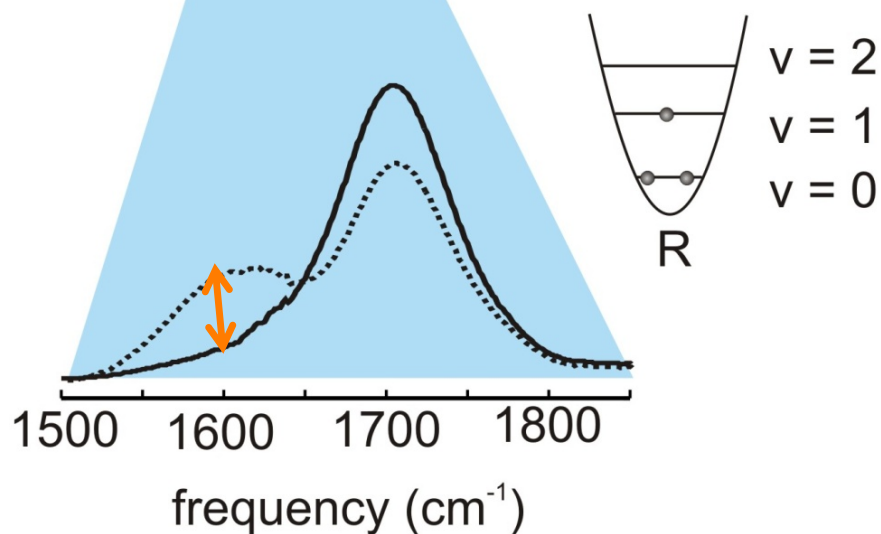
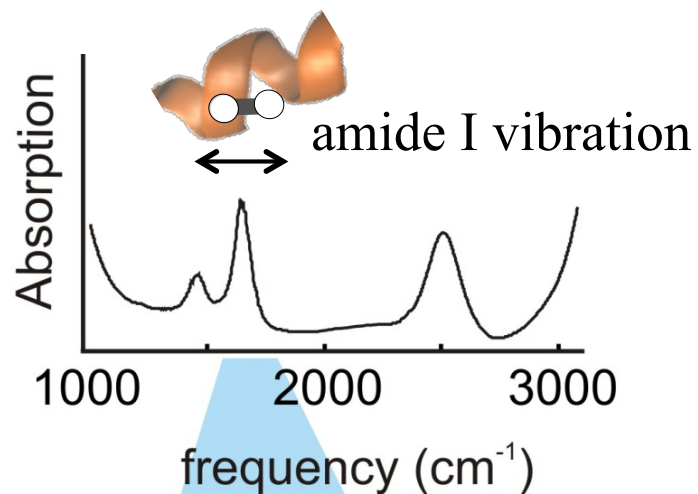




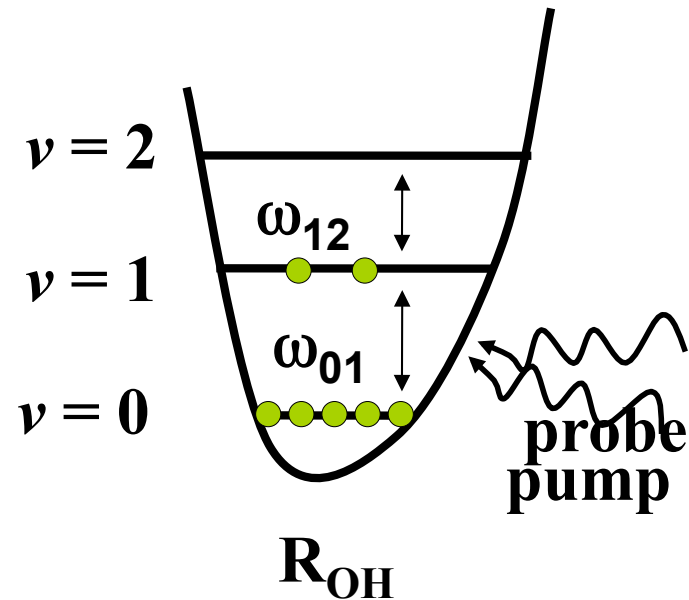
Pump-probe spectroscopy

Pump-probe spectroscopy

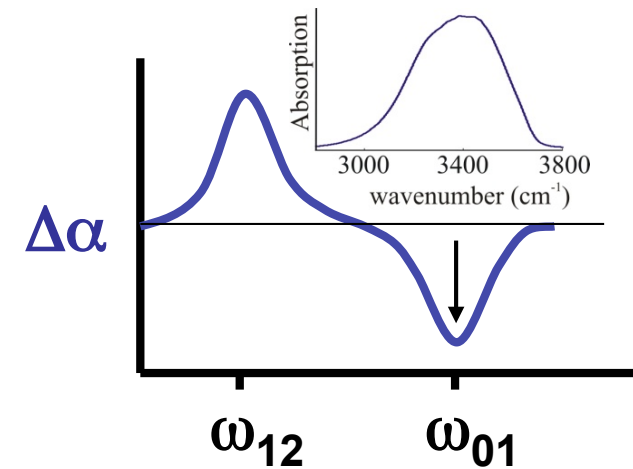


Pump-probe: principle

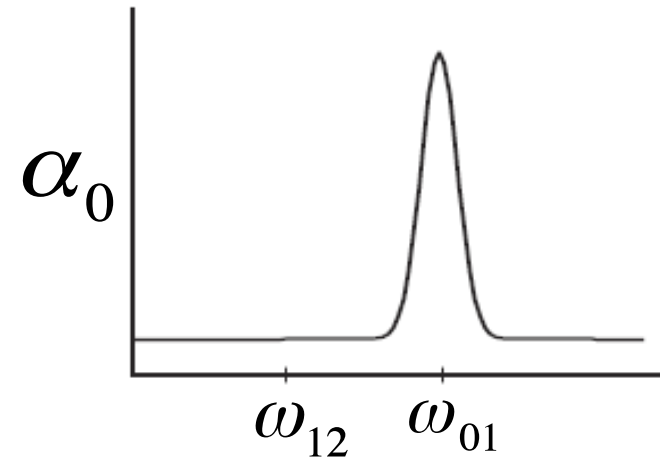
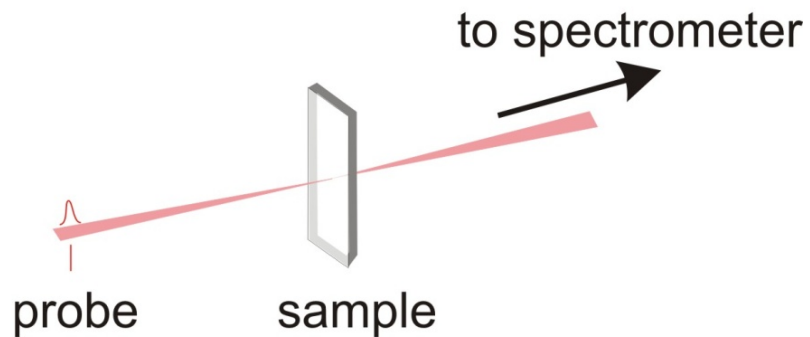
Energy levels



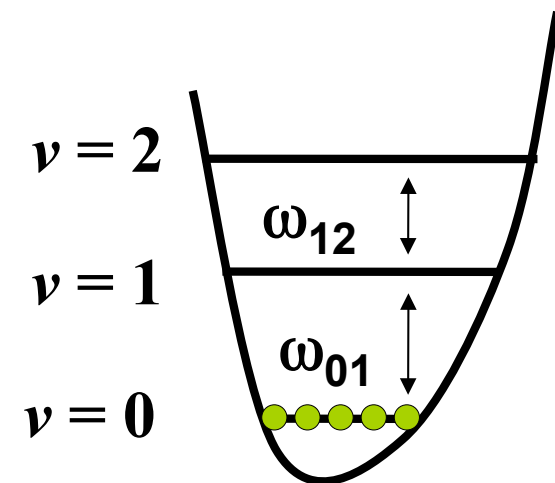
Transient spectrum



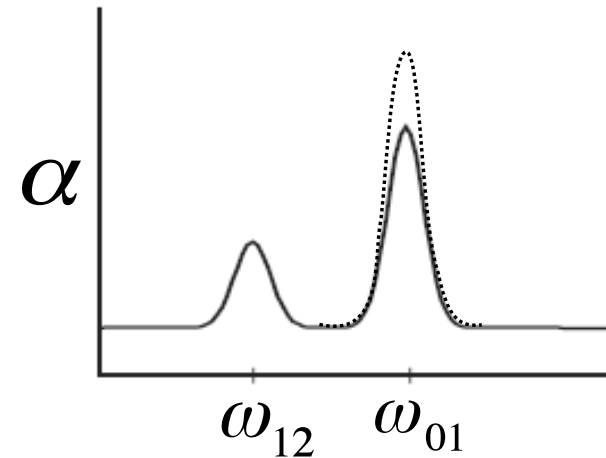
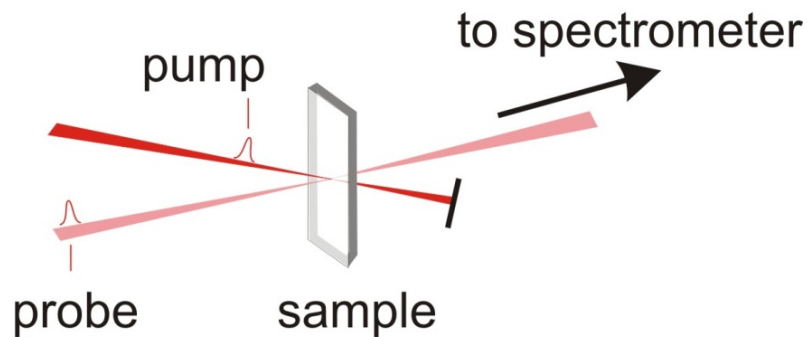
Pump-probe spectroscopy



$$\alpha_0 = \sigma_{01}(\omega)n$$

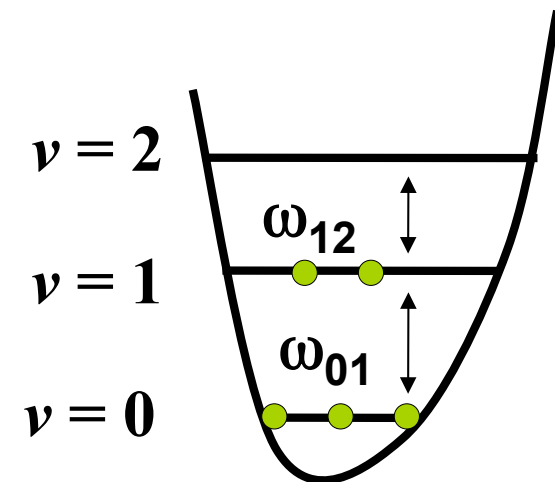


Pump-probe spectroscopy

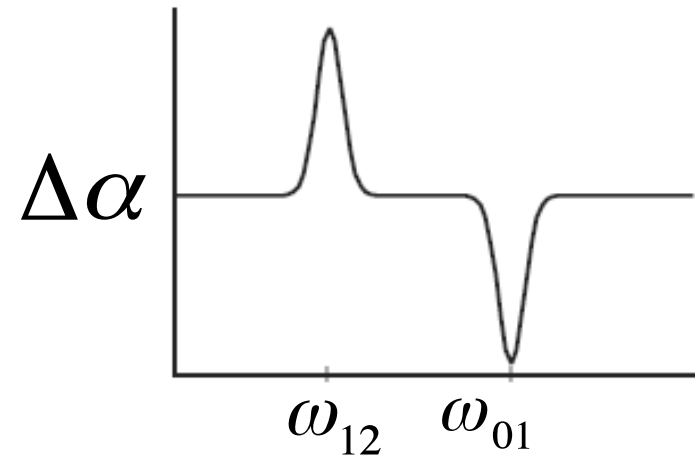
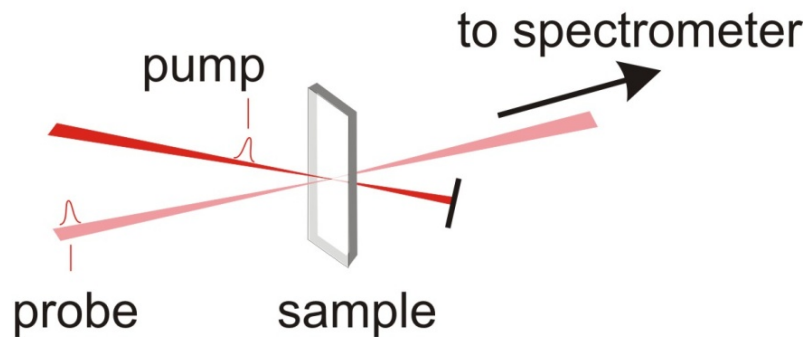


