

Charge transfer through DNA

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1

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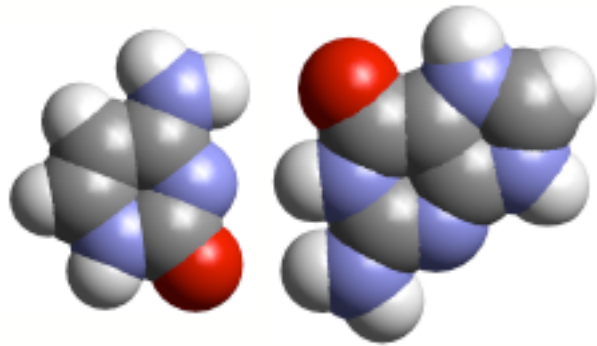
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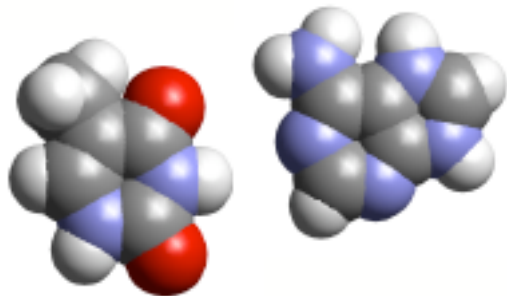
Funding

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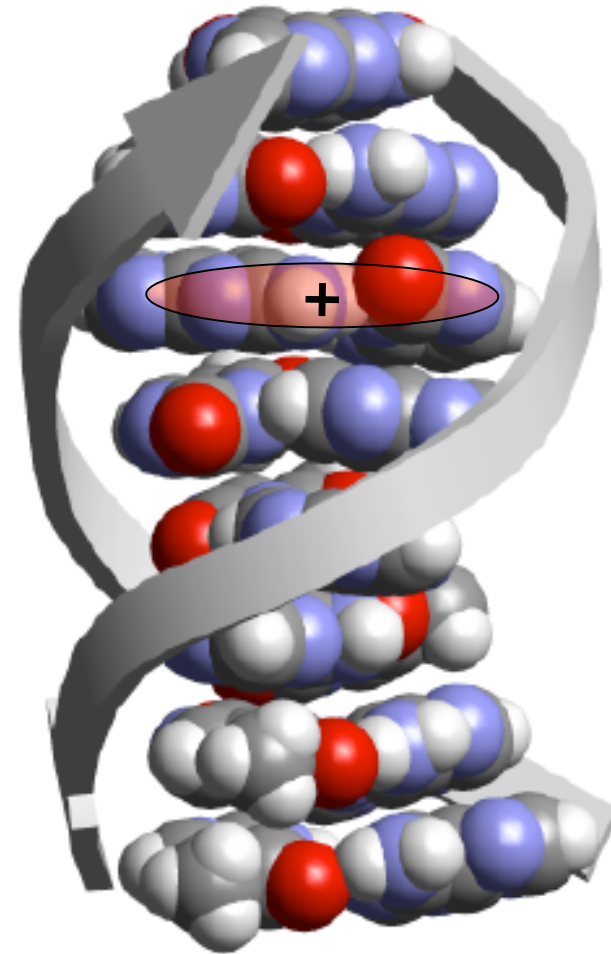
Base pair stacking in DNA



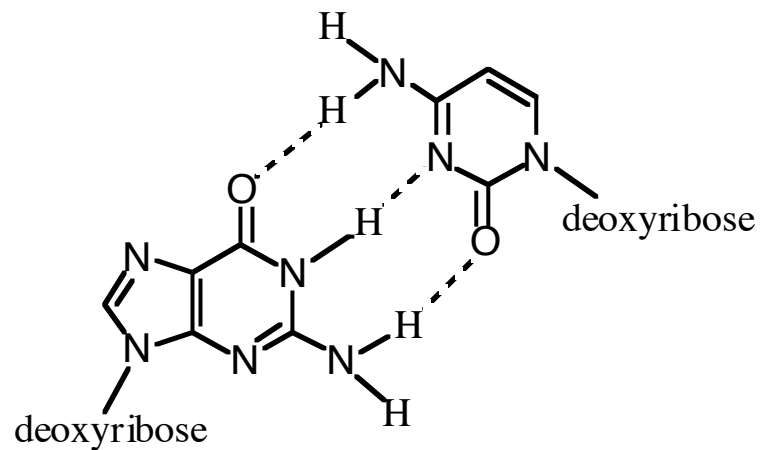
C:G



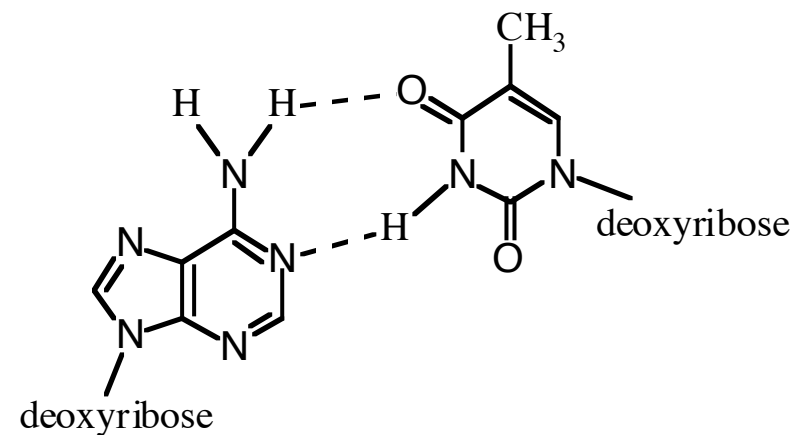
T:A



G:C and A:T base pairing



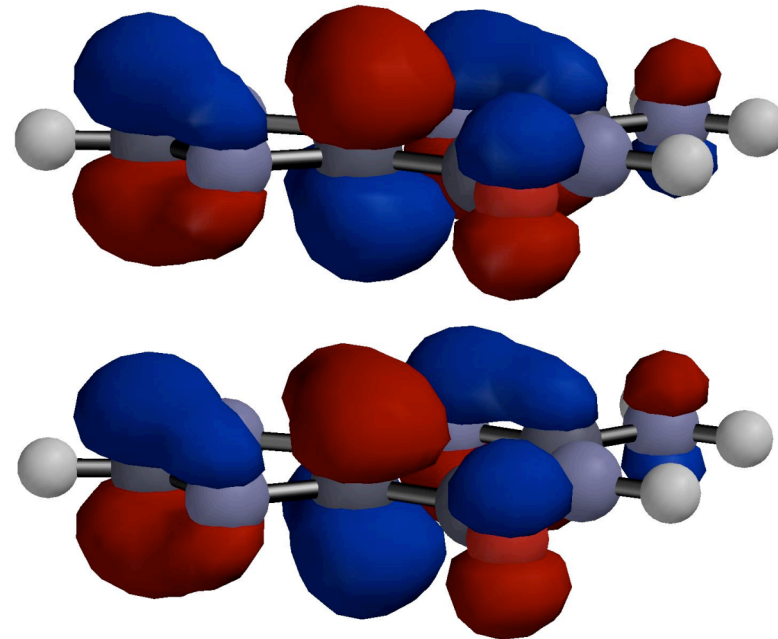
G:C



A:T

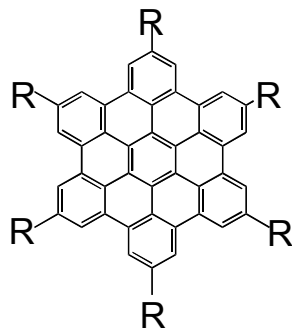
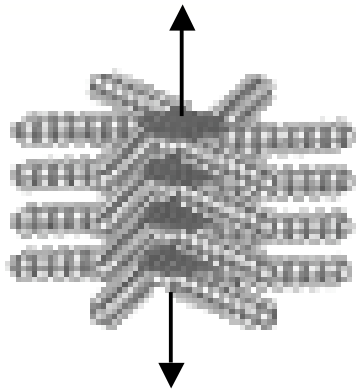
π -orbitals on adjacent bases interact and can provide pathway for charge transport

two stacked guanines

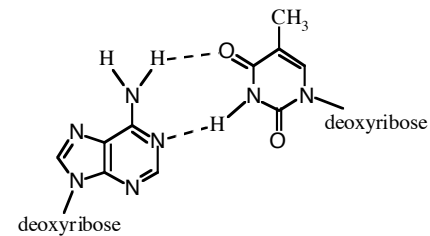
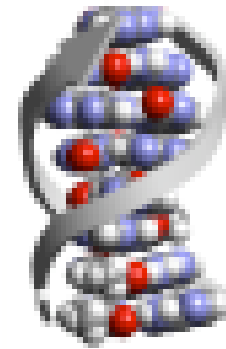


DNA analogous to discotic liquid crystalline materials

discotic liquid crystals
mobility 0.01 - 1 cm²/Vs



DNA ?



Charge migration in DNA

Electrons and holes can be created in DNA by:

- radiation (UV, high-energy radiation)
- chemical reactions
- injection from electrodes

Insight into charge migration along DNA is important for:

1. Understanding biological damage due to charges

- radiation induced mutations
- oxidative reactions

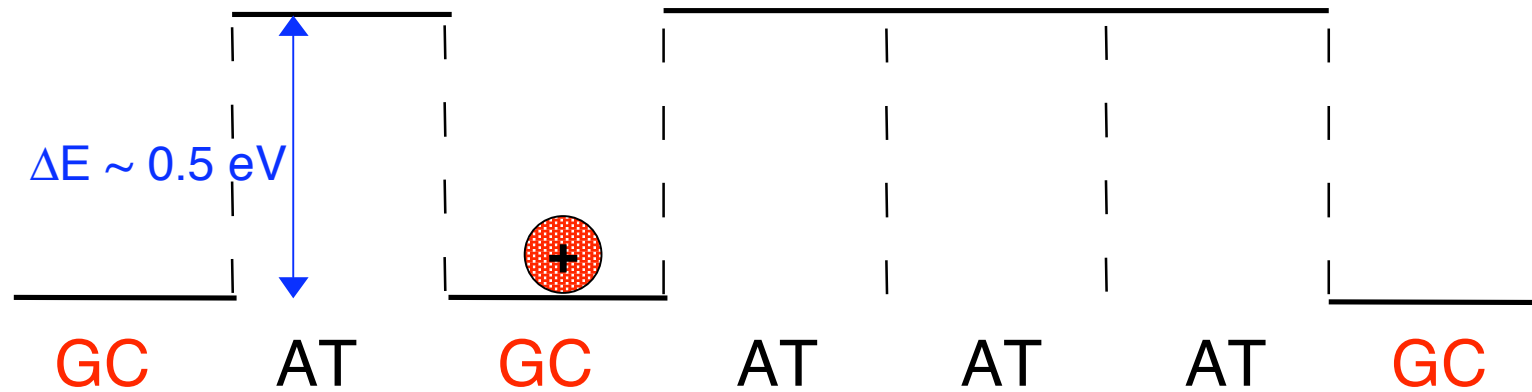
2. Application in nanoscale molecular electronics

- DNA used as a molecular wire
- DNA used as a scaffold for conducting wire

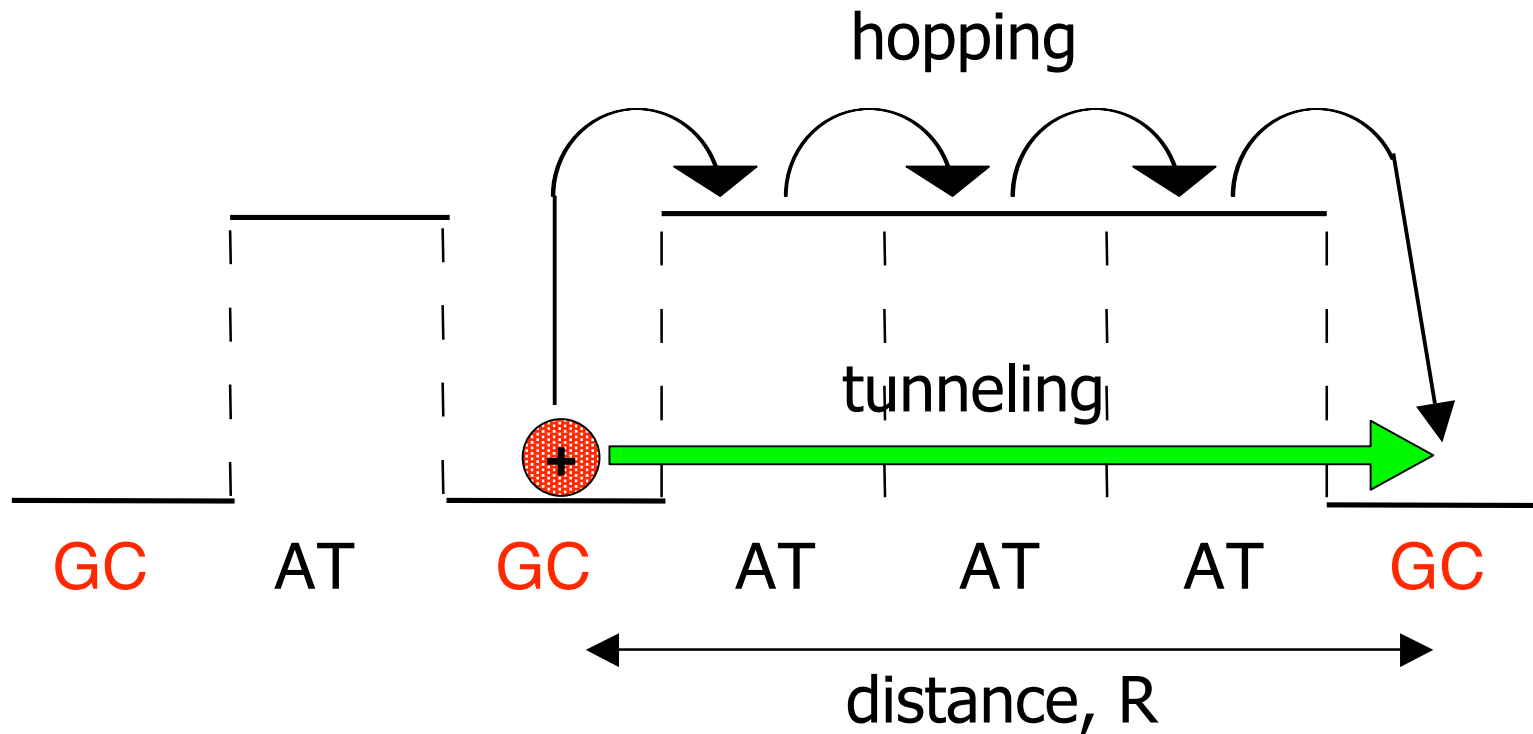
Present work

1. Charge transfer in Donor-DNA-Acceptor systems
2. Mobility of charges on DNA
3. Selective photo-oxidation of specific guanines

Positive charges reside on guanine



Mechanism of charge migration between G's ?



Guanine-DNA-Guanine

Charge transfer rate often decays exponentially with distance:

$$k \propto e^{-\beta R}$$

R : Distance between donor and acceptor

β : Fall of rate characterizes distance dependence

Aim of theoretical studies

- Explain **high** ($\sim 1.0 \text{ \AA}^{-1}$) and **low** ($\sim 0.1 \text{ \AA}^{-1}$) experimental values of β
- Provide insight into factors governing **absolute values** of charge transfer rates

Quantum mechanical model

- Wavefunction of the charge is superposition of HOMO's on nucleobases

$$\psi(t) = \sum c_k(t) \Phi_k$$

- Hamiltonian contains site-energies and electronic couplings from DFT (ADF) calculations

E_{ij} : on-site energy

J_{ij} : electronic coupling

Γ : decay parameter at acceptor site

$$\hat{H}_{el} = \begin{pmatrix} E_{11} & J_{12} & 0 & 0 \\ J_{21} & E_{22} & J_{23} & 0 \\ 0 & J_{32} & E_{33} & J_{34} \\ 0 & 0 & J_{43} & E_{44} - i\Gamma \end{pmatrix}$$

- Electronic couplings vary in time due to motion of base pairs (described classically)

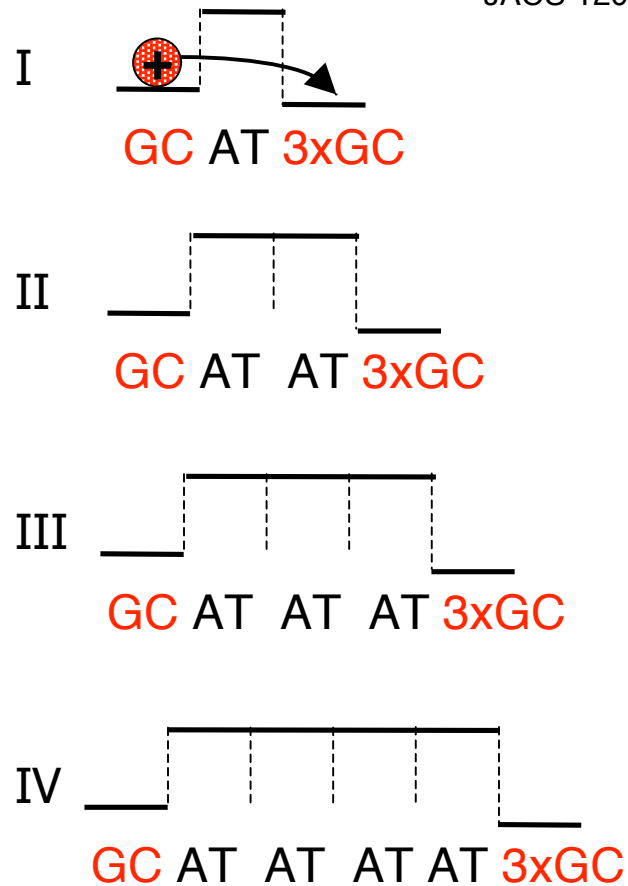
Charge is initially localized on donor site and delocalizes when wavefunction is propagated in time

$$i\hbar \frac{\partial \psi(t)}{\partial t} = \hat{H} \psi(t)$$

Distance dependence

Experimental studies by Meggers et al.

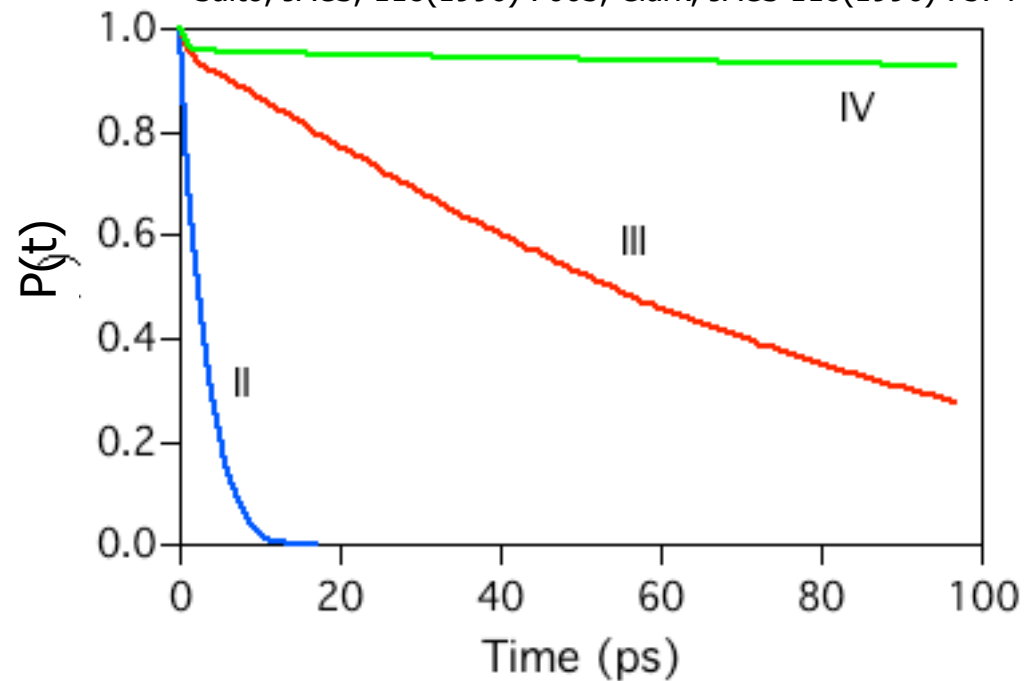
JACS 120 (1998) 12950



Theoretical results

$$J = 0.11 \text{ eV}, E_{AT} - E_{GC} = 0.55 \text{ eV}$$

Saito, JACS, 118(1996) 7063, Clark, JACS 118(1996) 7574



Decay of charge: $P(t) = e^{-k(R)t}$

In case $k(R) = k_0 e^{-\beta R}$

One gets linear behavior for

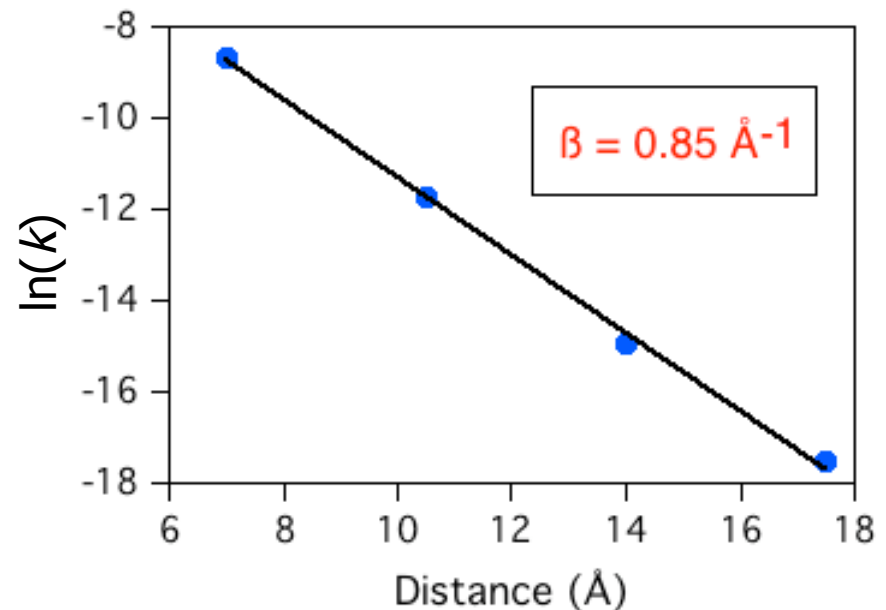
$$\ln[k(R)] = -\beta R + \ln[k_0]$$

Distance dependence

Charge migration rate through sequences I-IV shows **exponential dependence** on distance

Theoretical β value (0.85 \AA^{-1}) is close to experimental value (0.7 \AA^{-1}) of Meggers et al.

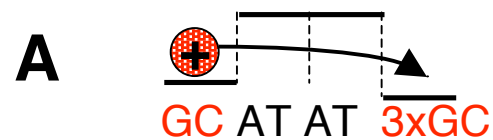
Charge tunnels through classically forbidden region of AT base pairs



Sequence dependence

Sequences of AT's interrupted with GC base pairs

Experiments by Giese et al. *Angew. Chem. Int. Ed.*, 38(1999) 996



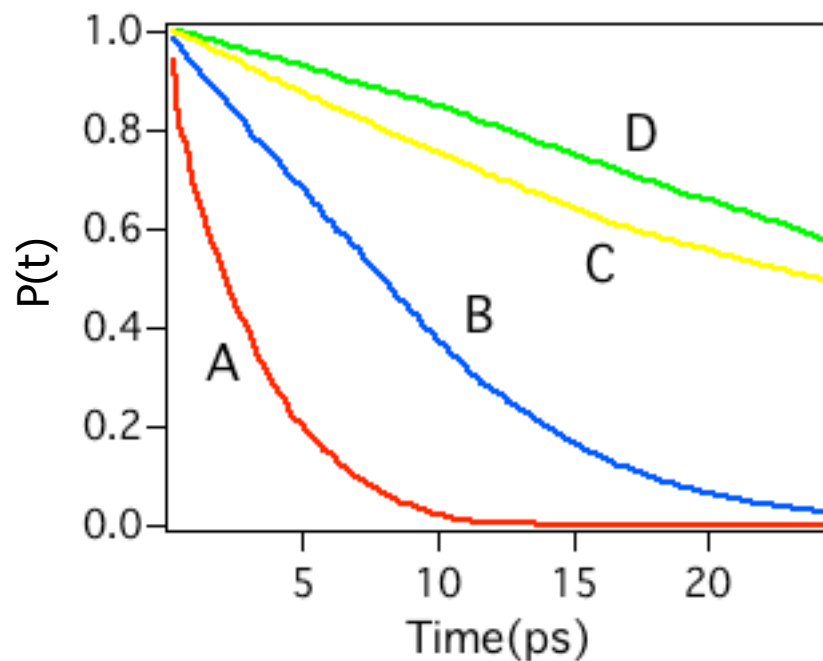
**Small distance dependence
observed: $\beta = 0.07 \text{ \AA}^{-1}$**



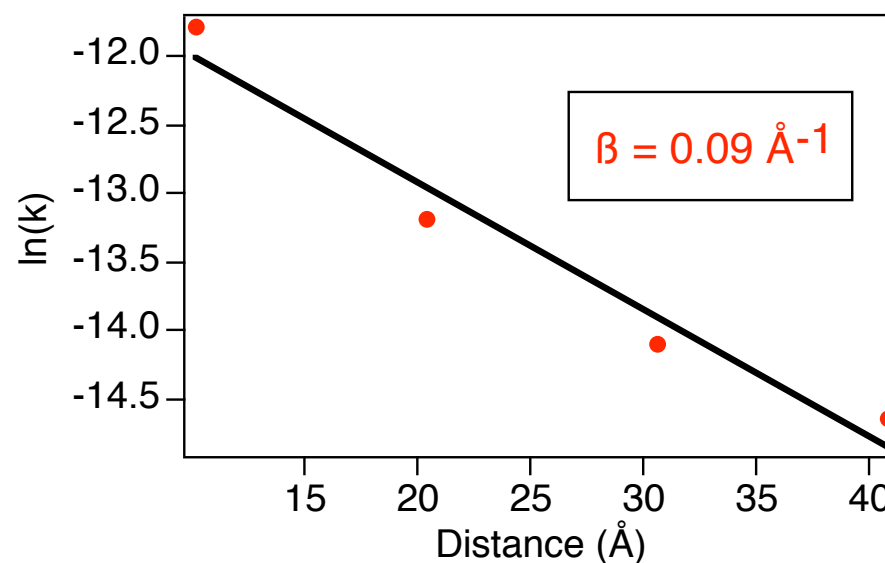
Hopping between GC
base pairs ???



Sequence dependence - Theoretical results



Weak distance dependence



Theoretical β value (0.09 \AA^{-1}) agrees with experimental value (0.07 \AA^{-1}) of Giese et al.