$$\alpha = \sigma_{01}(\omega)(n - 2N_1) + \sigma_{12}(\omega)N_1$$

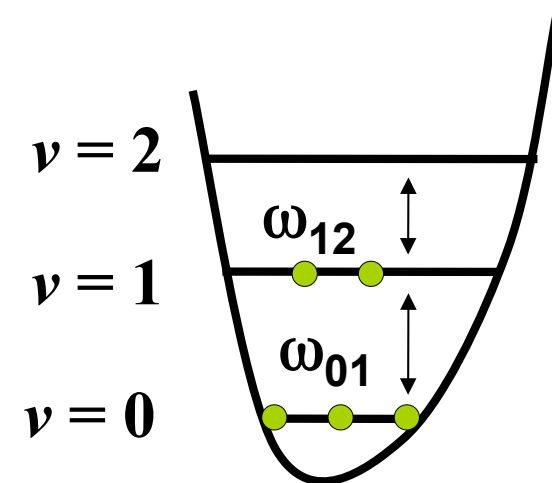
$$\alpha_0 = \sigma_{01}(\omega)n$$



Pump-probe spectroscopy



$$\Delta\alpha = -2N_1\sigma_{01}(\omega) + \sigma_{12}(\omega)N_1$$

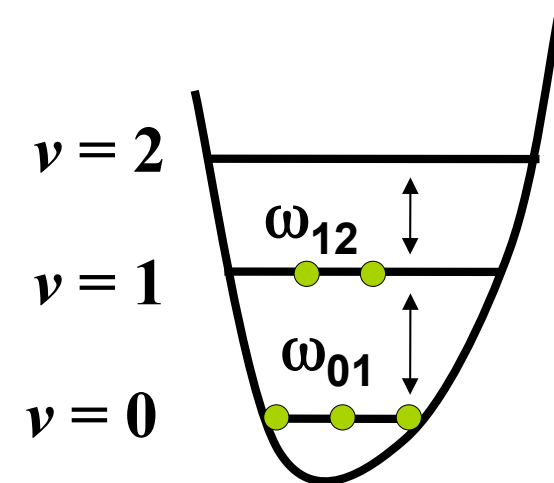
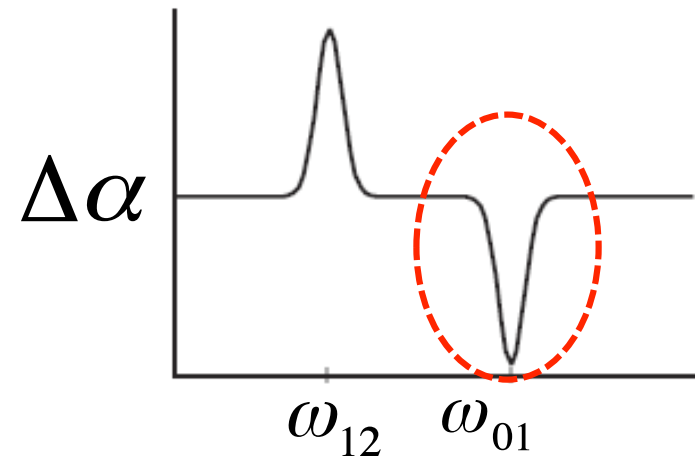


Pump-probe spectroscopy

$$\Delta\alpha = -2N_1\sigma_{01}(\omega) + \sigma_{12}(\omega)N_1$$

Bleach has two contributions

- Ground state depletion
- Stimulated emission

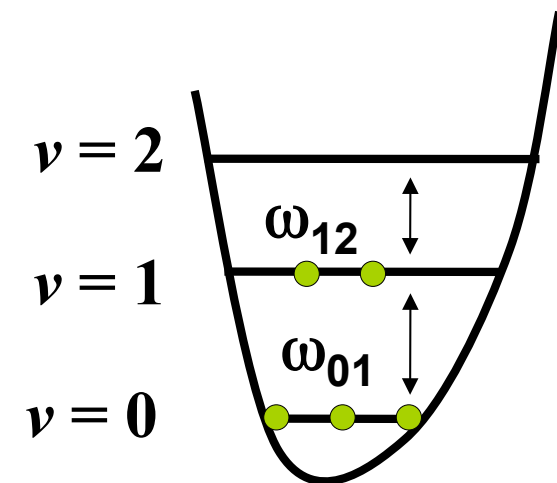
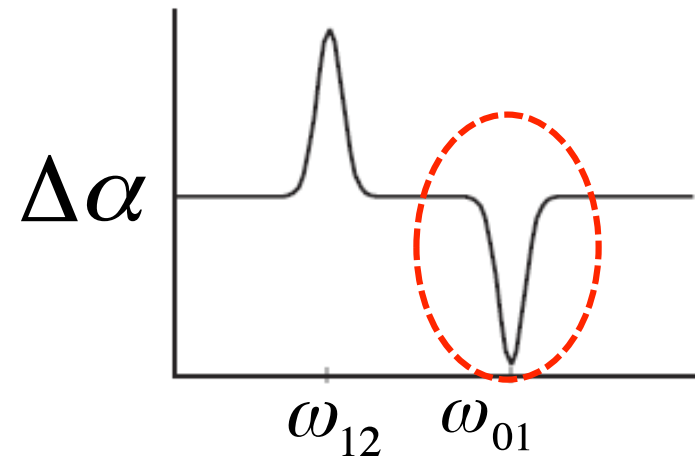


Pump-probe spectroscopy

$$\Delta\alpha = [-2\sigma_{01}(\omega) + \sigma_{12}(\omega)]N_1$$

Bleach has two contributions

- Ground state depletion
- Stimulated emission



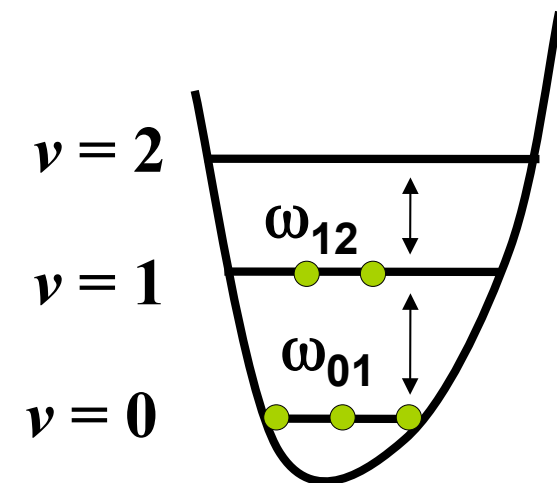
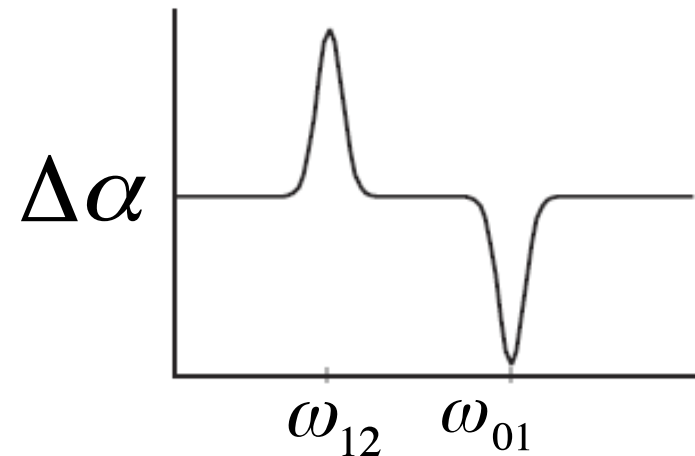
Pump-probe spectroscopy

$$\Delta\alpha = [-2\sigma_{01}(\omega) + \sigma_{12}(\omega)]N_1$$

For a perfect harmonic oscillator

$$\sigma_{12}(\omega) = 2\sigma_{01}(\omega)$$

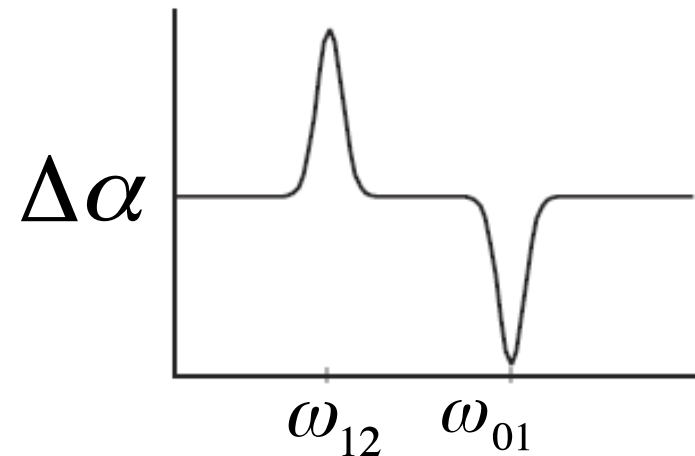
No pump-probe signal!



Pump-probe spectroscopy

$$\Delta\alpha = -2N_1\sigma_{01}(\omega) + \sigma_{12}(\omega)N_1$$

Galileo



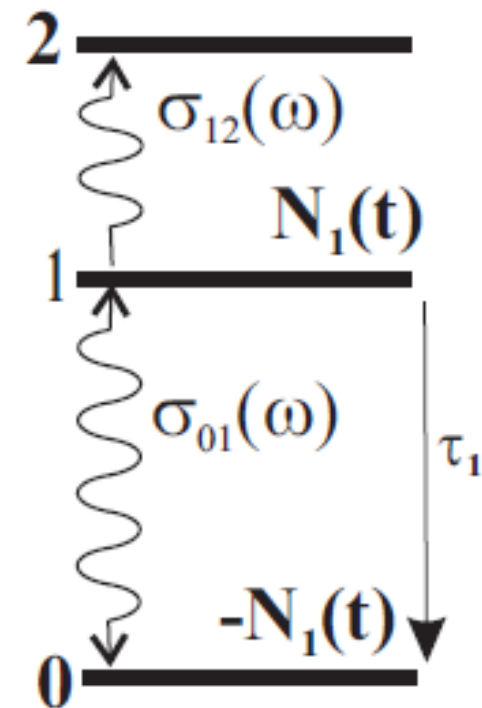
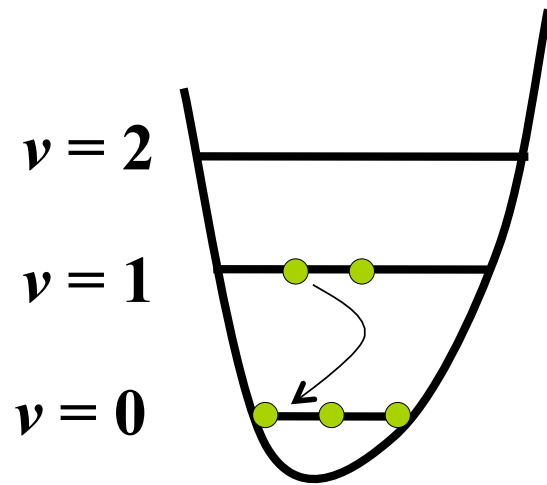
Anharmonicity is required for a pump-probe signal