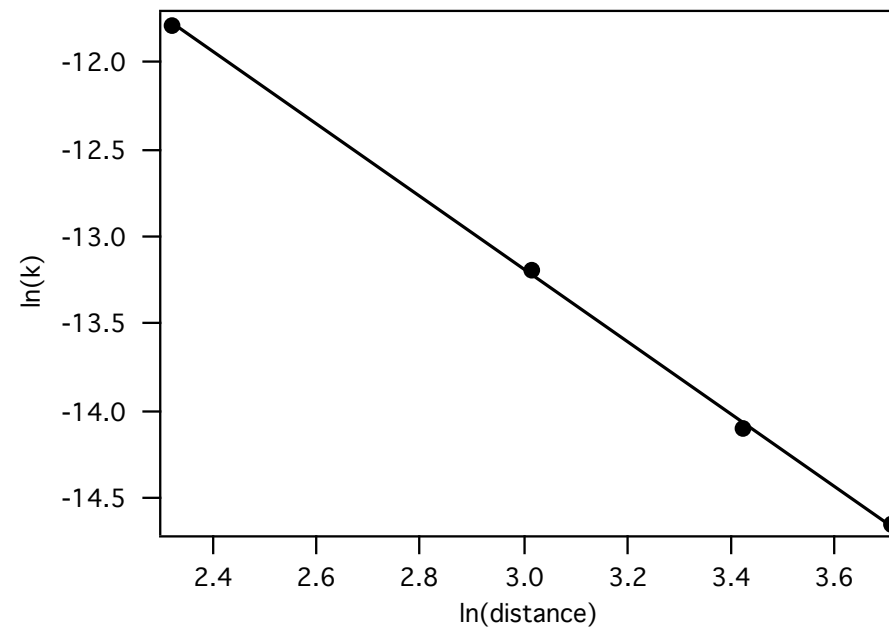
Transfer rate - Multi-step hopping

Charge transfer rate according to multi-step hopping:

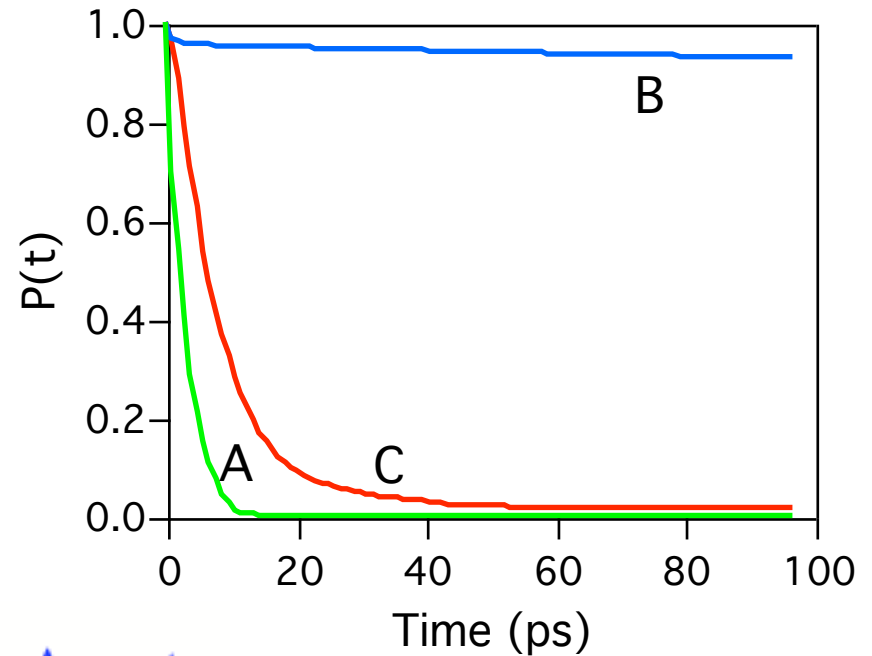
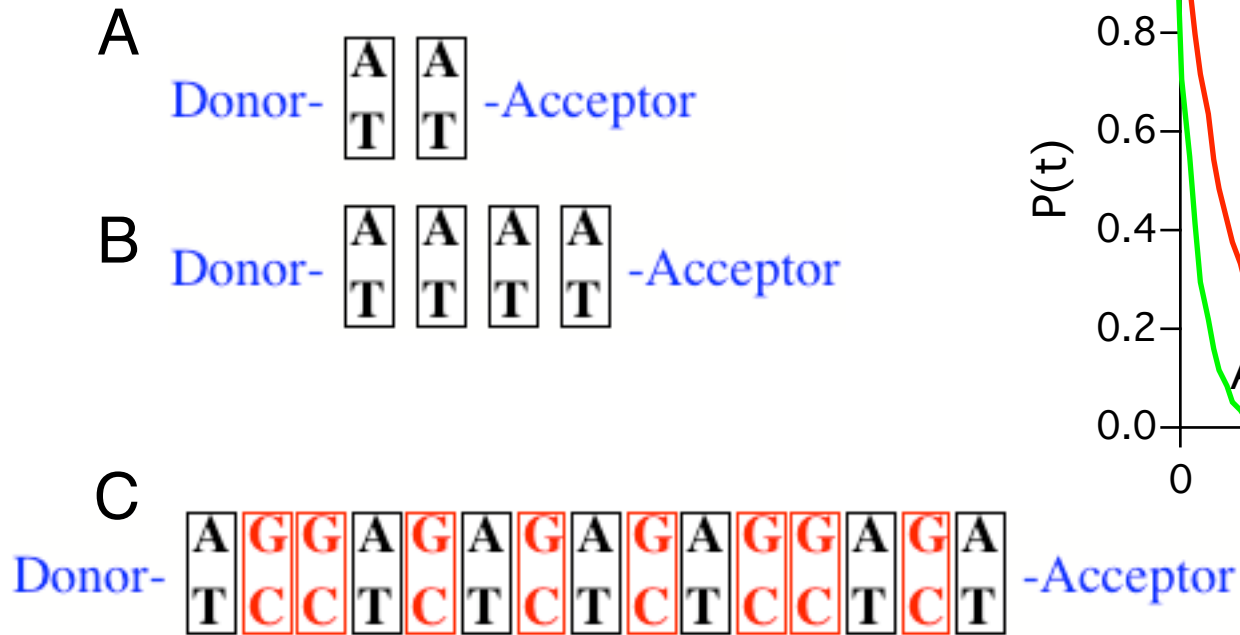
$$k_{ct} \sim R^\eta$$

$$\Rightarrow \ln k_{ct} \propto -\eta \ln R$$

The fit gives $\eta = 2.09$



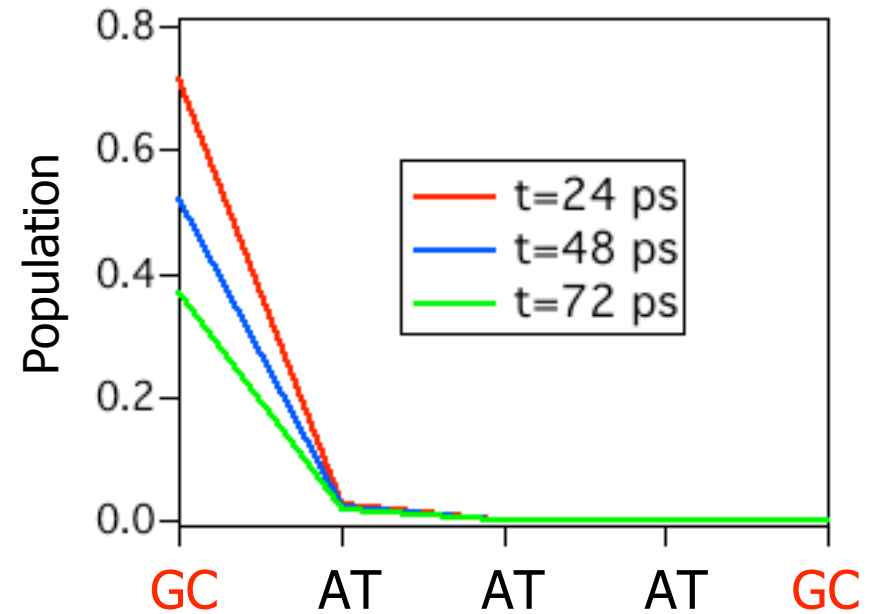
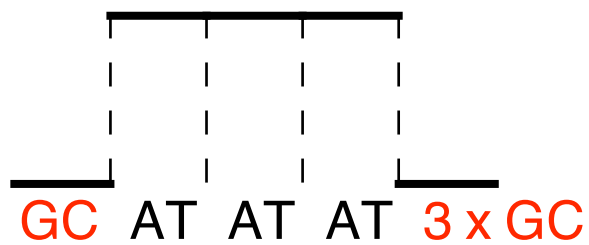
Sequence dependence



Charge migration over 54 Å in sequence C is nearly as efficient as over 10 Å in sequence A (agrees with expts. of Meggers)

Population analysis

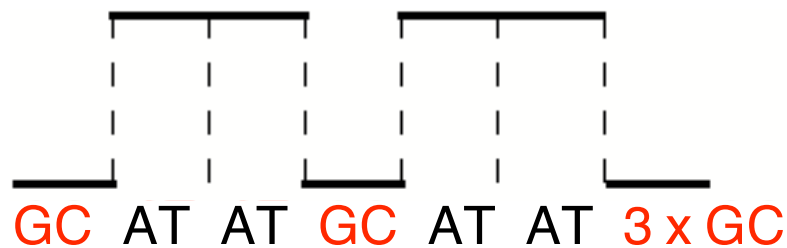
Charge distribution at three different times



Population on AT bridge is negligible at all times

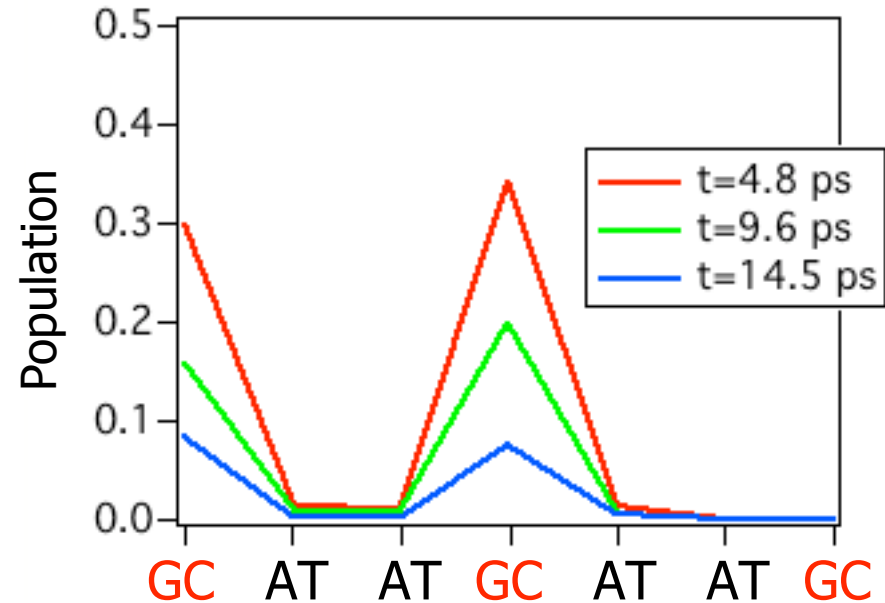
Population analysis

AT sequence interrupted by GC



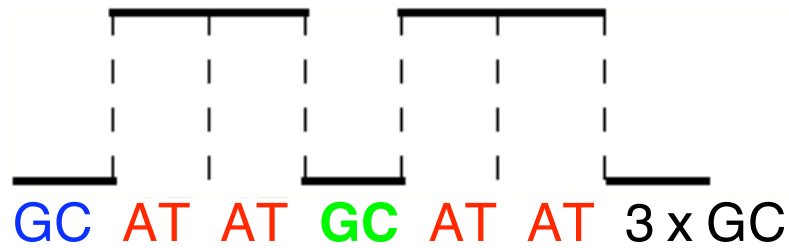
Population on AT is negligible

Population at three different times



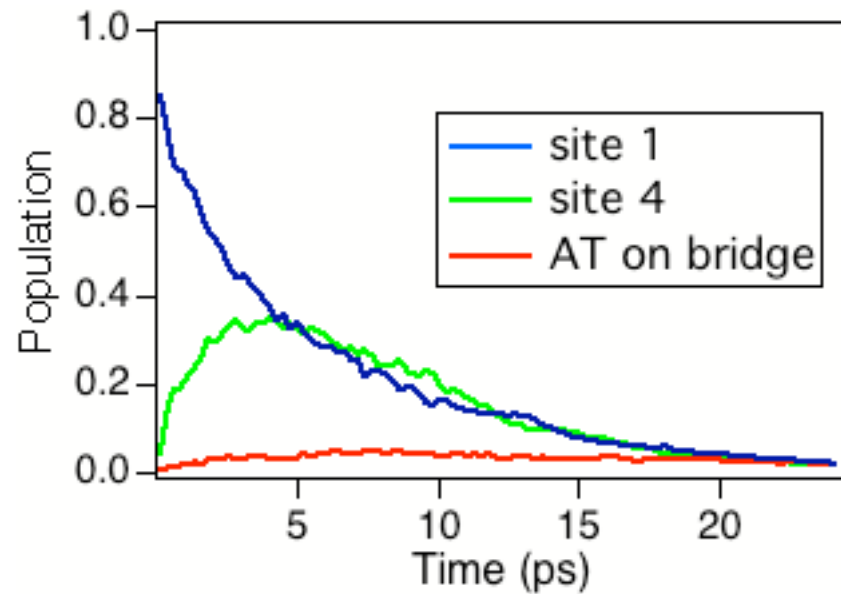
Charge tunnels through AT bridge to next GC

Population analysis

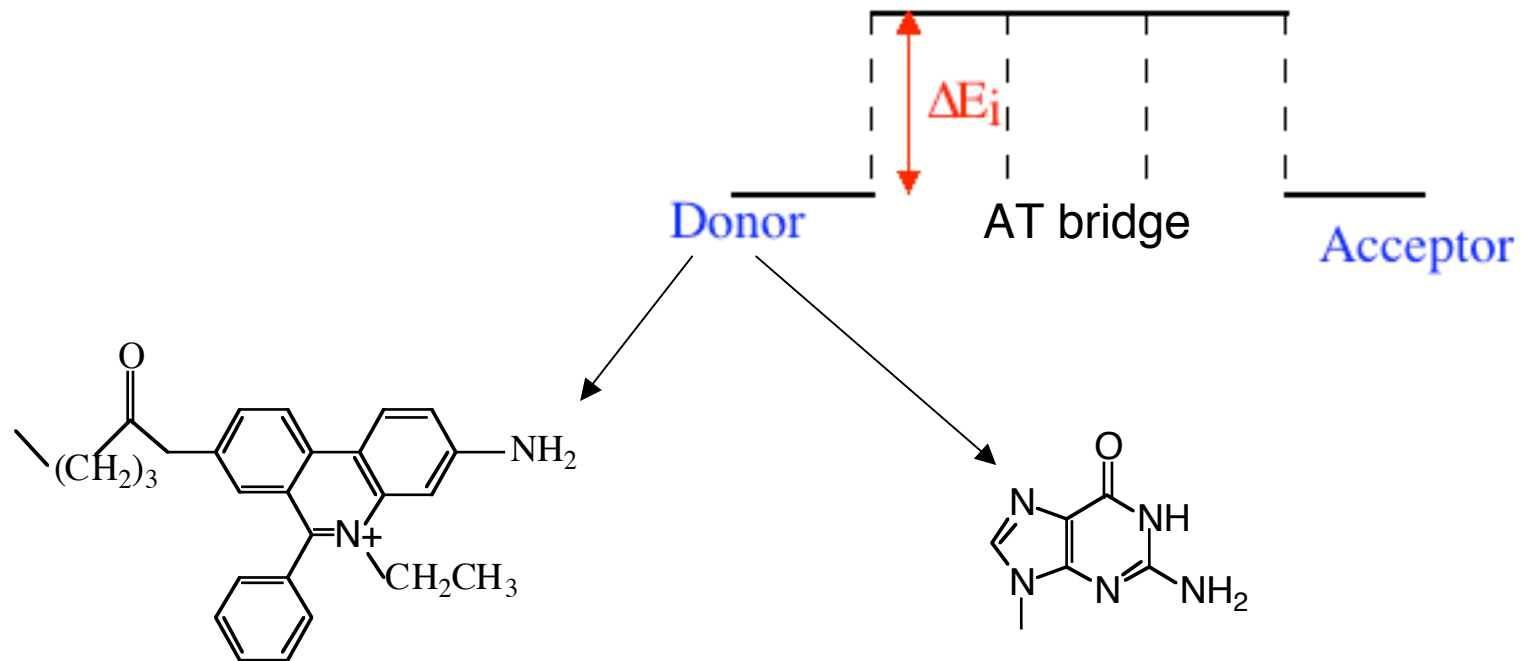


Charge effectively hops between GC base pairs

Population at GC sites as a function of time



Distance dependence depends on donor

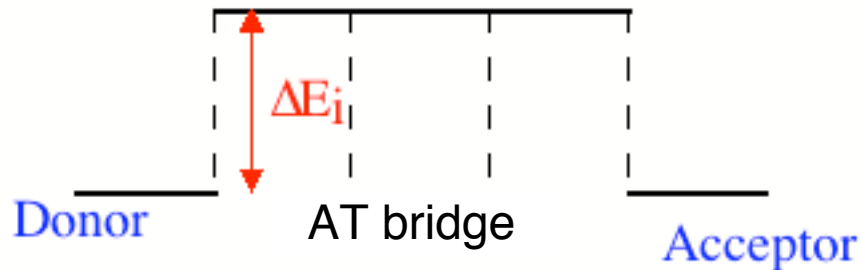


Donor used by Barton et al. is
photoexcited ethidium: $\beta \sim 0.2 \text{ \AA}^{-1}$

Donor used by Meggers et al.
is guanine cation: $\beta \sim 0.7 \text{ \AA}^{-1}$

Effect of injection barrier

Ionization potential of donor determines injection barrier ΔE_i



Strong dependence of β on ΔE_i

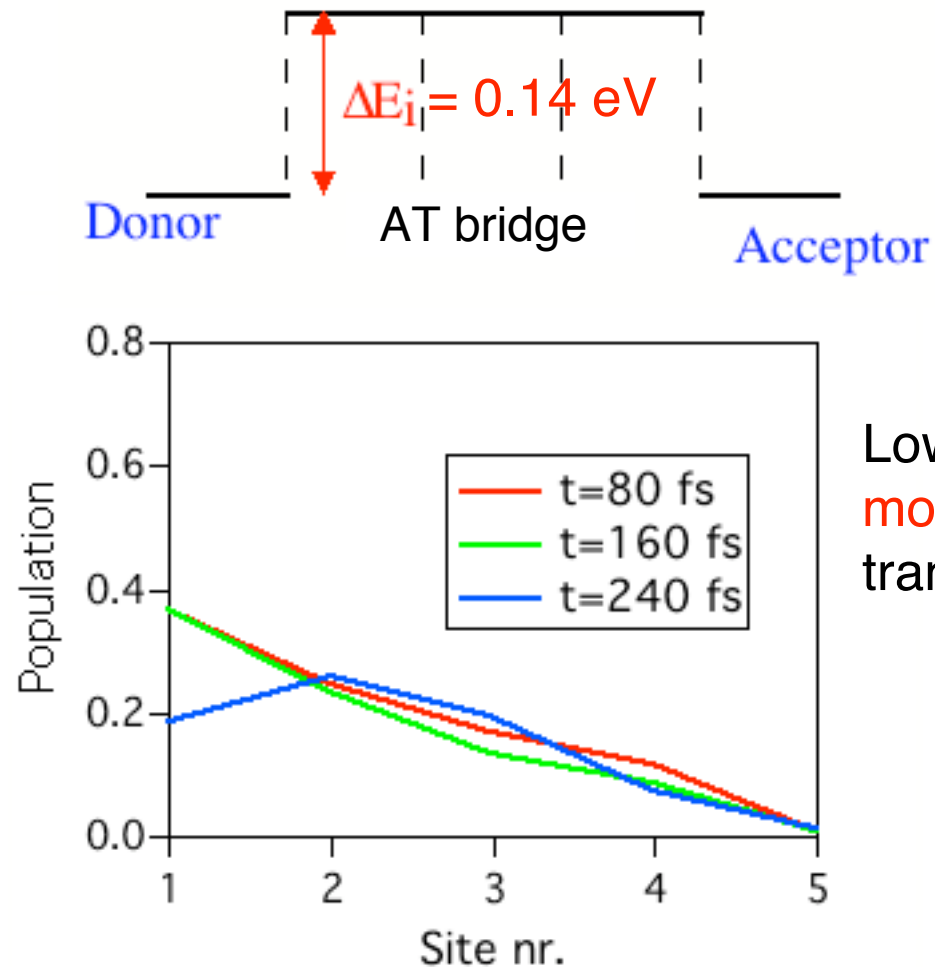
Distance dependence is very small for vanishing ΔE_i

- transition to **molecular wire** behaviour
- may explain results of Barton group

Chem. Biol. 5 (1998) 413

| ΔE_i eV | β \AA^{-1} |
|--------------------|------------------------------|
| 0 | 0.09 |
| 0.14 | 0.13 |
| 0.27 | 0.34 |
| 0.41 | 0.53 |
| 0.55 | 0.85 |
| 0.70 | ≈ 1 |

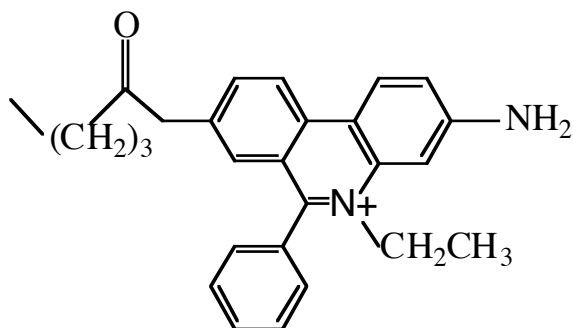
Charge distribution at three different times



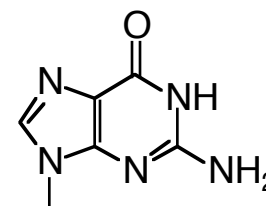
Low injection barrier leads to **molecular wire** type charge transport

Effect of donor energy

Distance dependence determined by donor energy



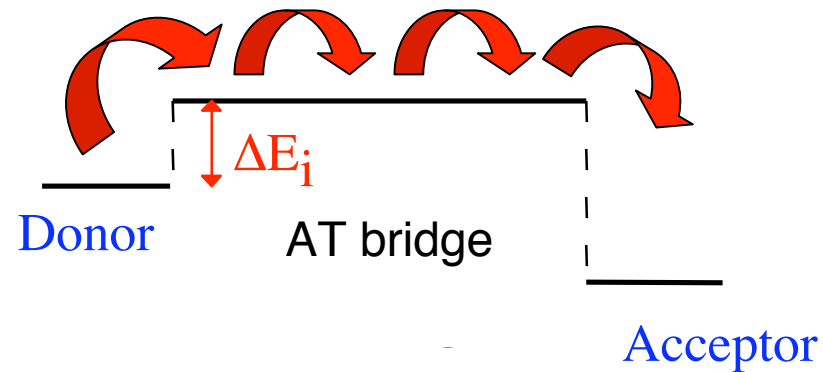
Donor used by Barton et al. is photoexcited ethidium: $\beta \sim 0.2 \text{ \AA}^{-1}$



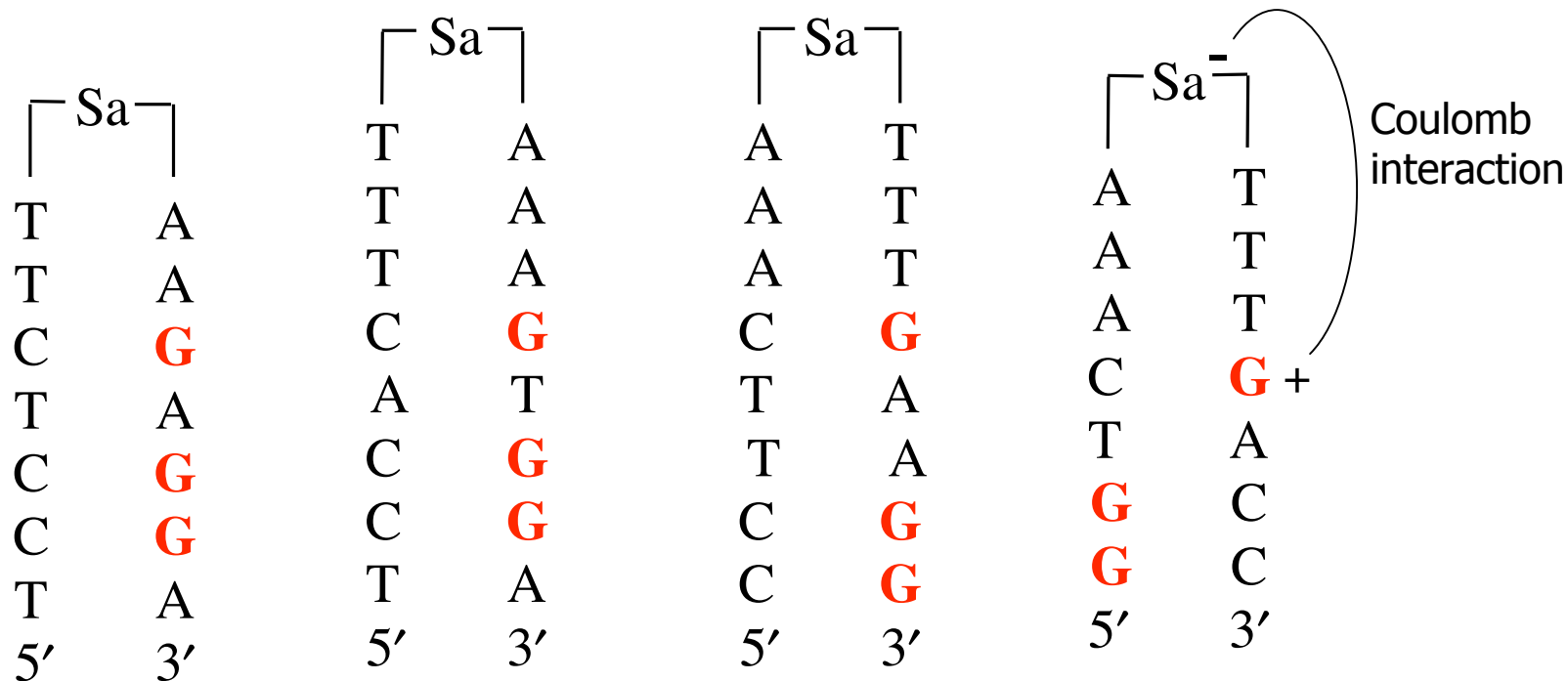
Donor used by Meggers et al. is guanine cation: $\beta \sim 0.7 \text{ \AA}^{-1}$