Vibrational relaxation and its effects

Vibrational relaxation

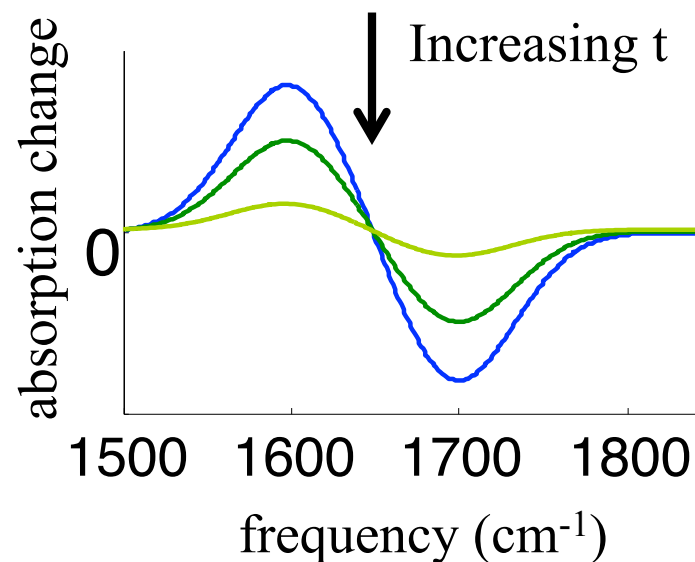
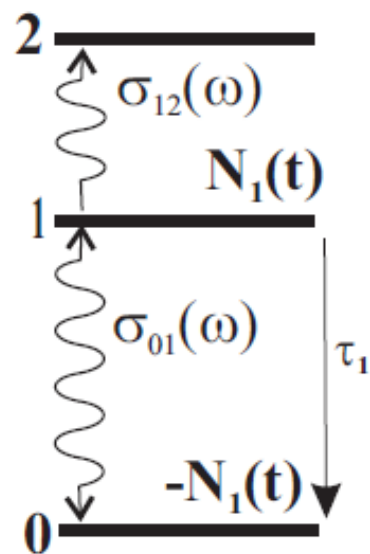
Molecules relax to the ground state



$$\Delta\alpha(\omega, t) = [-2\sigma_{01}(\omega) + \sigma_{12}(\omega)]N_1(t)$$

Vibrational relaxation

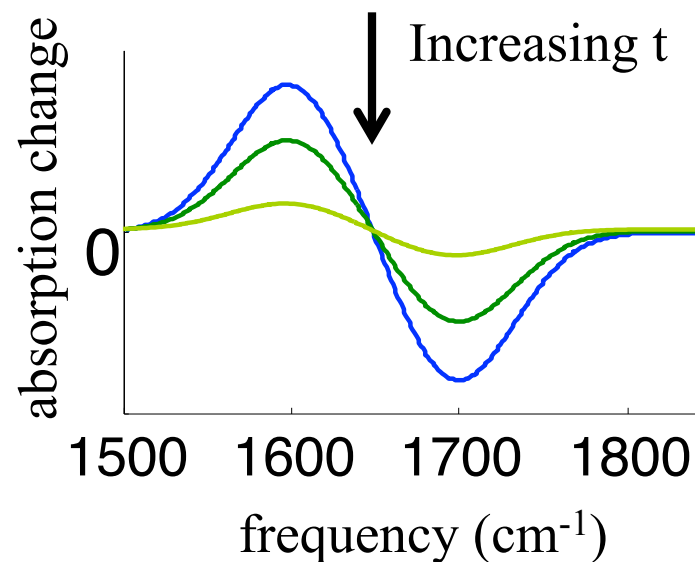
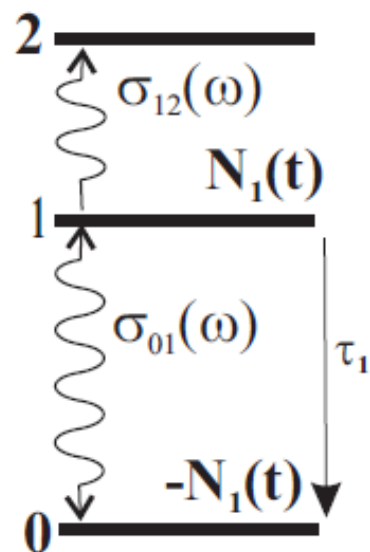
Molecules relax to the ground state



$$\Delta\alpha(\omega, t) = [-2\sigma_{01}(\omega) + \sigma_{12}(\omega)]N_1(t)$$

Vibrational relaxation

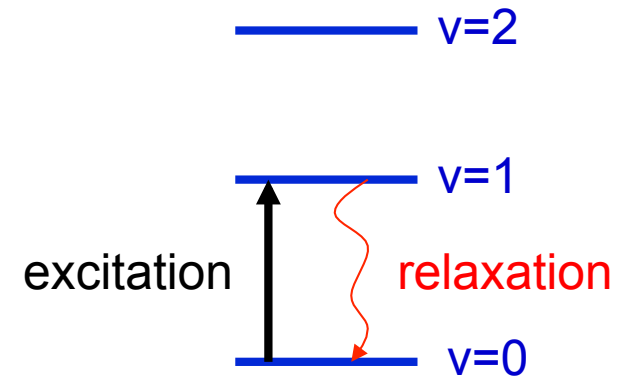
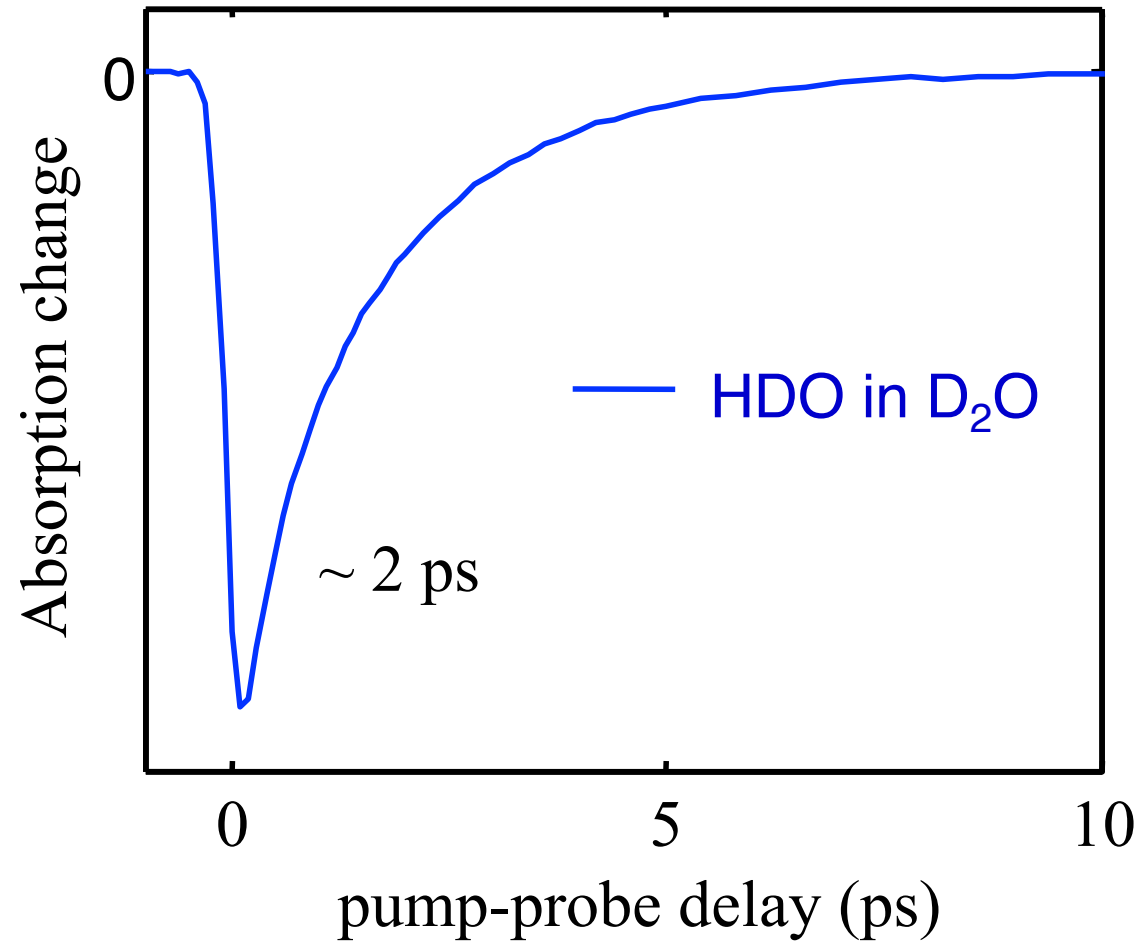
Molecules relax to the ground state



$$\Delta\alpha(\omega, t) = [-2\sigma_{01}(\omega) + \sigma_{12}(\omega)]N_1(0)e^{-t/\tau_1}$$

Simplest case: exponential relaxation

Delay time scan (shows vibrational relaxation)



Exponential relaxation

When do we get exponential relaxation (or decay)?

What does it mean microscopically?

Spontaneous emission rate (Einstein theory, Wigner-Weisskopf)

$$1/\tau_1 = \frac{\omega_{01}^3 |\mu_{01}|^2}{3\pi\epsilon_0 \hbar c^3}$$

Electronic transitions \rightarrow \sim nanosecond

Vibrational transitions \rightarrow microsecond-millisecond

Exponential relaxation

When do we get exponential relaxation (or decay)?
What does it mean microscopically?

Radiative decay

Vibrational transitions → microsecond-millisecond

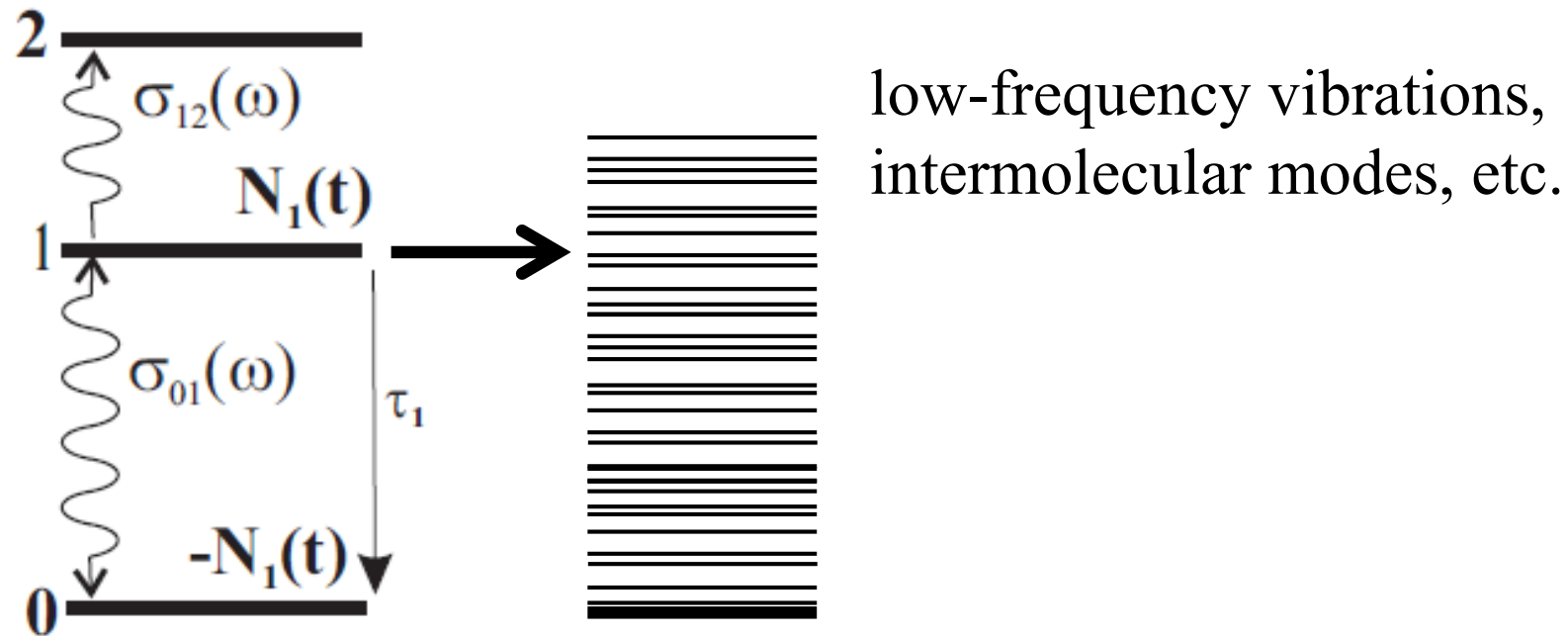
Non-radiative decay rate

Vibrational transitions → picosecond

In the condensed phase vibrational excitations decay non-radiatively on a picosecond timescale.