Molecular wire behaviour

Low β due to small injection energy from donor to bridge



Absolute rates of charge transport from **G** to **GG** sites in DNA hairpins



2b

Exptl. rate: 6.0
Exptl. time: 17 ns

3b

0.33
300 ns

4c

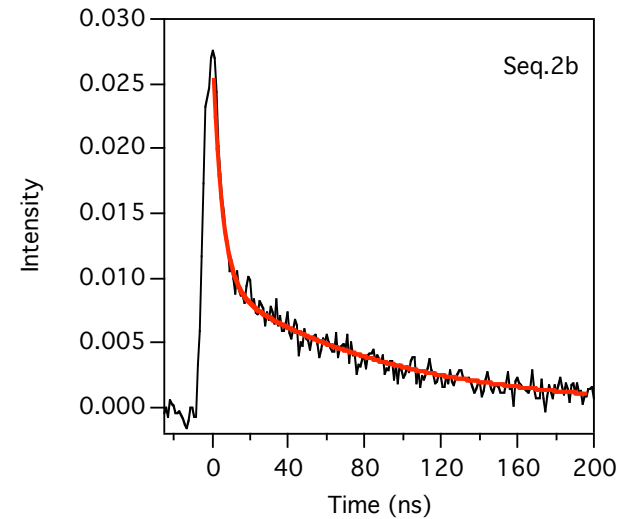
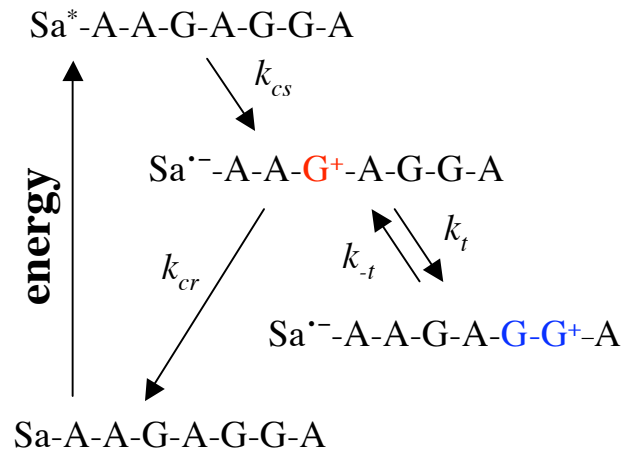
0.05
2000 ns

5b

0.09 (10⁷s⁻¹)
1100 ns

Kinetic analysis of transient absorption spectra

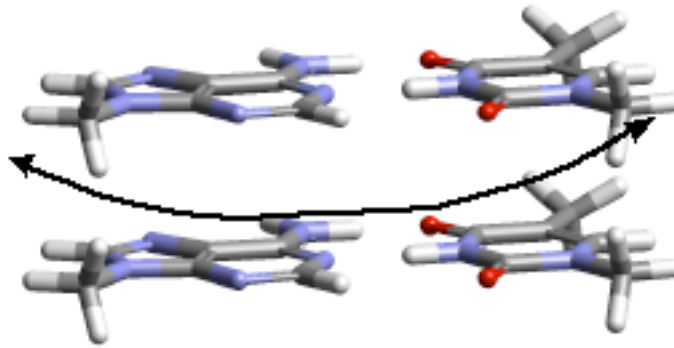
Kinetic scheme



$$\frac{dX}{dt} = -k_t X - k_{cr} X + k_{-t} Y$$

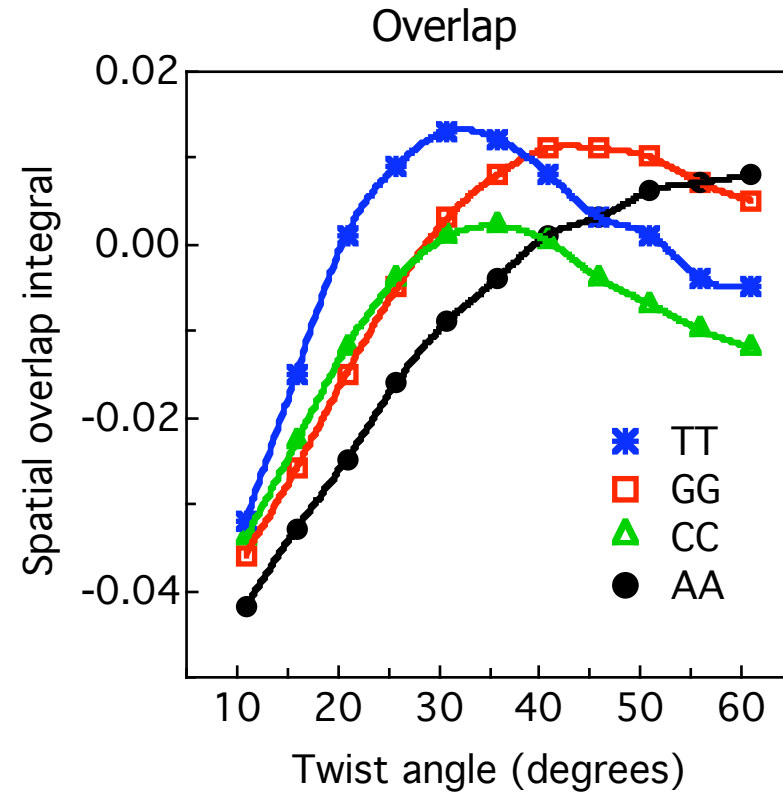
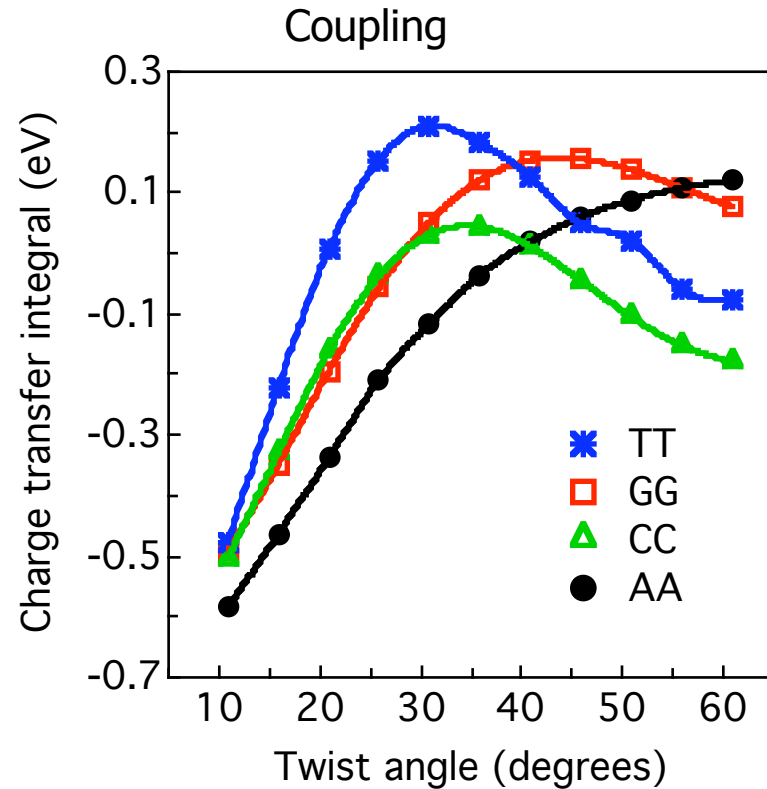
$$\frac{dY}{dt} = k_t X - k_{-t} Y$$

Theoretical model of charge transport via twisting base pairs

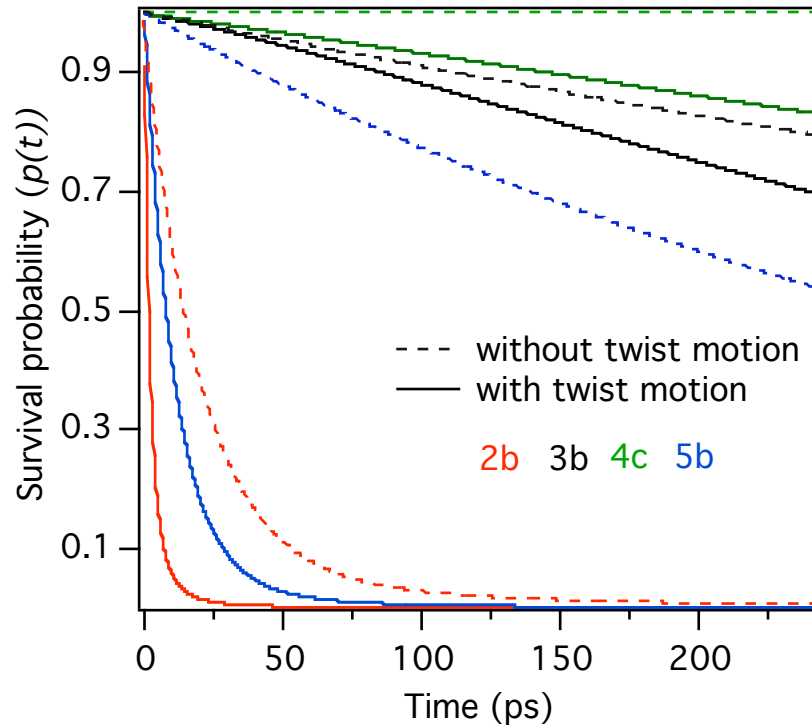


Twisting motion F_{rot}

Effect of twisting on electronic coupling



Twisting enhances charge transfer rate



No Coulomb interaction between Sa^- and hole on DNA in calculations

Calculated decay time for **3b > 5b!**

Disagreement with expt.

3b: 300 ns

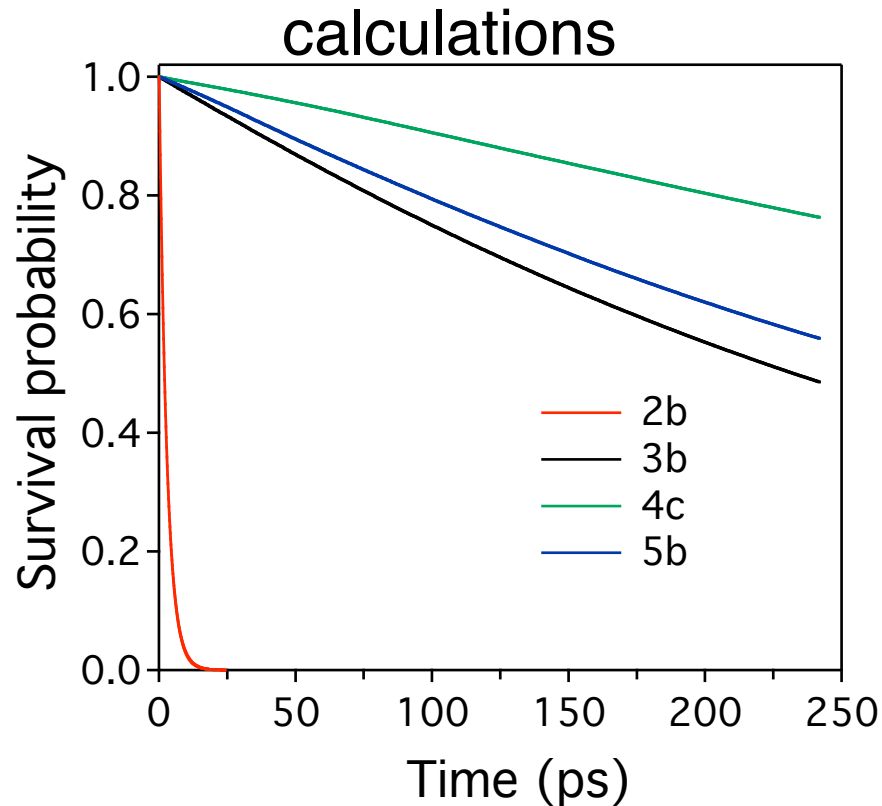
5b: 1100 ns

5'-AGT**GA**-
-TCACCT-

5'-T**G**ACC-
-ACT**GG**-

Relative rates reproduced by inclusion of Coulomb interaction in tight-binding calculations.

Absolute rates much too fast (~ factor 1000) !

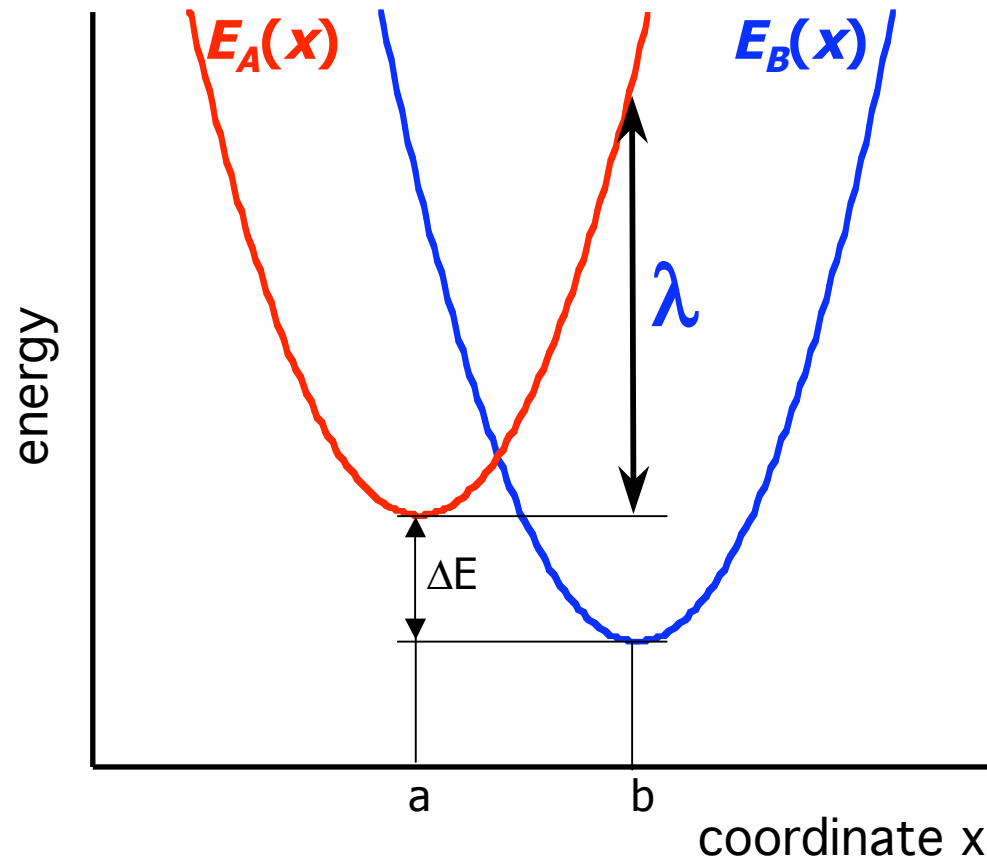


experiments

| | | |
|-----------|-------------------------|--------------|
| 2b | 5'-AGAGGA- -TCTCCT- | 17 ns |
| 3b | 5'-AGTGG A- -TCACCT- | 300 ns |
| 4c | 5'-TGAAGG- -ACTTCC- | 2000 ns |
| 5b | 5'-TGACC- -ACTGG- | 1100 ns |

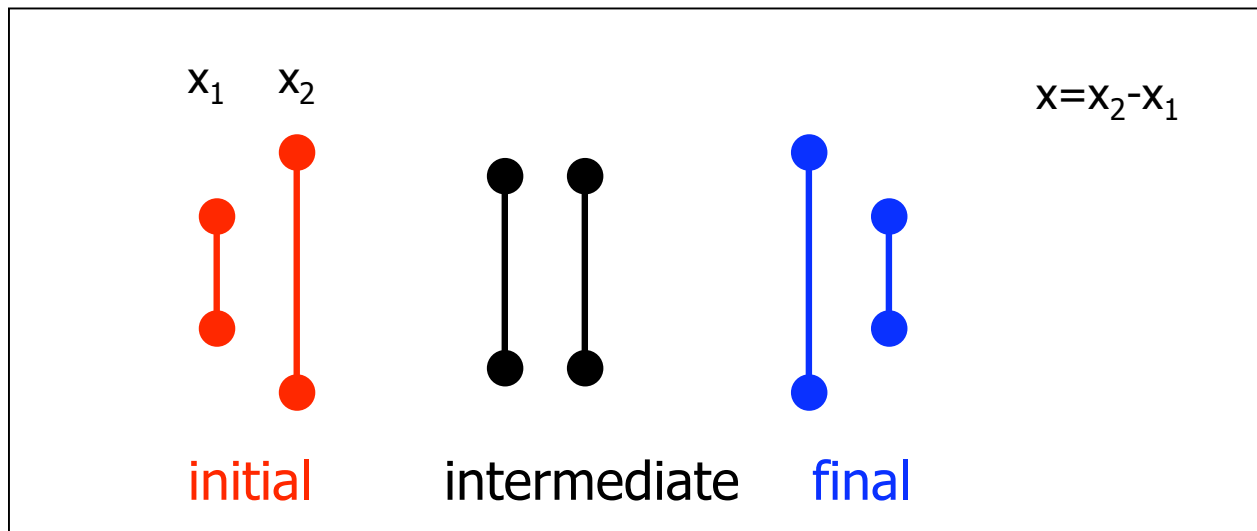
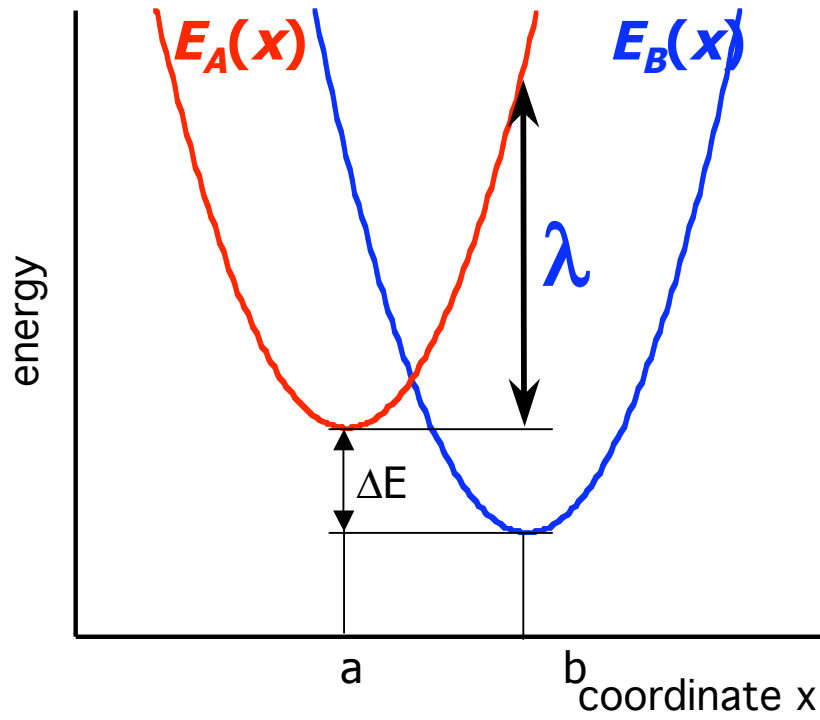
Charge induces lattice distortion of nucleobase and polarizes surrounding water: reorganization energy to be included

Marcus or Holstein theory for charge transfer rate



Initial and **final** state energies

Initial and final states



Classical Marcus rate

- classical treatment of vibration $k_B T \gg \hbar \omega$
- start from Fermi Golden Rule

$$k(x) = \frac{2\pi}{\hbar} V^2 \delta(E_B(x) - E_A(x))$$

$$E_A(x) = \bar{E}_A + \frac{1}{2} C x^2 \quad E_B(x) = \bar{E}_B + \frac{1}{2} C (x - b)^2$$

$$E_B(x) - E_A(x) = \bar{E}_B - \bar{E}_A + \frac{1}{2} C b^2 - C b x \quad \Delta E = \bar{E}_B - \bar{E}_A$$

$$k_{CT} \equiv \langle k \rangle = \int k(x) f(x) dx$$

$$f(x) = \sqrt{\frac{C}{2\pi k_B T}} e^{-E_A(x)/k_B T}$$

Boltzmann distribution of distances x

Classical Marcus rate

- classical treatment of vibration
- start from Fermi Golden Rule

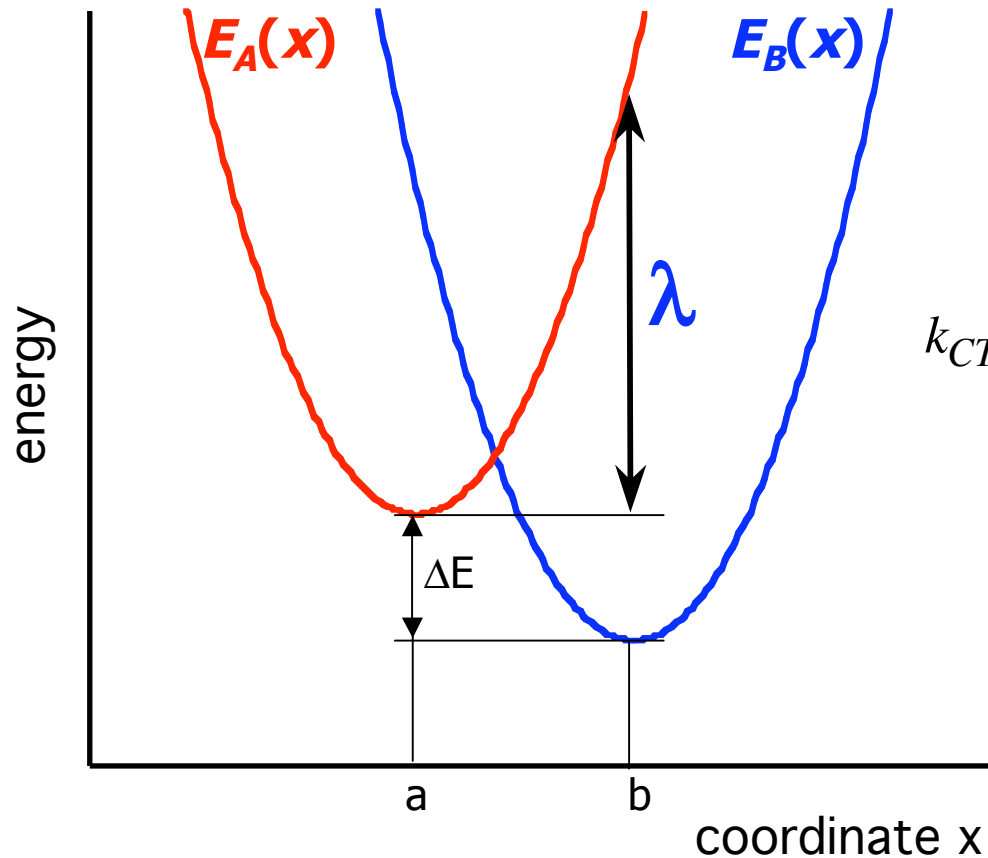
$$k_{CT} = \frac{2\pi}{\hbar} V^2 \sqrt{\frac{C}{2\pi k_B T}} \int \exp\left[-Cx^2/(2k_B T)\right] \delta(E_B(x) - E_A(x)) dx$$

$$y = Cbx$$

$$k_{CT} = \frac{2\pi}{\hbar} V^2 \sqrt{\frac{C}{2\pi k_B T}} \frac{1}{Cb} \int \exp\left[-y^2/(2Cb^2 k_B T)\right] \delta\left(\Delta E + \frac{Cb^2}{2} - y\right) dy$$

$$k_{CT} = \frac{2\pi}{\hbar} V^2 \sqrt{\frac{1}{2\pi k_B T C b^2}} \frac{1}{Cb} \exp\left[-\left(\Delta E + \frac{Cb^2}{2}\right)^2 / (2Cb^2 k_B T)\right]$$

Classical Marcus rate for charge transfer

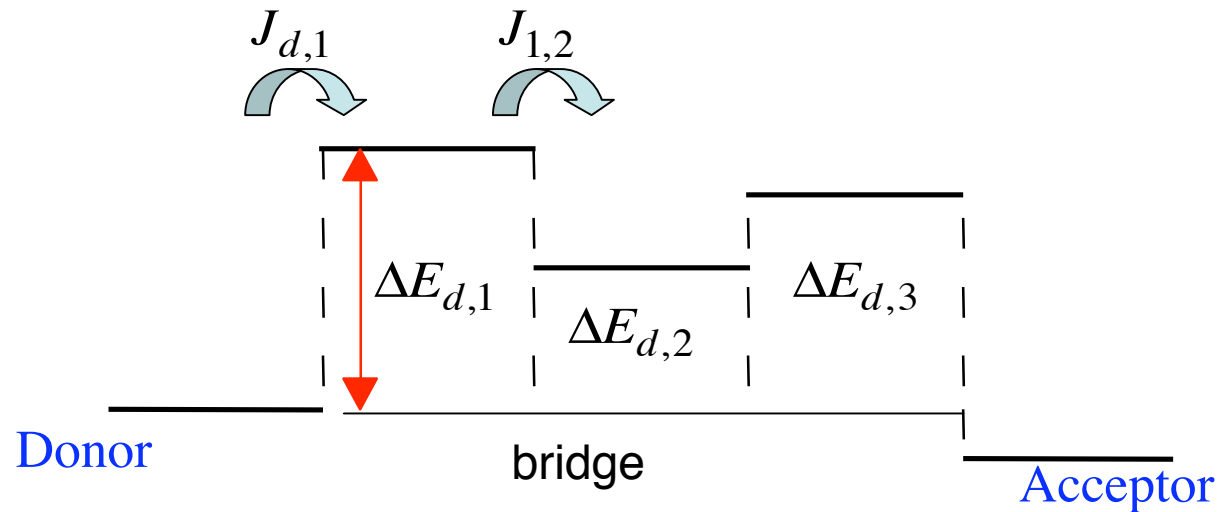


$$k_{CT} = \frac{2\pi}{\hbar} V^2 \sqrt{\frac{1}{4\pi\lambda k_B T}} \exp\left[-\frac{(\Delta E + \lambda)^2}{4\lambda k_B T}\right]$$

with the reorganization energy

$$\lambda = \frac{1}{2} C (b - a)^2 = \frac{1}{2} C b^2$$

Superexchange coupling V for tunneling through bridge



Superexchange coupling depends on J and ΔE ($J \ll \Delta E$):

$$V = \frac{J_{d,1} J_{n,a}}{\Delta E_{d,1}} \prod_{k=1}^{n-1} \frac{J_{k,k+1}}{\Delta E_{d,k+1}}$$

Exptl. rates reproduced with reorganization energy near 1 eV

| | Sequence | Exptl. rate K_{CT} (s^{-1}) | Coupling V (meV) | Reorg. energy λ (eV) |
|-----------|-------------------------|--------------------------------------|-----------------------|---------------------------------|
| 2b | 5'-AGAGGA- -TCTCCT- | 6.0×10^7 | 8.68 | 1.00 |
| 3b | 5'-AGTGGGA- -TCACCT- | 0.33×10^7 | 2.15 | 1.46 |
| 4c | 5'-TGAAGG- -ACTTCC- | 0.05×10^7 | 0.49 | 1.09 |
| 5b | 5'-TGACC- -ACTGG- | 0.09×10^7 | 0.42 | 1.00 |

Polaronic hopping mobility with $\lambda = 1$ eV



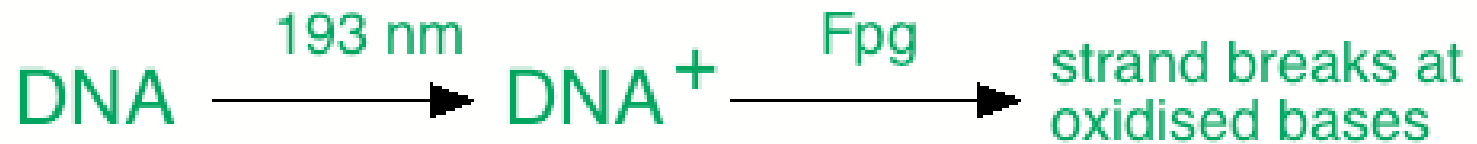
$$\mu = \frac{e}{kT} \frac{2\pi}{\hbar} \frac{|V|^2}{\sqrt{4\pi\lambda kT}} \exp\left(-\frac{\lambda}{4kT}\right) \delta^2 = 10^{-4} \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$$



$$\mu = 2 \cdot 10^{-5} \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$$

For $\lambda = 0$ mobility is few $\text{cm}^2 \text{ V}^{-1} \text{ s}^{-1}$; comparable with pentacene