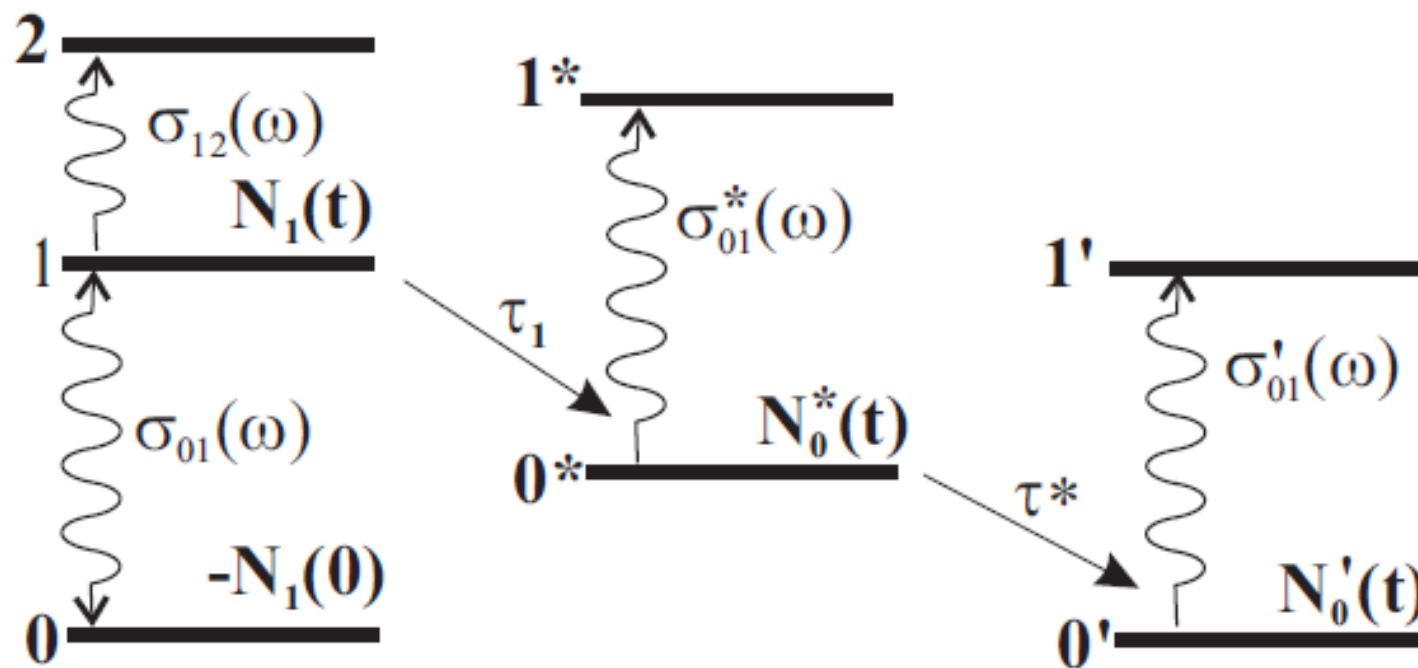
Exponential relaxation

Many closely lying states that are nearly resonant



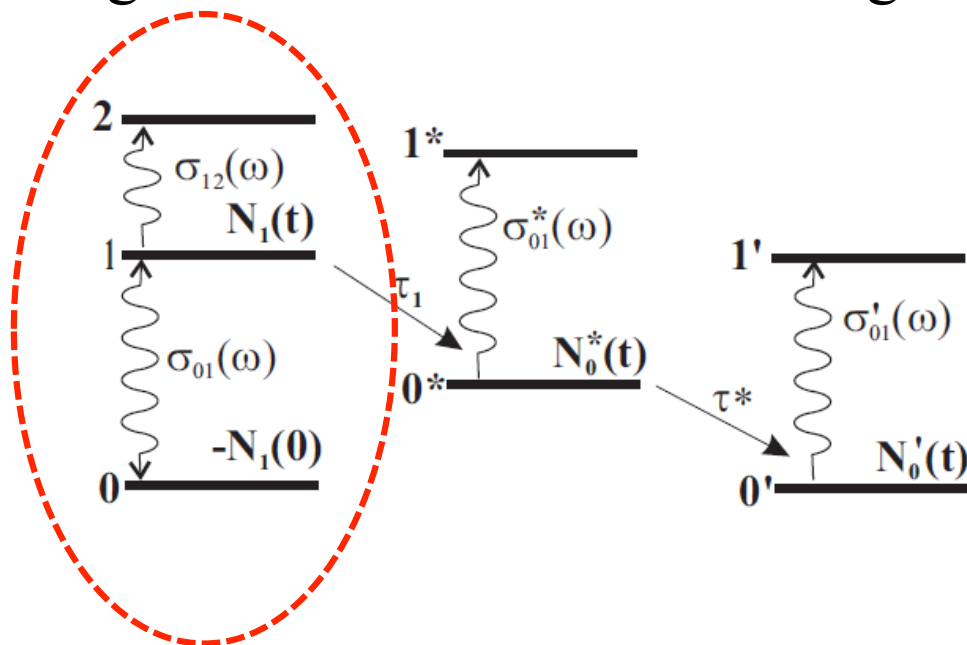
Relaxation mechanisms

E.g. relaxation of OD stretching vibration of HDO in H₂O



Relaxation mechanisms

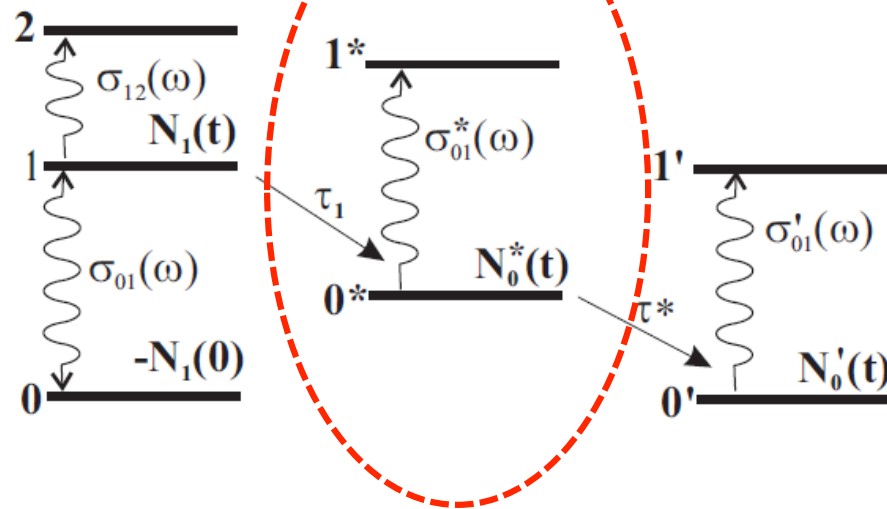
E.g. relaxation of OD stretching vibration of HDO in H₂O



Vibrational anharmonicity

Relaxation mechanisms

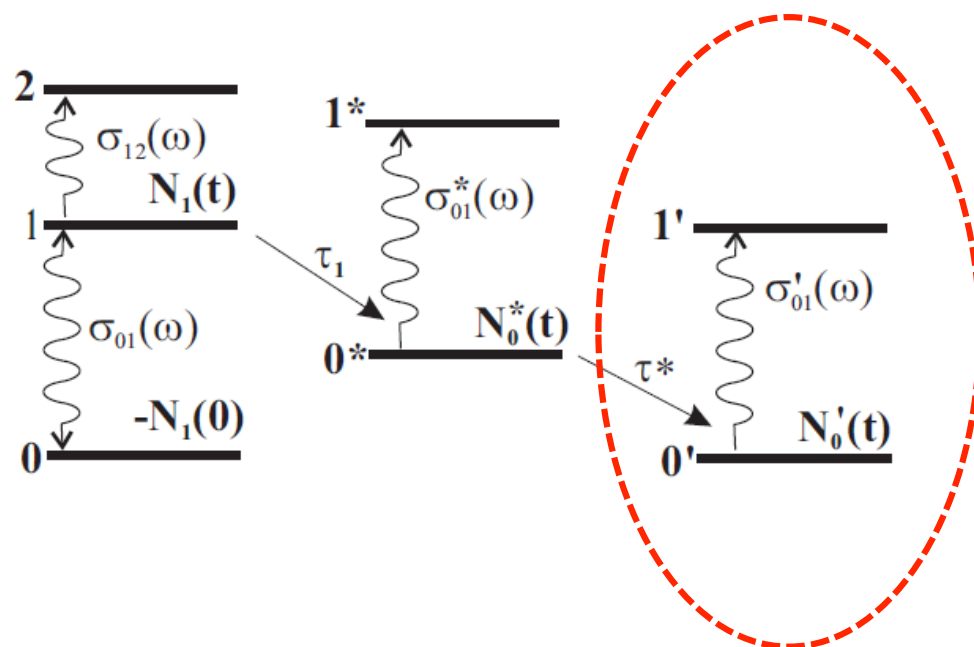
E.g. relaxation of OD stretching vibration of HDO in H₂O



Low-frequency mode excited (anharmonic shift)

Relaxation mechanisms

E.g. relaxation of OD stretching vibration of HDO in H₂O

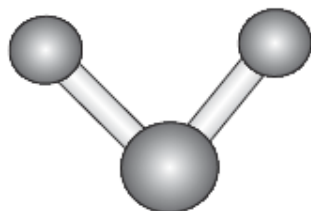


Sample heating

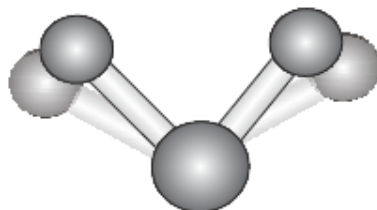
Anharmonic vibrational couplings

(a)

bend not excited

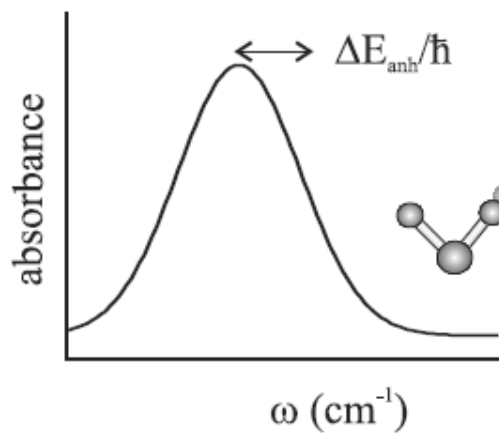
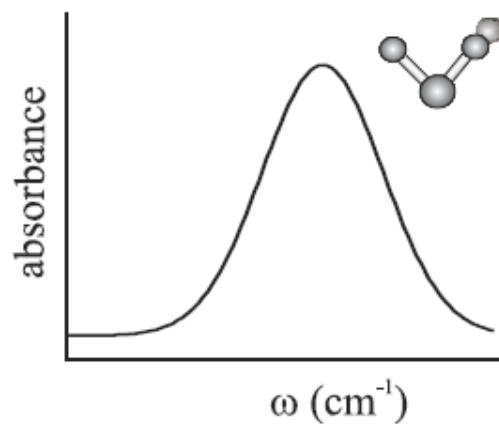


bend excited

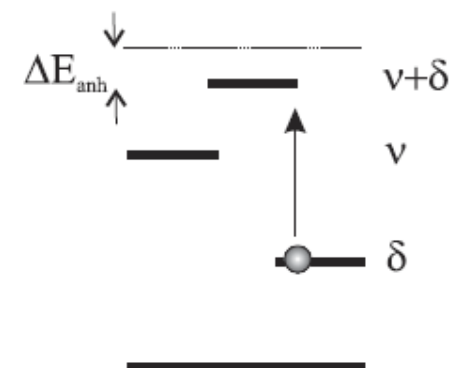
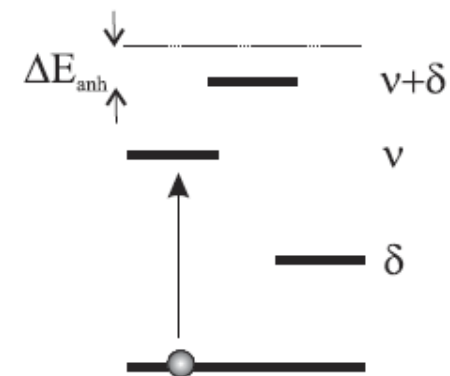