Charge distribution on photo-oxidized DNA

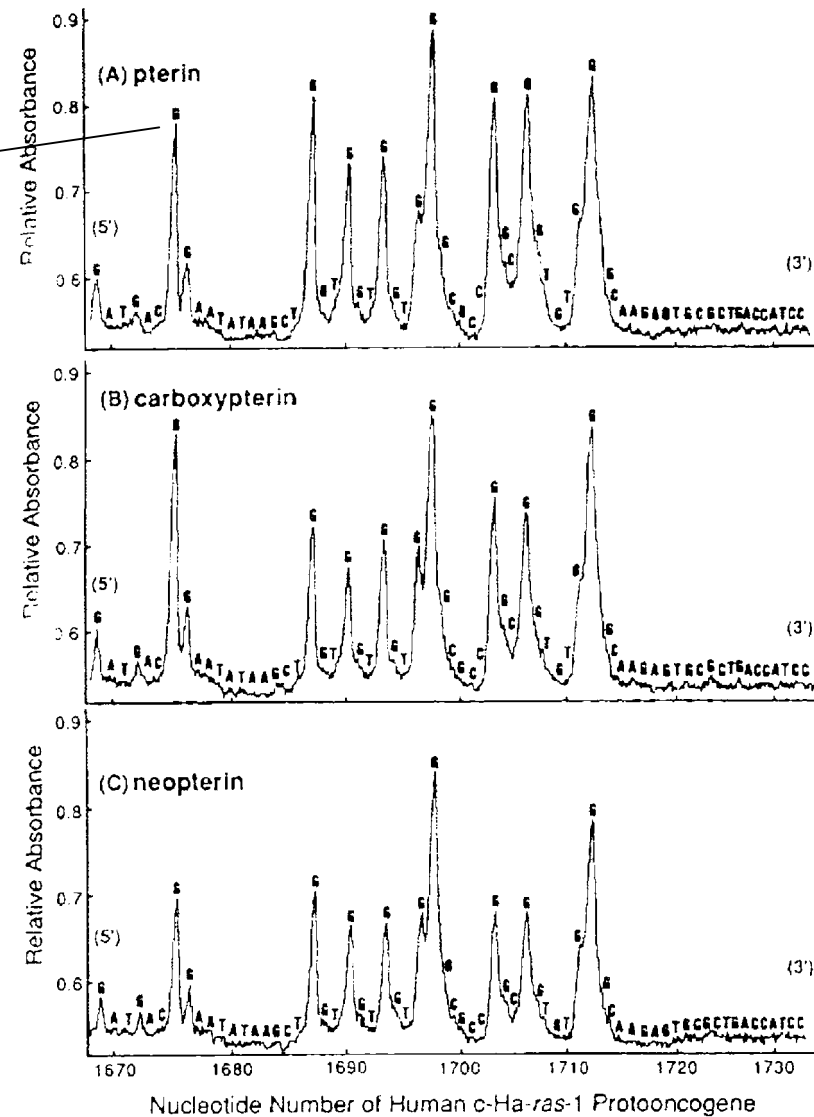


| BASE | ϵ (M ⁻¹ cm ⁻¹) | Φ | ION. PROB. | IP (VERT.) |
|------|--|--------|------------|------------|
| G | 25900 | 0.044 | 0.43 | 8.21 eV |
| C | 19500 | 0.029 | 0.22 | 8.88 eV |
| A | 18600 | 0.033 | 0.23 | 8.54 eV |
| T | 5700 | 0.055 | 0.12 | 9.16 eV |

Photocleavage is site-selective

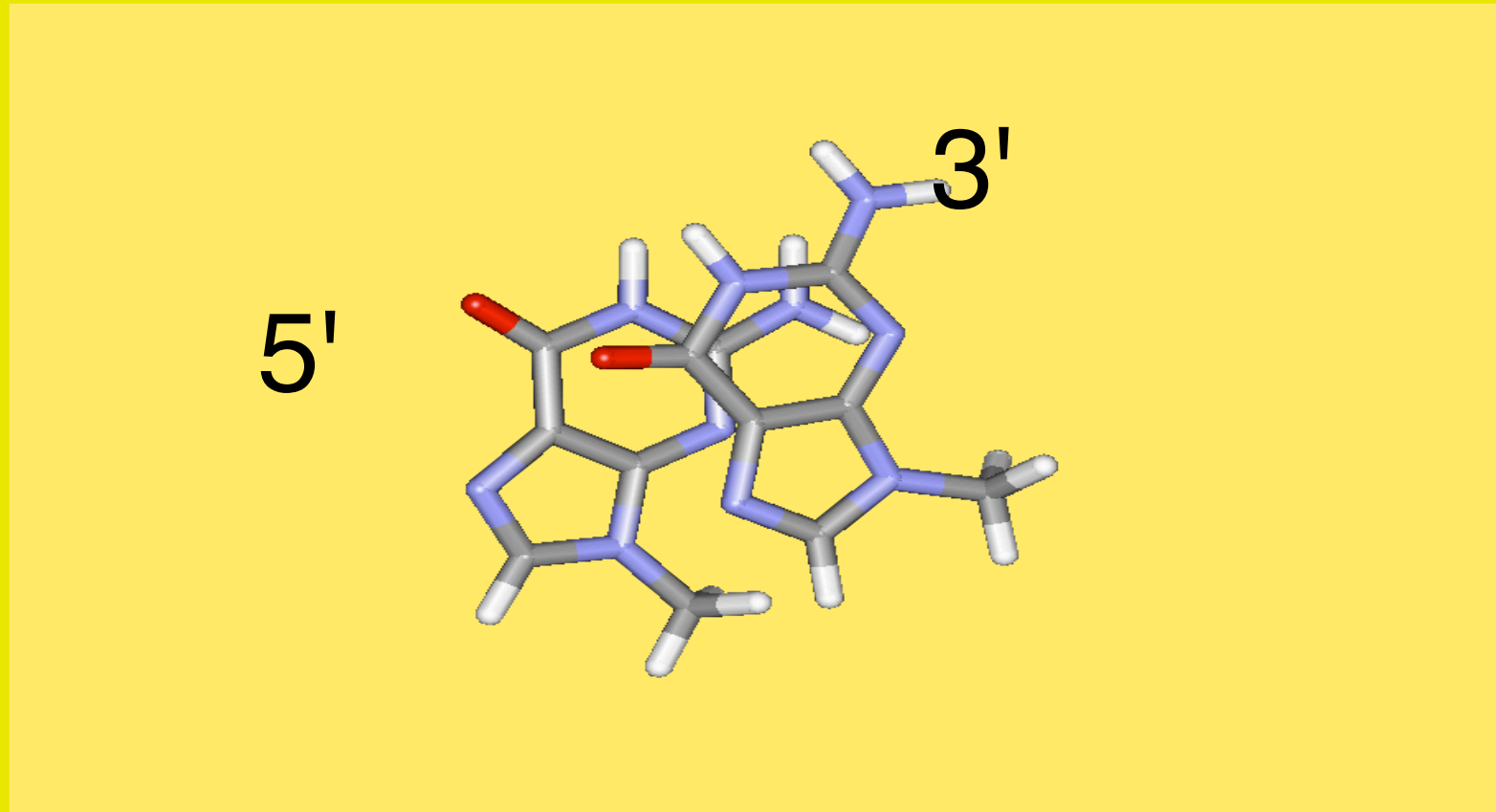
Ito *et al.* Bio. Chem. 36 (1997) 1774

5'-C**G**G**A**-3' ←
↓
G oxidized most



December 7, 2007

Energy of charge at 5' G and 3' G are different: site-selective photo-oxidation



5' and 3' guanine are in different environment

Site energy of 5' G lower than 3' G

$$E = \langle \Psi_{HOMO} | H | \Psi_{HOMO} \rangle$$

Charge

$$q_i = C_i^2 + C_i C_j S_{ij}$$

$$J_{GG} = 0.165 \text{ eV}$$

$$S_{GG} = 0.012$$

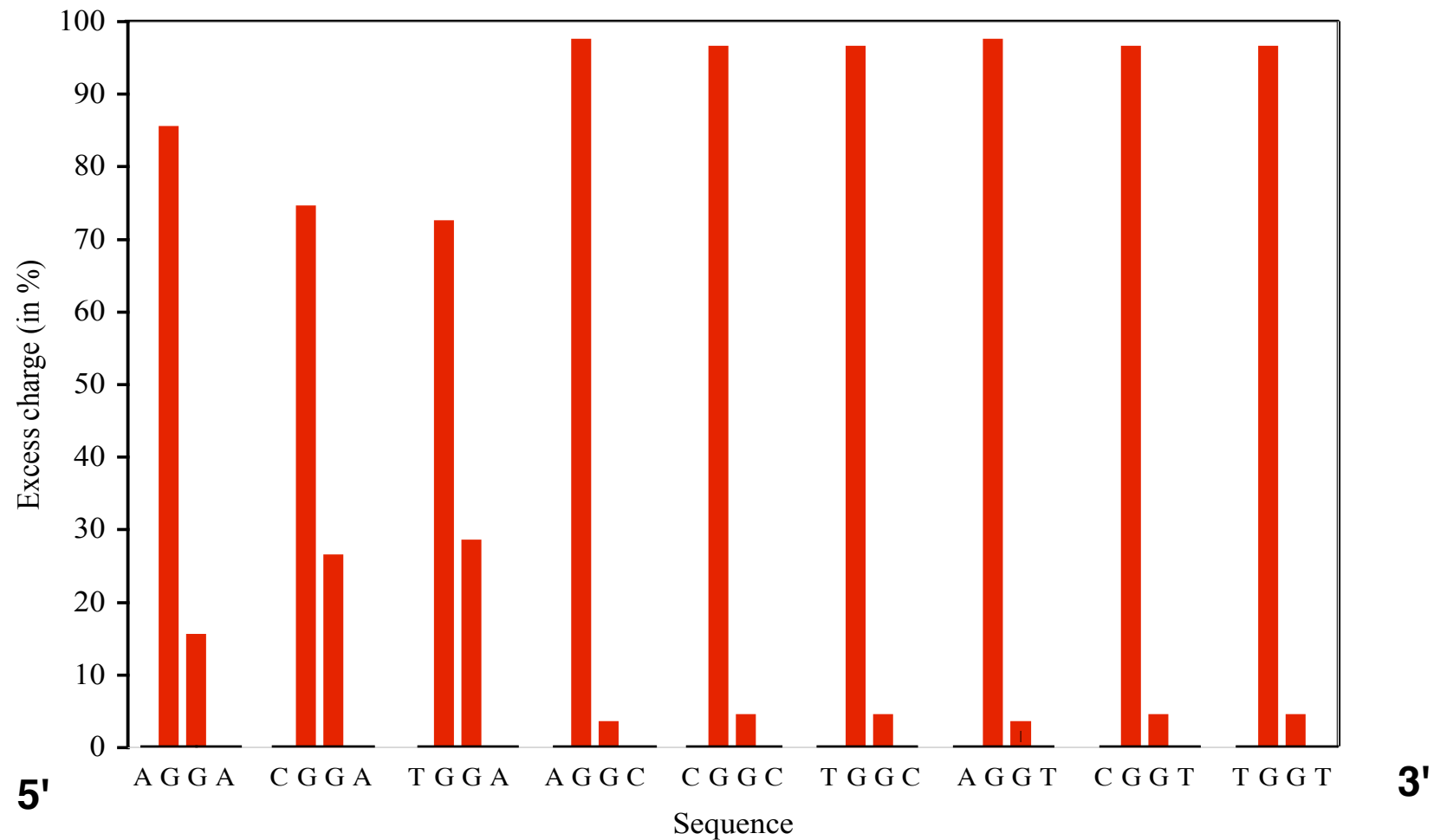
G site-energies in eV

| | | |
|---------------------|---------------------|---------------------|
| 7.90 8.04 | 7.90 8.31 | 7.90 8.29 |
| 5'-A GG A-3' | 5'-A GG C-3' | 5'-A GG T-3' |
| 3'-TCCT-5' | 3'-TCCG-5' | 3'-TCCA-5' |