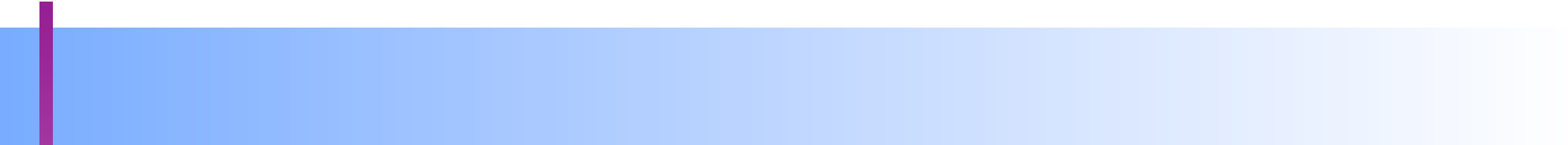
(b)

OH stretch spectrum



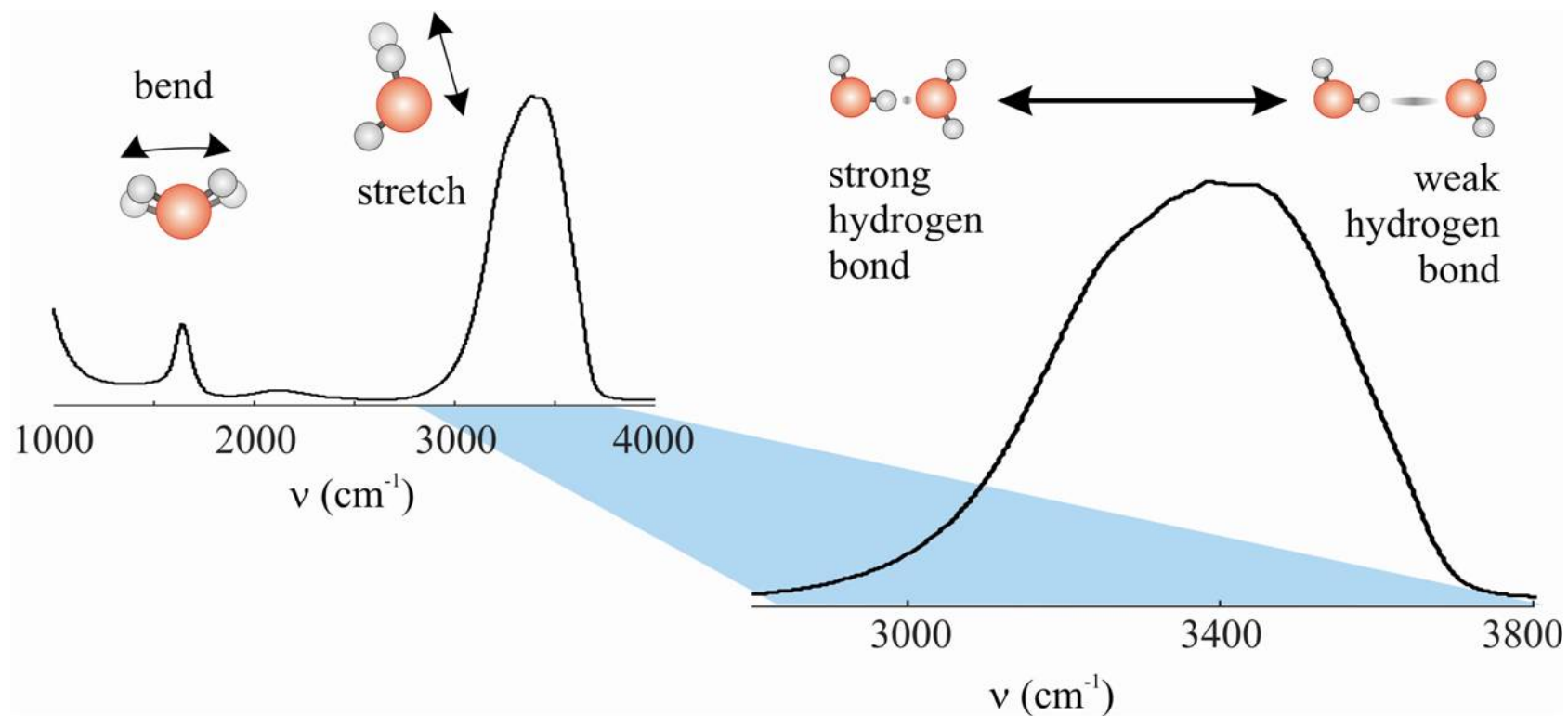
(c)



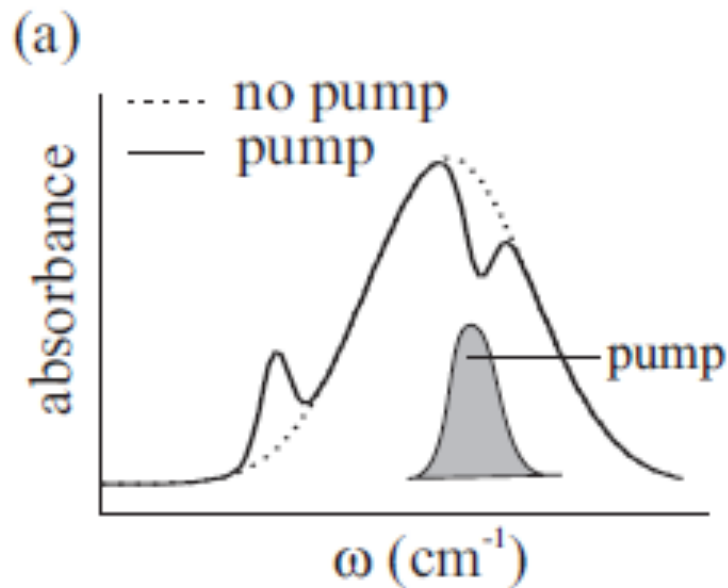


Inhomogeneous broadening and spectral diffusion

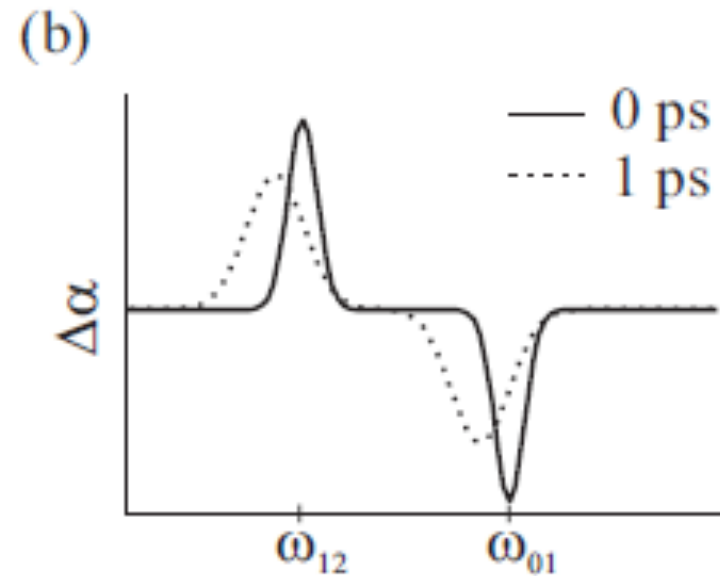
Inhomogeneous broadening



Probing spectral diffusion



Spectral hole

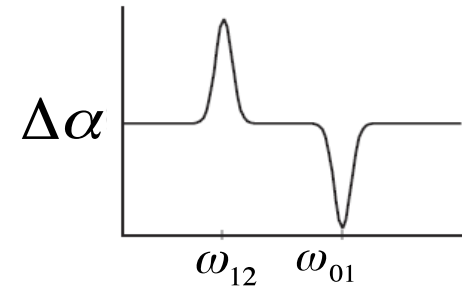


Spectral hole in
transient spectrum

Spectral hole broadens due to spectral diffusion

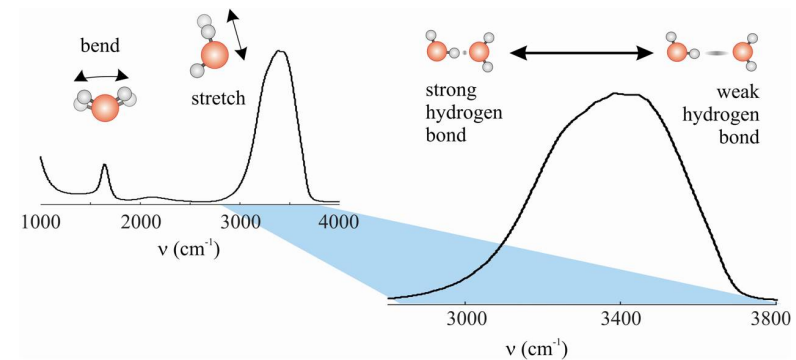
Summary ‘Pump-probe spectroscopy’

- Origin of the vibrational pump-probe signal → anharmonicity



- Vibrational relaxation

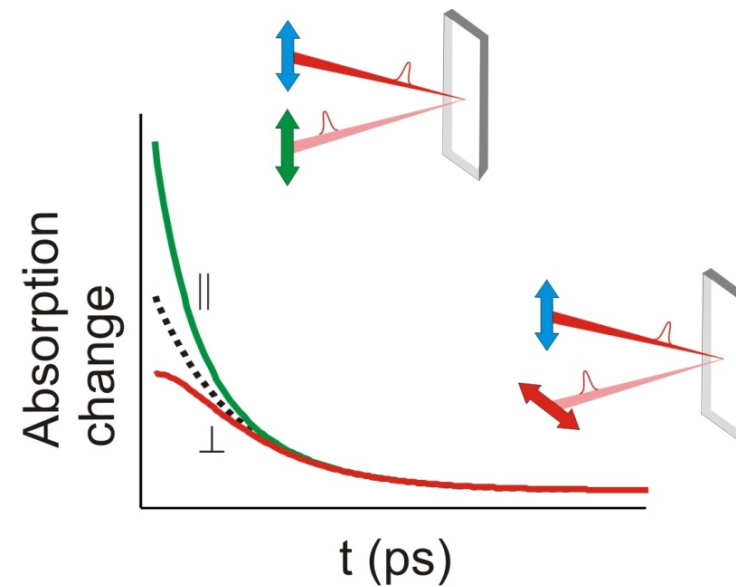
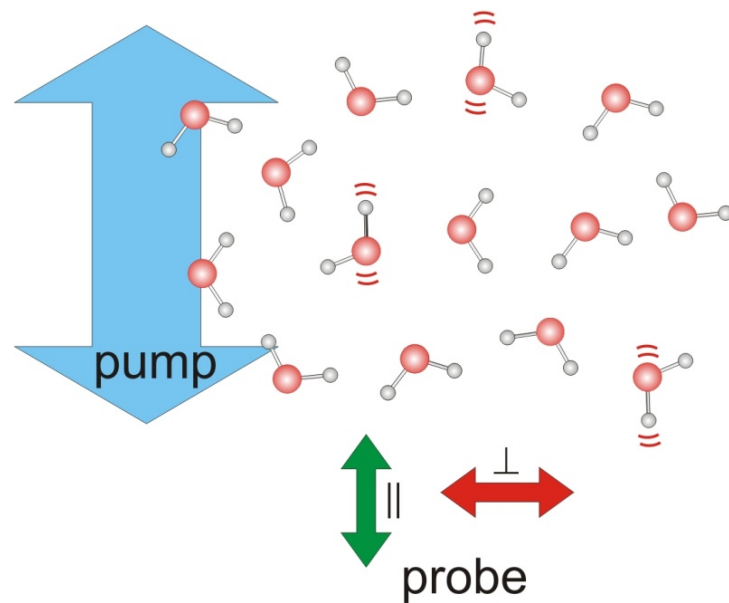
- Spectral diffusion





Polarization properties of the pump-probe signal

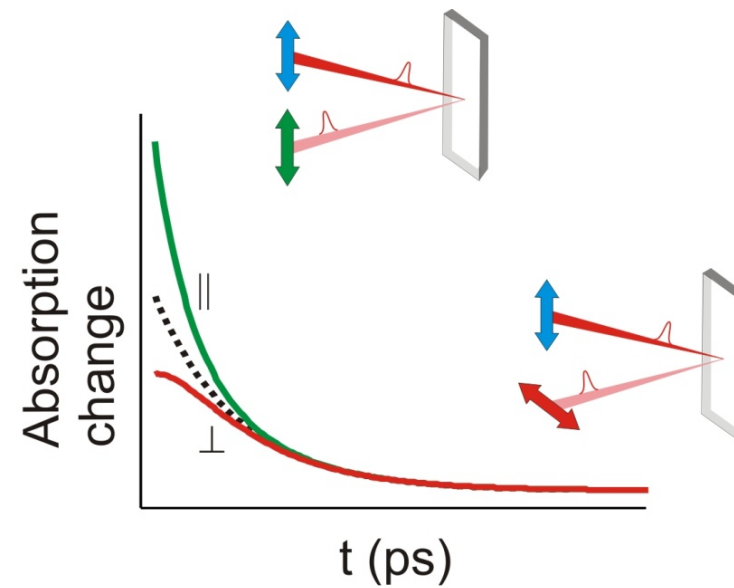
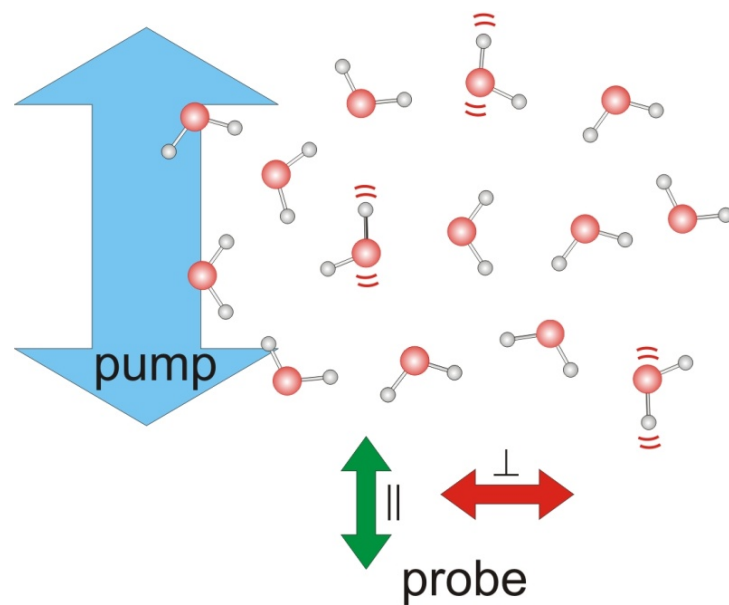
Polarization



To study vibrational relaxation we need the isotropic signal:

- which depends only on the concentration of excited molecules
- which is not affected by orientational motion

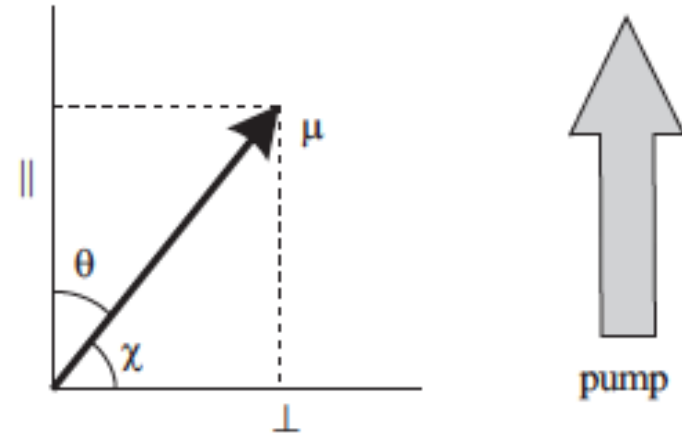
Polarization



$$\Delta\alpha_{iso} \neq \frac{\Delta\alpha_{||} + \Delta\alpha_{\perp}}{2}$$

Polarization

In two dimensions



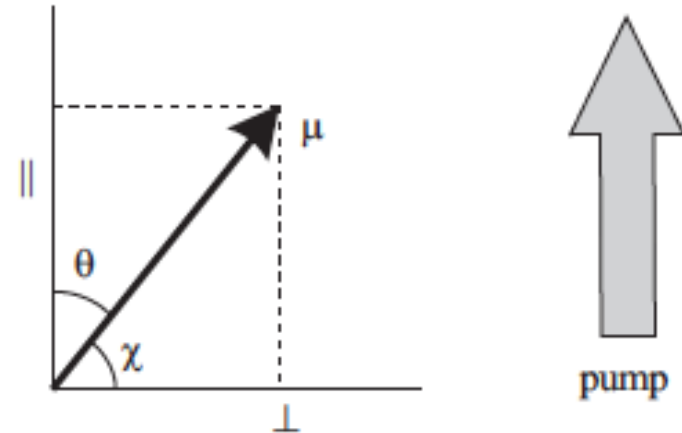
Contribution of an excited vibration to the parallel and perpendicular signal:

$$\Delta\alpha_{||} \propto \cos^2 \theta,$$

$$\Delta\alpha_{\perp} \propto \cos^2 \chi$$

Polarization

In two dimensions



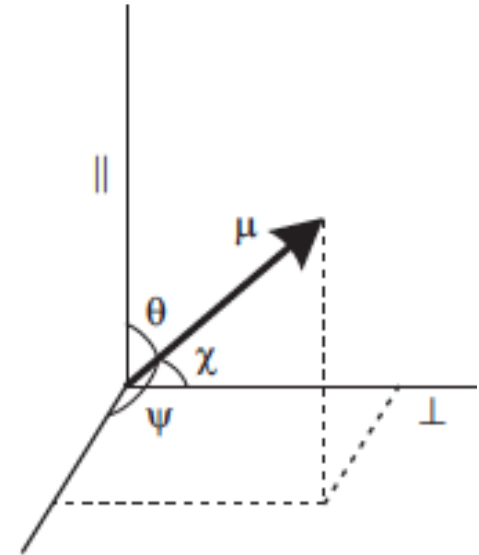
The following quantity is independent of orientation

$$\Delta\alpha_{||} + \Delta\alpha_{\perp} \propto \cos^2 \theta + \cos^2 \chi$$

In two dimensions this would be the isotropic signal

Polarization

In three dimensions

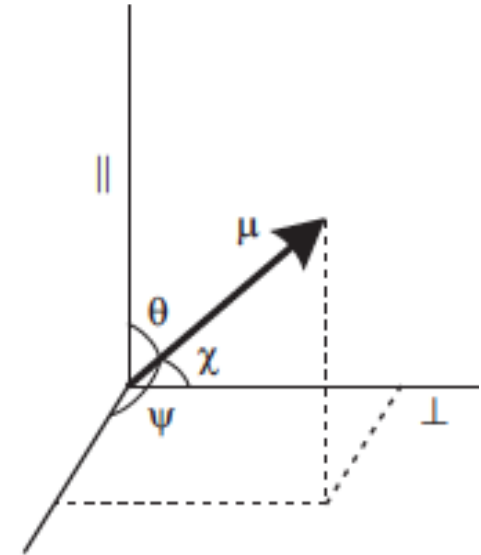


Independent of the orientation of an excited dipole

$$\cos^2 \theta + \cos^2 \chi + \cos^2 \psi$$

Polarization

In three dimensions



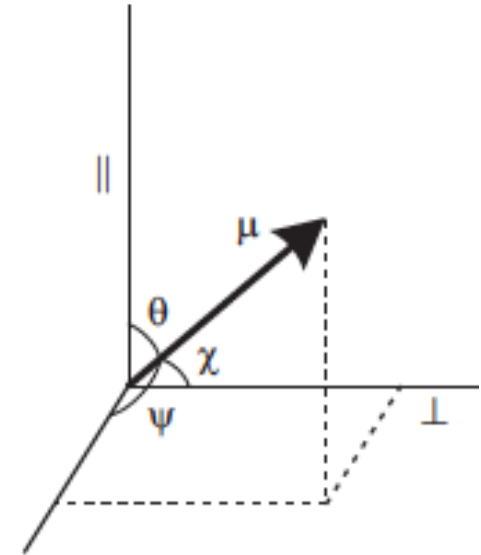
However in a macroscopic measurement one probes the average over all molecules

$$\langle \cos^2 \theta \rangle + \langle \cos^2 \chi \rangle + \langle \cos^2 \psi \rangle$$

Polarization

In three dimensions

$$\langle \cos^2 \chi \rangle = \langle \cos^2 \psi \rangle$$



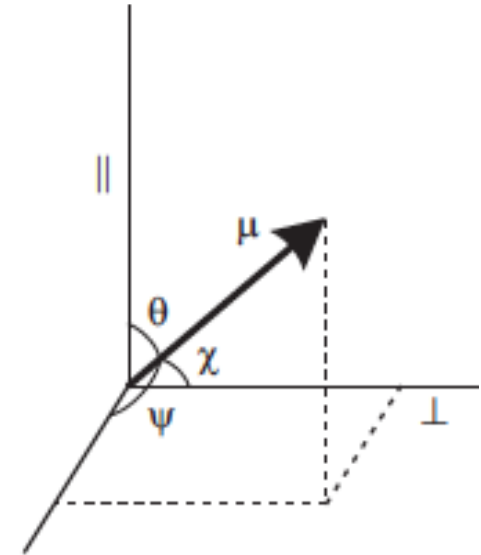
However in a macroscopic measurement one probes the average over all molecules

$$\langle \cos^2 \theta \rangle + \langle \cos^2 \chi \rangle + \langle \cos^2 \psi \rangle$$

Polarization

In three dimensions

$$\langle \cos^2 \chi \rangle = \langle \cos^2 \psi \rangle$$



The quantity independent of orientation is

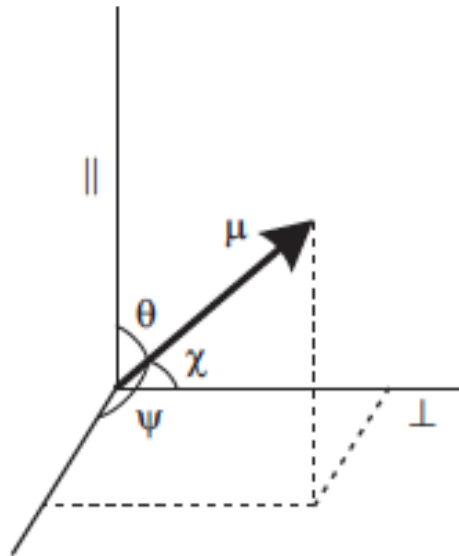
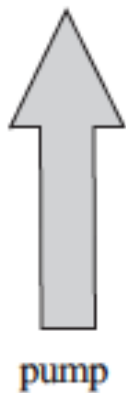
$$\Delta\alpha_{iso} = \frac{\Delta\alpha_{||} + 2\Delta\alpha_{\perp}}{3} = \langle \cos^2 \theta \rangle + 2\langle \cos^2 \chi \rangle$$

Using a distribution function

Distribution of excited molecules

$$N(\vartheta, \varphi, t) = g(\vartheta, \varphi, t) N_1$$

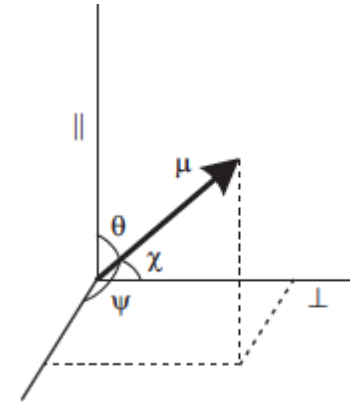
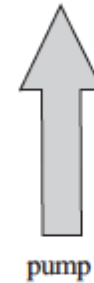
Total number of excited molecules