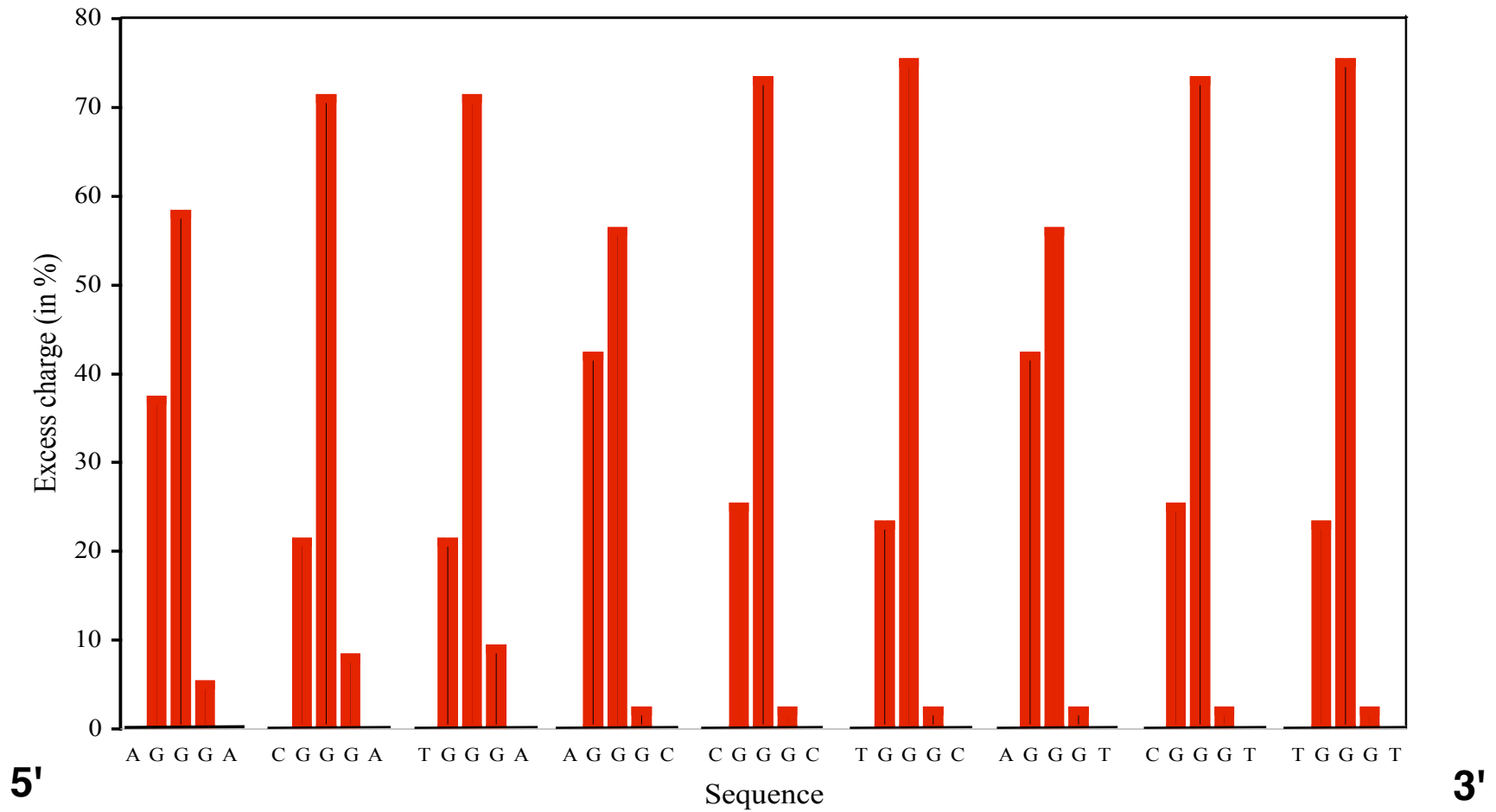
| | | |
|---------------------|---------------------|---------------------|
| 7.96 8.04 | 7.96 8.31 | 7.96 8.29 |
| 5'-C GG A-3' | 5'-C GG C-3' | 5'-C GG T-3' |
| 3'-GCCT-5' | 3'-GCCG-5' | 3'-GCCA-5' |

| | | |
|---------------------|---------------------|---------------------|
| 7.97 8.04 | 7.97 8.31 | 7.97 8.29 |
| 5'-T GG A-3' | 5'-T GG C-3' | 5'-T GG T-3' |
| 3'-ACCT-5' | 3'-ACCG-5' | 3'-ACCA-5' |

Charge distribution in 5'-XGGY-3' sequences



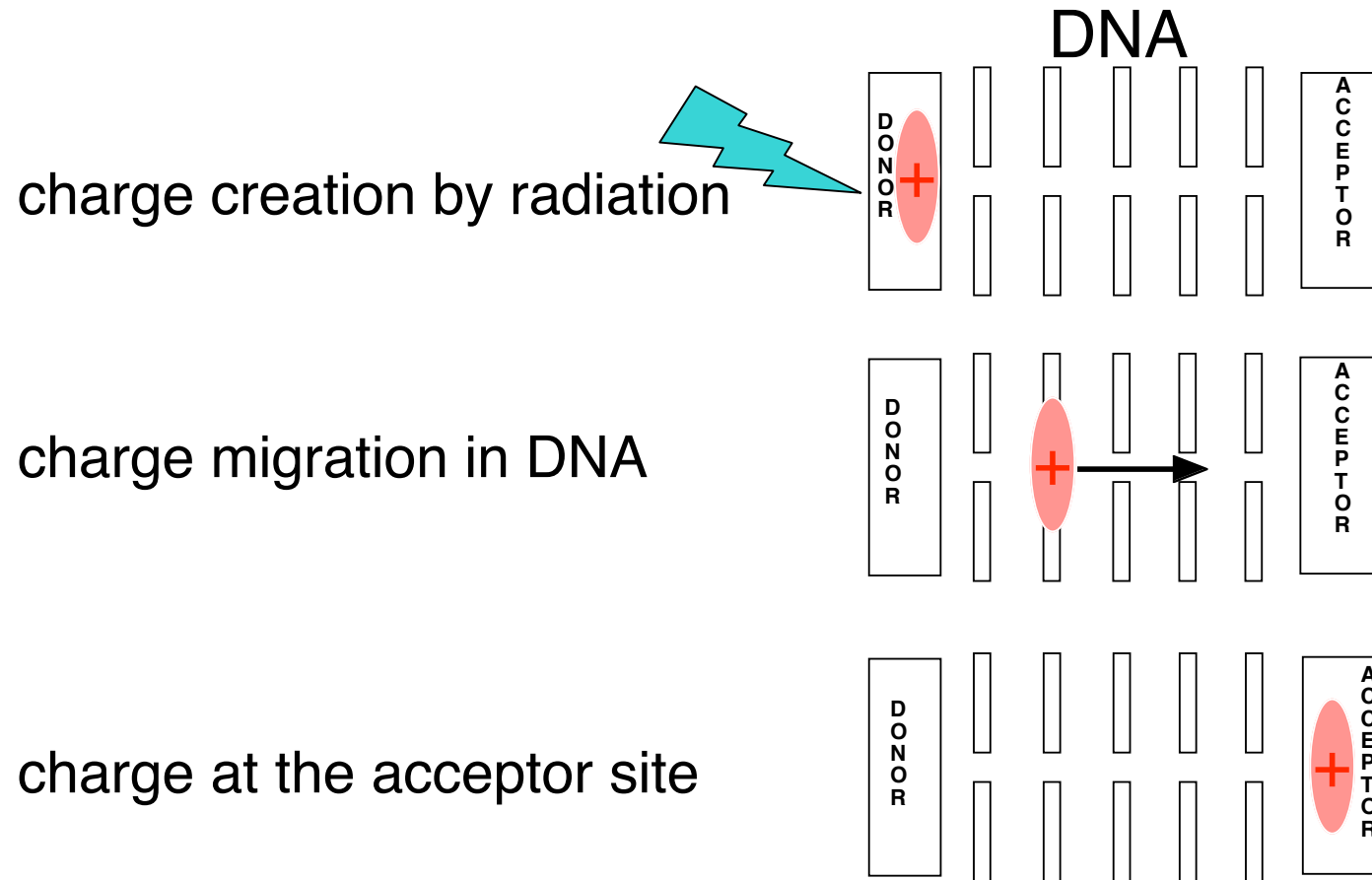
Charge distribution in 5'-XGGGY-3' sequences



Conclusions

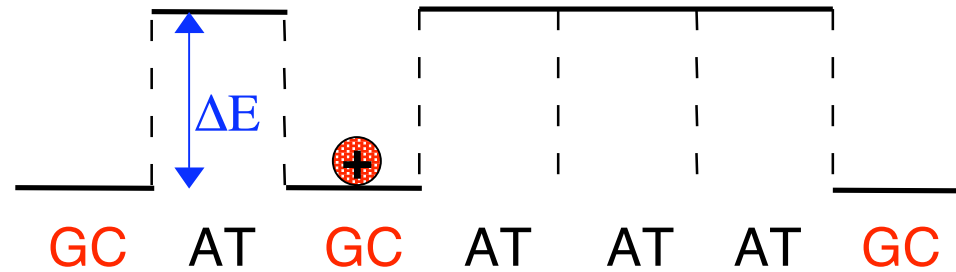
1. Distance and sequence dependence of charge transfer through donor-DNA-acceptor systems can be understood by tight-binding model
2. Experimental rate constants were reproduced with reorganization energy near 1 eV.
3. Mobility along GC (AT) stacks $\sim 10^{-4}$ ($\sim 10^{-5}$) cm^2/Vs
4. Selective photo-oxidation of specific G's due to different site-energies

Donor-DNA-Acceptor



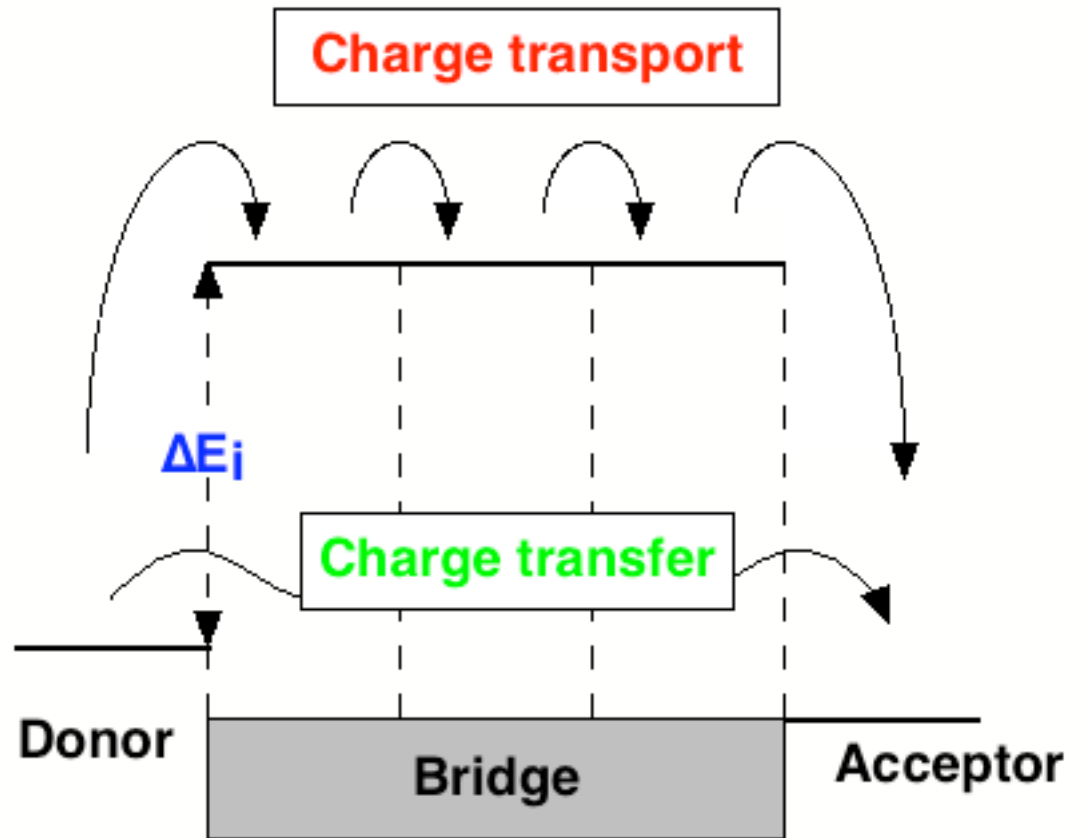
Positive charges reside on guanine

$\Delta E \sim 0.5 \text{ eV}$

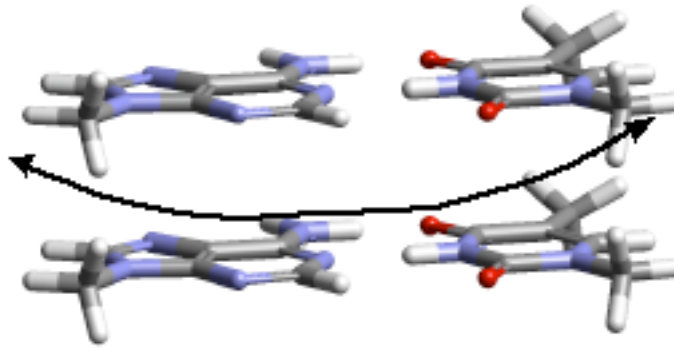


Tunneling vs. Hopping

- High β indicates single step tunneling transport
- Low β characteristic for hopping type transport



Theoretical model of charge transport via twisting base pairs



Twisting motion F_{rot}

Site energy of a nucleobase **B** in 5'-X**B**Y-3' triplets (X, B, Y = G, A, C, T)

| Y → | G | A | C | T |
|-------------|-------|-------|-------|-------|
| G GY | 7.890 | 8.040 | 8.310 | 8.290 |
| A GY | 7.900 | 8.060 | 8.341 | 8.320 |
| C GY | 7.957 | 8.115 | 8.383 | 8.361 |
| T GY | 7.965 | 8.124 | 8.407 | 8.380 |
| G AY | 8.343 | 8.487 | 8.716 | 8.712 |
| A AY | 8.376 | 8.558 | 8.763 | 8.799 |
| C AY | 8.438 | 8.584 | 8.800 | 8.793 |
| T AY | 8.434 | 8.630 | 8.810 | 8.858 |

| Y → | G | A | C | T |
|-------------|-------|-------|-------|-------|
| G CY | 9.446 | 9.637 | 9.857 | 9.870 |
| A CY | 9.441 | 9.630 | 9.851 | 9.867 |
| C CY | 9.490 | 9.667 | 9.882 | 9.917 |
| T CY | 9.499 | 9.679 | 9.895 | 9.925 |
| G TY | 9.111 | 9.308 | 9.557 | 9.533 |
| A TY | 9.130 | 9.370 | 9.578 | 9.586 |
| C TY | 9.268 | 9.451 | 9.701 | 9.662 |
| T TY | 9.273 | 9.499 | 9.705 | 9.699 |

* E strongly depends on neighboring bases