Properties

- Normalization

$$\int g(\theta, \phi, t) d\Omega = 1$$



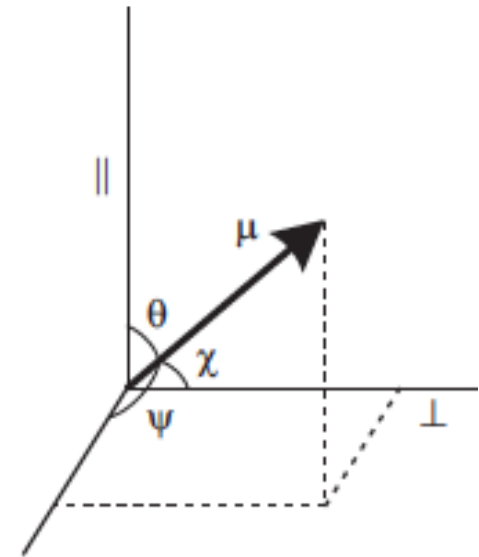
- At zero delay

$$g(\theta, \phi, 0) = \frac{3}{4\pi} \cos^2 \theta.$$

- Tends to an isotropic distribution for long delays

$$\lim_{t \rightarrow \infty} g(\theta, \phi, t) = \frac{1}{4\pi}$$

Signals

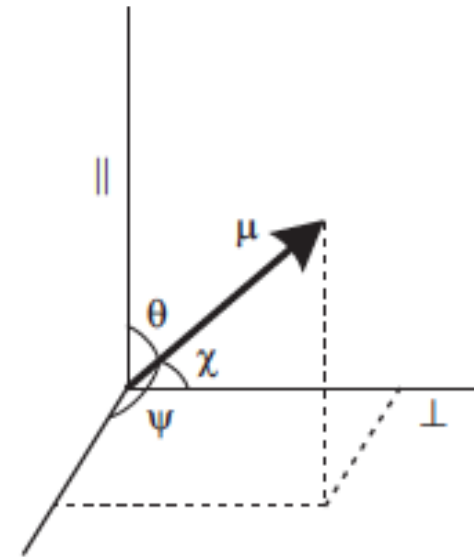


$$\Delta\alpha_{||}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \cos^2 \theta d\Omega,$$

$$\Delta\alpha_{\perp}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \sin^2 \theta \sin^2 \phi d\Omega,$$

Signals

$$\begin{aligned}\cos^2 \chi &= (\vec{\mu}(\theta, \phi) \cdot \hat{y})^2 \\ &= \sin^2 \theta \sin^2 \phi\end{aligned}$$

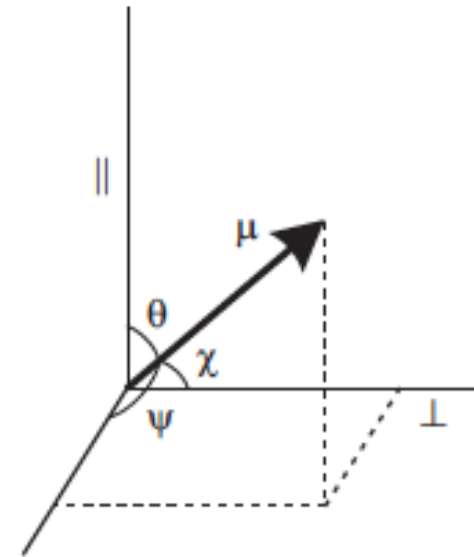


$$\Delta\alpha_{||}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \cos^2 \theta d\Omega,$$

$$\Delta\alpha_{\perp}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \sin^2 \theta \sin^2 \phi d\Omega,$$

Signals

Cross section is defined as isotropic average = 1/3 of maximum value



$$\Delta\alpha_{||}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \cos^2 \theta d\Omega,$$

$$\Delta\alpha_{\perp}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \sin^2 \theta \sin^2 \phi d\Omega,$$

Signals

$$\Delta\alpha_{||}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \cos^2 \theta d\Omega,$$

$$\Delta\alpha_{\perp}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \sin^2 \theta \sin^2 \phi d\Omega,$$

$$\Delta\alpha_{iso} = \frac{1}{3}(\Delta\alpha_{||} + 2\Delta\alpha_{\perp})$$

$$\Delta\alpha_{iso} = \sigma_{12}N_1 \int g(\theta, \varphi, t) [\cos^2 \theta + 2\sin^2 \theta \sin^2 \varphi] d\Omega$$

Signals

$$\Delta\alpha_{iso} = \sigma_{12}N_1 \int g(\theta, \varphi, t) [\cos^2 \theta + 2 \sin^2 \theta \sin^2 \varphi] d\Omega$$

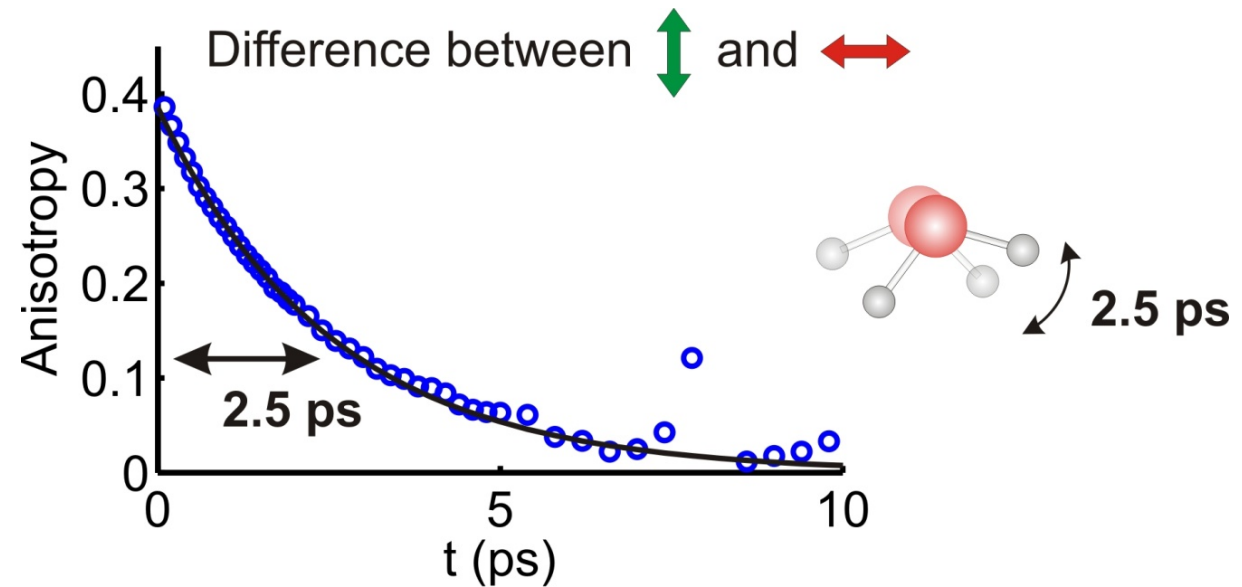
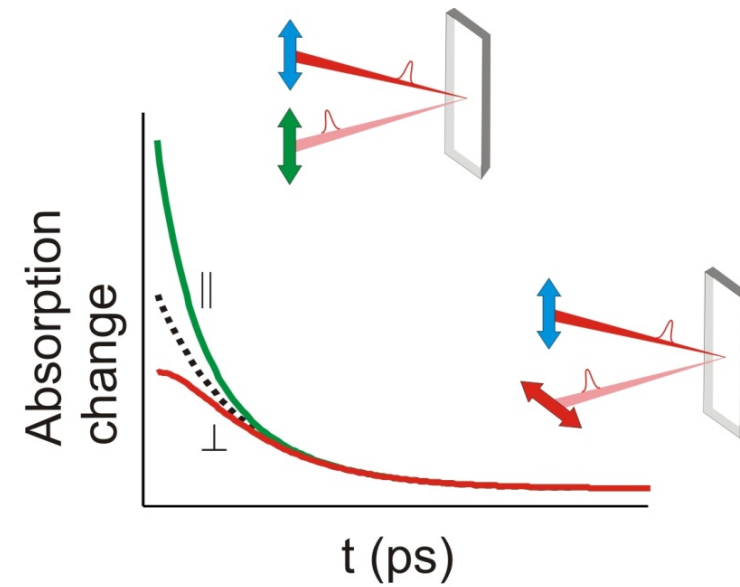
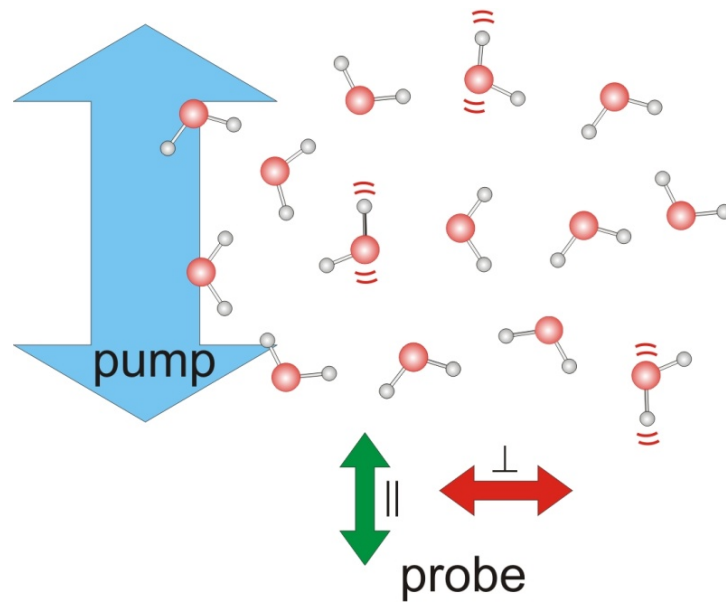
Isotropic sample

$$g(\vartheta, \varphi, t) = g(\vartheta, t)$$

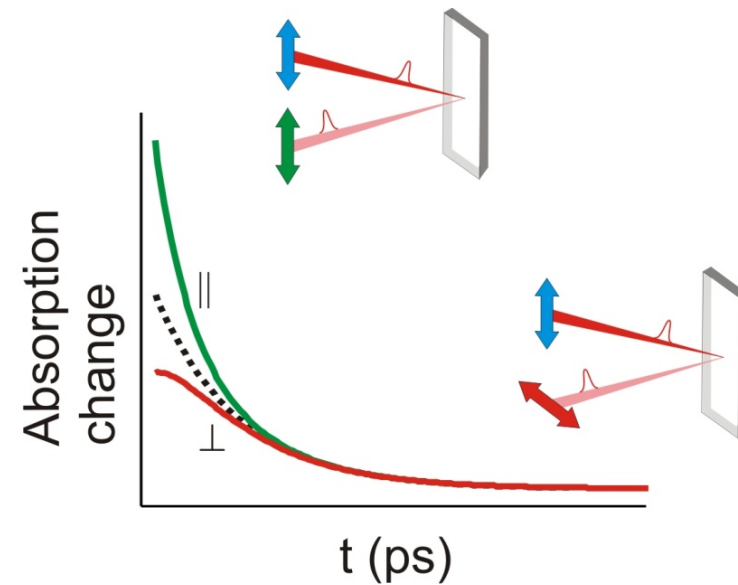
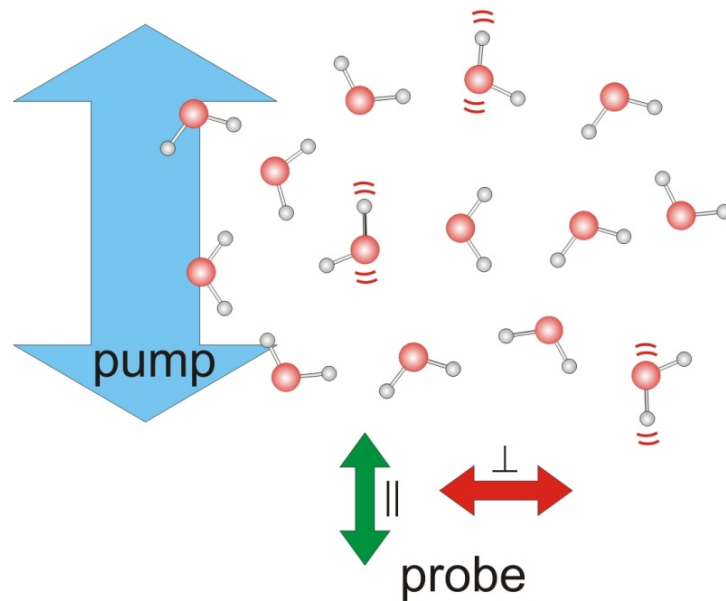
$$\Delta\alpha_{iso} = \sigma_{12}N_1$$

Indeed the isotropic signal depends only on the total number of excited molecules!

Anisotropy: molecular motion



Anisotropy: molecular motion



$$R(t) = \frac{\Delta\alpha_{||} - \Delta\alpha_{\perp}}{3\Delta\alpha_{iso}}$$

What microscopic quantity does the anisotropy represent?

Anisotropy

$$\Delta\alpha_{||}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \cos^2 \theta d\Omega,$$

$$\Delta\alpha_{\perp}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \sin^2 \theta \sin^2 \phi d\Omega,$$

$$R(t) = \frac{\Delta\alpha_{||} - \Delta\alpha_{\perp}}{3\Delta\alpha_{iso}} \quad \Delta\alpha_{iso} = \sigma_{12}N_1$$

$$R(t) = \int g(\theta, \varphi, t) [\cos^2 \theta - \sin^2 \theta \sin^2 \varphi] d\Omega$$

Anisotropy

$$\Delta\alpha_{||}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \cos^2 \theta d\Omega,$$

$$\Delta\alpha_{\perp}(t) = 3\sigma_{12}N_1 \int g(\theta, \phi, t) \sin^2 \theta \sin^2 \phi d\Omega,$$

Indeed:

The anisotropy reflects the time-dependent distribution of excited molecules!

$$R(t) = \int g(\theta, \varphi, t) [\cos^2 \theta - \sin^2 \theta \sin^2 \varphi] d\Omega$$

Anisotropy

- Expression is difficult to interpret
- Let's rewrite in terms of properties of the individual molecules

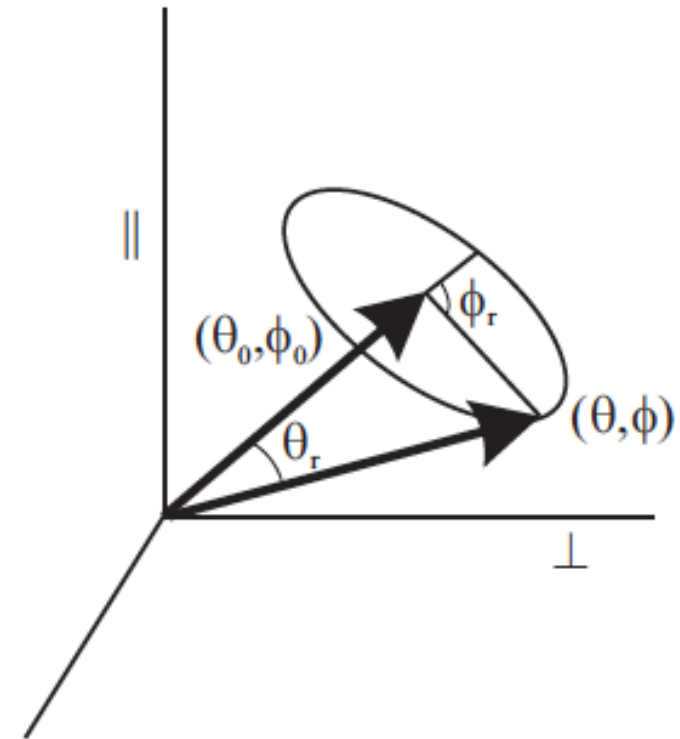
$$R(t) = \int g(\theta, \varphi, t) [\cos^2 \theta - \sin^2 \theta \sin^2 \varphi] d\Omega$$

Anisotropy

$$g(\theta, \varphi, t) = \int p(\theta, \varphi, t \mid \theta_0, \varphi_0, 0) g(\theta_0, \varphi_0, 0) d\Omega_0$$

$$p(\theta, \varphi, t \mid \theta_0, \varphi_0, 0) d\Omega =$$

- Probability that a molecule with orientation (θ_0, ϕ_0) at $t=0$ has diffused to (θ, ϕ) at $t=0$
- Green's function for the rotational diffusion equation



Anisotropy

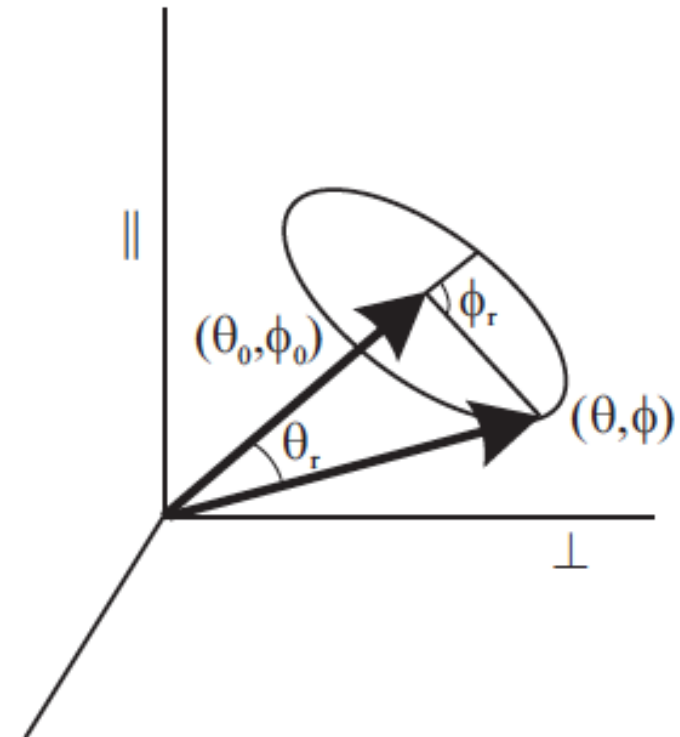
$$g(\theta, \varphi, t) = \int p(\theta, \varphi, t \mid \theta_0, \varphi_0, 0) g(\theta_0, \varphi_0, 0) d\Omega_0$$

$$g(\theta, \varphi, t) = \int p(\theta, \varphi, t \mid \theta_0, \varphi_0, 0) \frac{3}{4\pi} \cos^2 \theta_0 d\Omega_0$$

Anisotropy

$$R(t) = \int g(\theta, \varphi, t) [\cos^2 \theta - \sin^2 \theta \sin^2 \varphi] d\Omega$$

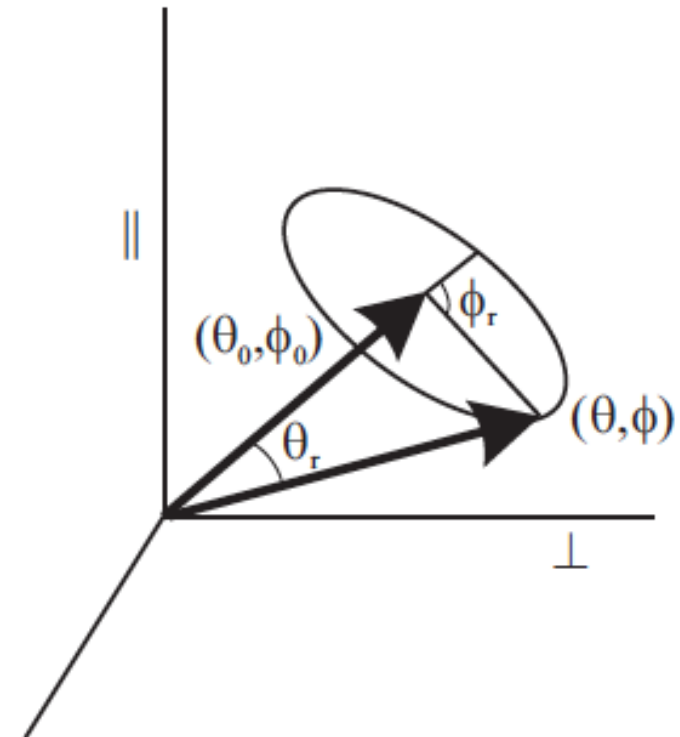
$$R(t) = \int \int p(\theta, \varphi, t \mid \theta_0, \varphi_0, 0) \frac{3 \cos^2 \theta_0}{4\pi} [\cos^2 \theta - \sin^2 \theta \sin^2 \varphi] d\Omega d\Omega_0$$



Anisotropy

$$R(t) = \iint p(\theta, \varphi, t \mid \theta_0, \varphi_0, 0) \frac{3 \cos^2 \theta_0}{4\pi} [\cos^2 \theta - \sin^2 \theta \sin^2 \varphi] d\Omega d\Omega_0$$

Change integration variables to (θ_0, ϕ_0) and (θ_r, ϕ_r)



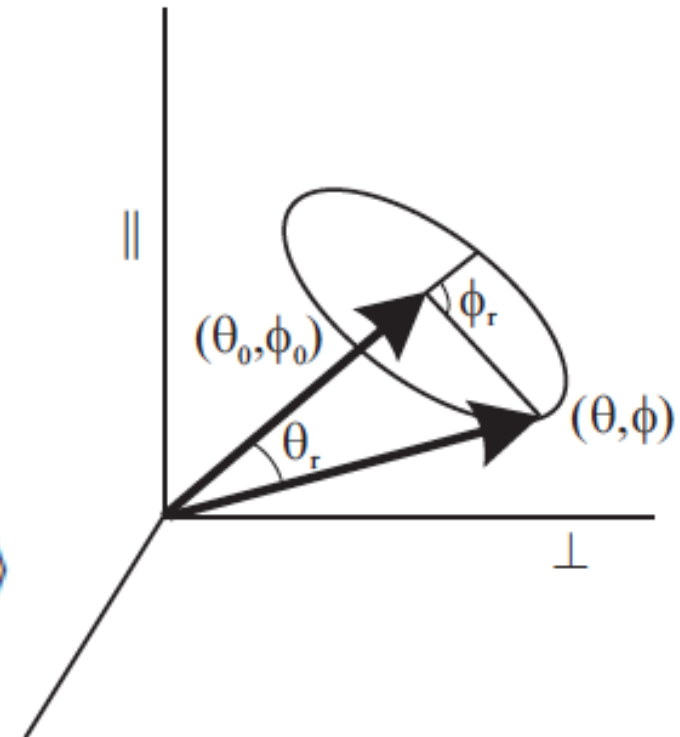
Anisotropy

$$R(t) = \int \int p(\theta, \varphi, t \mid \theta_0, \varphi_0, 0) \frac{3 \cos^2 \theta_0}{4\pi} [\cos^2 \theta - \sin^2 \theta \sin^2 \varphi] d\Omega d\Omega_0$$

- Change integration variables to (θ_0, ϕ_0) and (θ_r, ϕ_r)
- Do a lot of algebra

- Finally this gives

$$\begin{aligned} R(t) &= \frac{2}{5} \langle P_2(\cos \theta_r) \rangle, \\ &= \frac{2}{5} \langle P_2(\vec{\mu}(0) \cdot \vec{\mu}(t)) \rangle, \\ &= \frac{2}{5} \langle (3 \cos^2 \theta_r - 1)/2 \rangle \end{aligned}$$



Anisotropy

$$\begin{aligned} R(t) &= \frac{2}{5} \langle P_2(\cos \theta_r) \rangle, \\ &= \frac{2}{5} \langle P_2(\vec{\mu}(0) \cdot \vec{\mu}(t)) \rangle, \\ &= \frac{2}{5} \langle (3 \cos^2 \theta_r - 1)/2 \rangle \end{aligned}$$

Jump/diffusion angle θ_r

The anisotropy is the average over all molecules of the following function of θ_r

$$\frac{2}{5} \cdot \frac{3 \cos^2 \theta_r - 1}{2}$$

Simple applications

- Isotropic diffusion (check)
- Delocalization in a plane
- Energy transfer over an angle θ_t

$$R(t) = \frac{2}{5} \left\langle \frac{3 \cos^2 \theta_r(t) - 1}{2} \right\rangle$$

Summary ‘Polarization properties’

- Moving from the lab frame to a molecular frame

- Isotropic signal

$$\Delta\alpha_{iso} = \frac{1}{3}(\Delta\alpha_{\parallel} + 2\Delta\alpha_{\perp})$$

- Anisotropy

$$R(t) = \frac{2}{5} \left\langle \frac{3 \cos^2 \theta_r(t) - 1}{2} \right\rangle$$